

# Towards Extreme-Scale Multiphysics Simulations for Induced Earthquakes

PASC22

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*TUM Uhrenturm*

# Induced Earthquakes

- Earthquakes caused by human activity
- Mining, geothermal energy production, carbon capture and storage, oil/gas extraction
- 1239 induced earthquakes in the HiQuake database<sup>1</sup>.
- Examples
  - Pohang 2017: M5.5 (Palgunadi et al. 2020)
  - Otaniemi 2018: < M2 (Hillers et al. 2020)

In order to understand these earthquakes better: Numerical simulations with SeisSol

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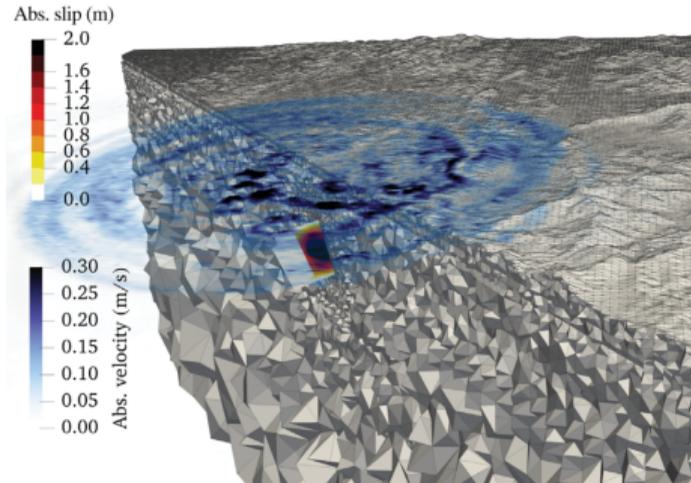
<sup>1</sup>Wilson et al. 2017: <https://inducedearthquakes.org/>, accessed 23<sup>rd</sup> June, 2022

# Earthquake simulations

Solve the elastic wave equation:

- $\partial_t q + A\partial_x q + B\partial_y q + C\partial_z q = 0$
- $q$  contains stresses and velocities,  $A$ ,  $B$  and  $C$  contain material information.

**Figure:** (Palgunadi et al. 2020):  
“Dynamic Fault Interaction during a  
Fluid-Injection-Induced Earthquake:  
The 2017 Mw 5.5 Pohang Event”

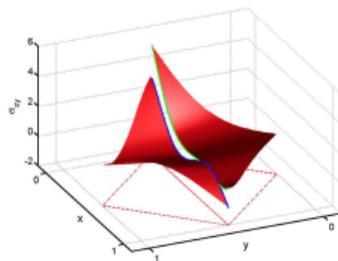


# SeisSol: ADER-DG for Earthquake simulations

Discontinuous Galerkin method with Arbitrary DERivatives time-stepping: ADER-DG: Achieve the same high order in space *and* time

SeisSol specific:

- Tetrahedral elements
- Modal (orthogonal) basis functions: Diagonal mass matrix, upper triangular stiffness matrix
- Exact Riemann solver for the numerical flux between elements



# HPC optimizations

## Parallelization

- Element local discretization with DG
- Mesh partitioning based on workload estimate
- Exchange values at partition boundaries

