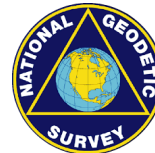
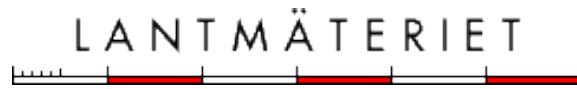


IHRF2019: the first realisation of the International Height Reference System

L Sánchez, J Ågren, J Huang, YM Wang, J Mäkinen, H Denker, J Ihde, H Abd-Elmotaal, K Ahlgren, M Amos, R Barzaghi, T Bašić, D Blitzkow, D Carrion, S Claessens, B Erol, S Erol, M Filmer, R Forsberg, VN Grigoriadis, M Serkan Işık, T Jiang, X Li, Q Liu, ACOC Matos, K Matsuo, P Novák, R Pail, M Pitoňák D. Roman, M Schmitd, M Sideris, M Varga, GS Vergos, M Véronneau, M Willberg, C Zhang, P Zingerle



IUGG General Assembly 2019
Montreal, Canada, July 12, 2019

Introduction

A reference frame realises a reference system in two ways:

- physically, by a **solid materialisation of points** (or observing instruments),
- mathematically, by the **determination of coordinates** referring to that reference system.
- The coordinates of the points are computed from the measurements following the definition of the reference system.

In July 2015, the IAG released a resolution for the “**Definition and Realisation of a International Height Reference System (IHR)**”. During the last four years different actions have been conducted to

- Establish a global **reference network** for the IHR realisation: the International Height Reference Frame (IHRF)
- Evaluate different **strategies for the determination of reference coordinates** at the reference stations
- Identify **required standards, conventions and procedures** needed to ensure consistency between the definition (IHR) and the realisation (IHRF).

Introduction

Results presented here are a joint effort of

- GGOS JWG: [Strategy for the realisation of the IHRS](#) (chair: L Sánchez)
- IAG JWG 2.2.2: [The 1 cm geoid experiment](#) (chair: YM Wang)
- IAG SC 2.2: [Methodology for geoid and physical height systems](#) (chair: J Ågren)
- ICCT JSG 0.15: [Regional geoid/quasi-geoid modelling - Theoretical framework for the sub-centimetre accuracy](#) (chair: J Huang)
- IAG JWG 2.1.1: [Establishment of a global absolute gravity reference system](#) (chair: H Wziontek)
- IAG regional sub-commissions for reference frames and geoid modelling
- IAG Commission 2 – Gravity Field (chair R Pail)
- International Gravity Field Service – IGFS (chair R Barzaghi)
- GGOS Bureaus of Networks and Observations – GGOS-BNO (chair: M Pearlman) and Products and Standards – GGOS-BPS (chair: D Angermann)

Outline

- Definition of the International Height Reference System (IHR)
- Some considerations for the determination of IHR/IHRF coordinates
- Colorado experiment: comparison of potential values and learnings from a successful international cooperation initiative
- International Height Reference Frame (IHRF): station selection for the reference network and first computations of reference coordinates
- Outlook

International Height Reference System (IHRIS)

IAG Resolution No. 1, Prague, July 2015

- 1) Vertical coordinates are **potential differences** with respect to a **conventionally fixed W_0** value:

$$C_P = C(P) = W_0 - W(P) = -\Delta W(P)$$

$$W_0 = \text{const.} = 62\,636\,853.4 \text{ m}^2\text{s}^{-2}$$

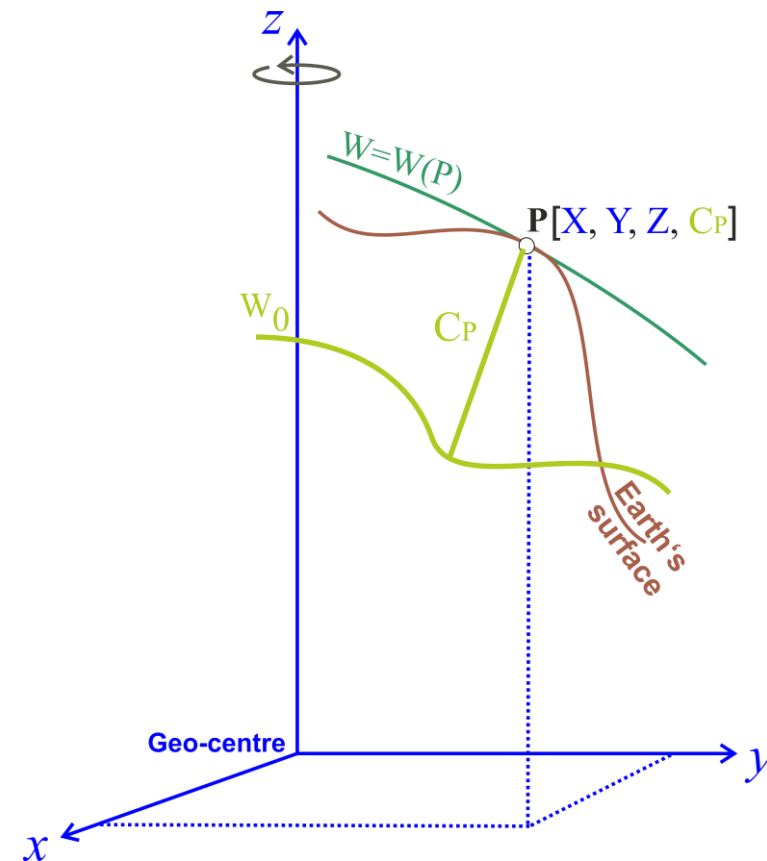
- 2) The position P is given in the ITRF

$$\mathbf{X}_P (X_P, Y_P, Z_P); \text{ i.e., } W(P) = W(\mathbf{X}_P)$$

- 3) The estimation of $\mathbf{X}(P)$, $W(P)$ (or $C(P)$) includes their variation with time; i.e., $\dot{\mathbf{X}}(P)$, $\dot{W}(P)$ (or $\dot{C}(P)$).

- 4) Coordinates are given in **mean-tide system / mean (zero) crust**.

- 5) The unit of length is the **meter** and the unit of time is the **second (SI)**.



See: Ihde J. et al.: *Definition and proposed realization of the International Height Reference System (IHRIS)*. *Surv Geophy