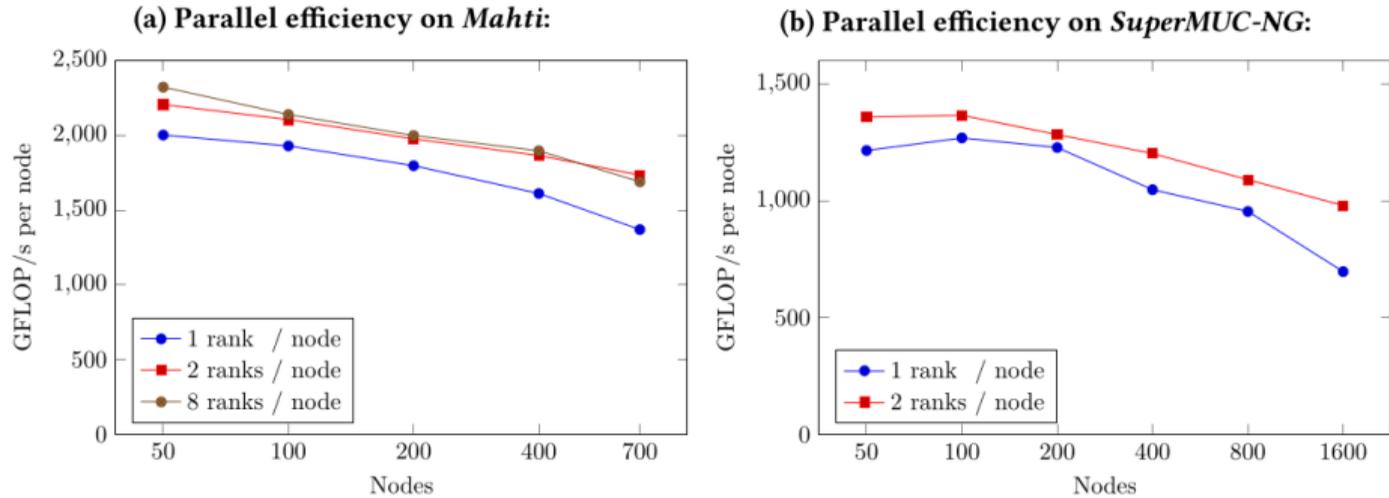
## Node-level performance

- Update scheme is a sequence of tensor contractions.
- Use code generator YATeTo<sup>2</sup> to map the tensor operations to GEMMs ( $C = \alpha AB + \beta C$ ).
- Use architecture specific backends for optimized code.

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<sup>2</sup>(Uphoff and Bader 2020)

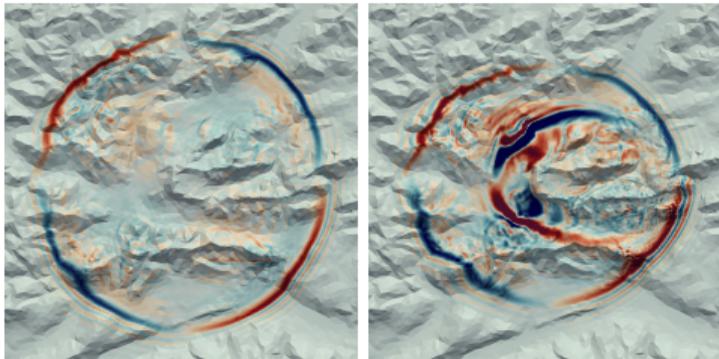
# Strong Scaling



**Figure:** Strong scaling on recent supercomputers. Image taken from (Krenz, Uphoff, et al. 2021).

# Anisotropic materials

- Directional dependent material behaviour, e.g. cracked or layered media
- Jacobian  $A$ ,  $B$ ,  $C$  are more densely populated, but can reuse the numerical scheme from the elastic wave equation (Wolf, Gabriel, and Bader 2020)



**Figure:** Left: isotropic material, Right: anisotropic material

Isotropic:

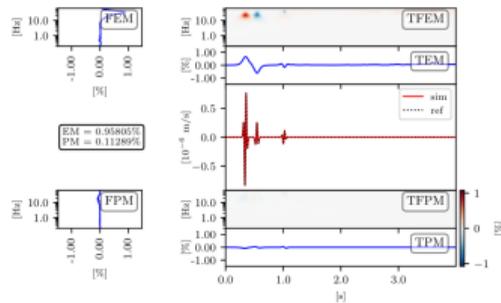
$$\sigma = \lambda \text{tr}(\epsilon) I + 2\mu \epsilon$$

Anisotropic:

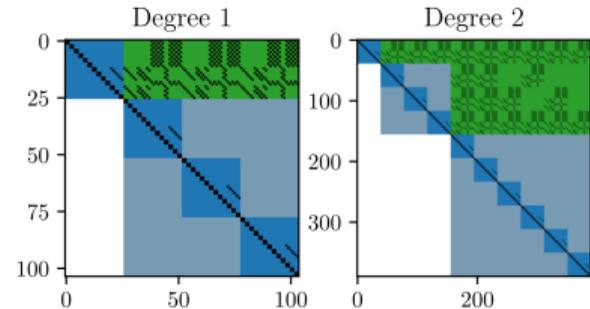
$$\sigma_{ij} = \sum_{k,l=1}^3 c_{ijkl} \epsilon_{kl}$$

# Poroelastic materials

- Interaction of fluid and solid phase introduces a stiff source term to the wave equation
- Replace Cauchy-Kowalevski procedure with space-time variant of ADER-DG
- Use sparsity pattern of the system matrix to efficiently solve the linear system (Wolf, Galis, et al. 2022)



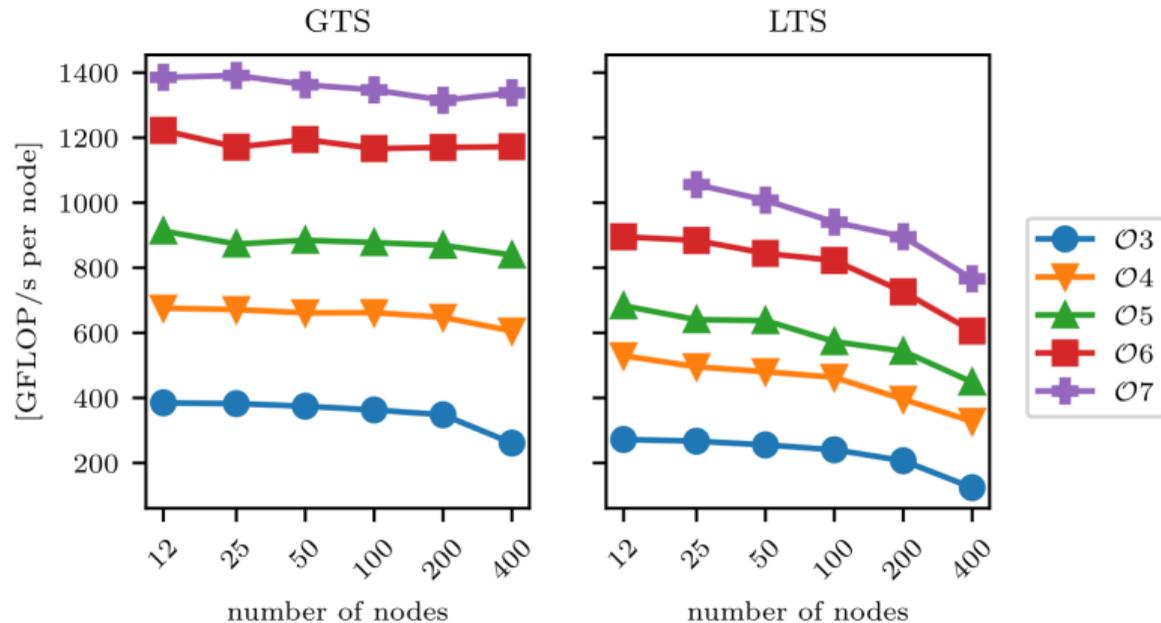
**Figure:** Double couple source in a poroelastic medium



**Figure:** Sparsity patterns for the space-time ADER-DG variant

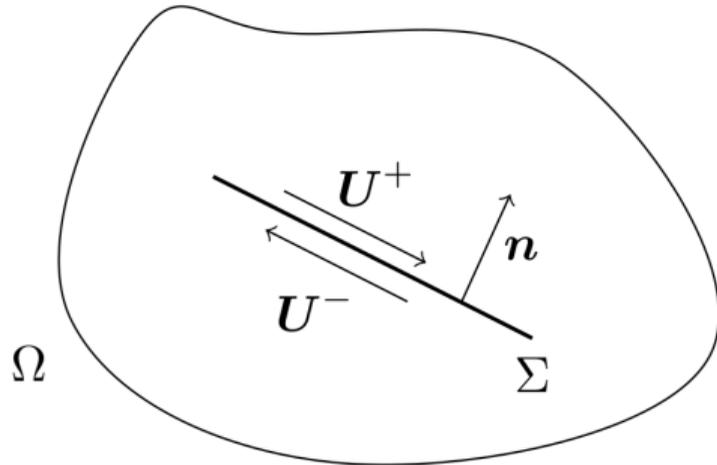
# Scalability

**Figure:** Parallel efficiency of a poroelastic setup with 7.3 million elements for global (GTS) and local (LTS) time-stepping on SuperMUC-NG.



# Kinematic earthquake sources

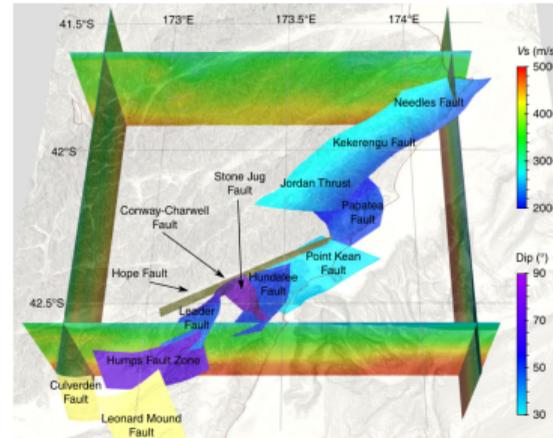
- Prescribe slip at a several points or along the complete fault fault.
- Watch how waves propagate through the medium.
- No information about what happens at the fault
- No interaction between wavefield and fault.



**Figure:** Sketch of an earthquake source along a fault. Image taken from (Uphoff 2020)

# Dynamic rupture earthquake sources

- Instead of numerical fluxes: Solve a friction problem at (selected) element interfaces.
- Interaction between wave propagation and source dynamics
- Gives insight into the rupture process
- Up to now dynamic rupture works only with (visco-)elastic materials.



**Figure:** Complicated fault network, image taken from (Ulrich et al. 2019).

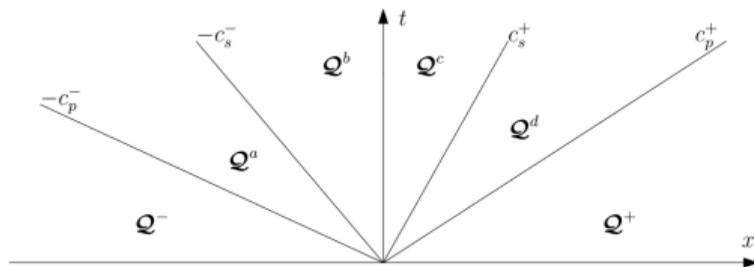
# Combine all the Multiphysics

**Elasticity + Pore Fluids + Friction Problem**

# How does Dynamic Rupture work in elastic media

## Elasticity + Pore Fluids + Friction Problem

1. Solve the Riemann problem to get states at the interface.
2. Compute fault strength  $\tau_S$  based on the friction law.
3. Find shear traction  $\mathbf{t}$  and slip rate  $\mathbf{s}$  such that  $\tau_S \mathbf{s} = \mathbf{t} \|\mathbf{s}\|$ .
4. Impose state with  $\mathbf{s}$  and  $\mathbf{t}$  at the interface.

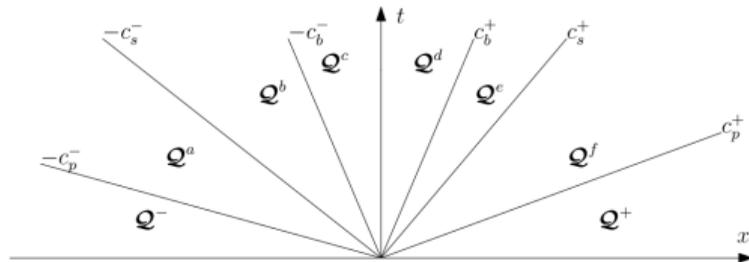


**Figure:** Solution structure of the elastic Riemann problem

# What do we need to change for poroelastic media

## Elasticity + Pore Fluids + Friction Problem

1. Fluid pressure now affects solution of the Riemann problem.
2. Fault strength depends on the pressure (and temperature)<sup>3</sup>.
3. Find shear traction  $\mathbf{t}$  and slip rate  $\mathbf{s}$ , but what about relative fluid velocity?

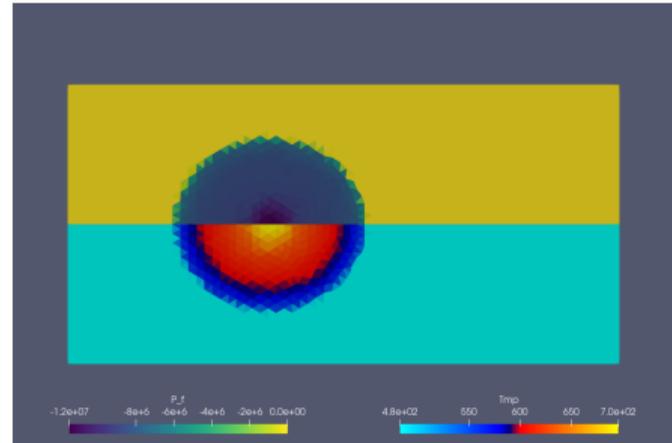
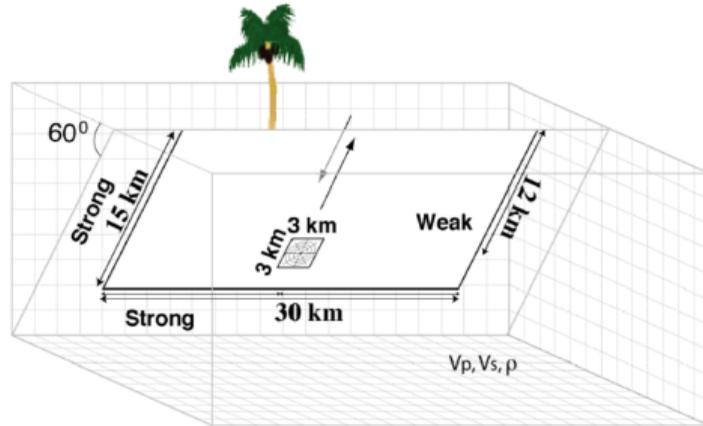


**Figure:** Solution structure of the poroelastic Riemann problem

<sup>3</sup>(Noda and Lapusta 2010)

## How to verify the results?

- Hard to find analytic solutions for combined friction and wave propagation problem.
- Community effort through SCEC to compare different dynamic rupture codes.



**Figure:** Left: Geometry of the SCEC benchmark TPV12. Image taken from (Harris et al. 2009). Right: Results of the TPV105 benchmark (top: pressure, bottom: temperature).

# Conclusion

- Extended SeisSol's functionality to incorporate more complicated material models.
- Work in progress: Dynamic Rupture in poroelastic materials.
- Upcoming work: Compute, compute, compute

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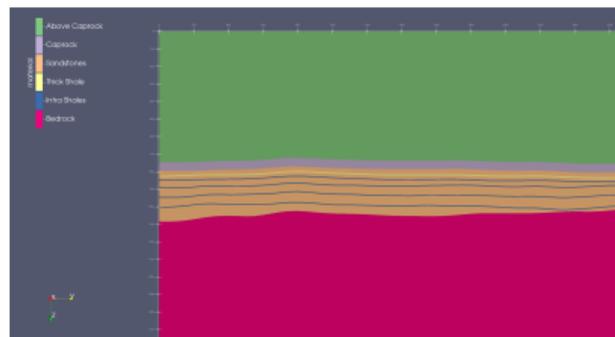
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## Quantify poroelastic effects relevant for wave propagation

- Compare poroelastic materials with their elastic equivalents
- Study the Utsira sandstone formation used for CCS<sup>4</sup>
- Energy dissipation at material interfaces.



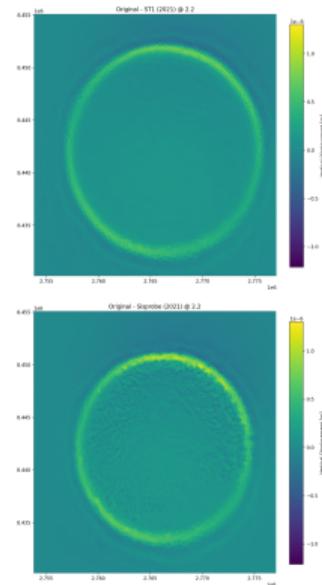
**Figure:** Cut through the layered Utsira model.

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<sup>4</sup>Equinor 2022

# Nuisance patterns from the stimulation of Enhanced Geothermal systems

- Geothermal Energy production near Helsinki: Neighbors reported sound disturbance connected to induced earthquakes.
- We used the elastic-acoustic coupling feature of SeisSol to simulate which sounds an earthquake emits.
- Parameter study: How does the source mechanism and the geological subsurface structure influence the nuisance pattern? (Krenz, Wolf, et al. 2022).



# Backup Slide Equations

Weak formulation of the PDE in 1D:

$$\int_T \partial_t \mathbf{q} \cdot \phi \, d\mathbf{x} - \int_T \mathbf{A} \mathbf{q} \partial_x \phi \, d\mathbf{x} + \int_{\partial T} \phi \mathbf{A} \mathbf{q} \cdot \mathbf{n} \, ds = \int_T \mathbf{E} \mathbf{q} \phi \, d\mathbf{x}$$

Semidiscrete form:

$$\begin{aligned} & \partial_t \mathbf{Q}_{pl} \int_T \phi_l \phi_k \, d\mathbf{x} - \mathbf{A}_{pq} \mathbf{Q}_{pl} \int_T \phi_l \partial_x \phi_k \, d\mathbf{x} \\ & + \int_{\partial T} F_{pk}(\mathbf{Q}_{pl}, \mathbf{Q}_{pl}^i) \, ds \\ & = \mathbf{E}_{pq} \mathbf{Q}_{pl} \int_T \phi_l \phi_k \, d\mathbf{x} \end{aligned}$$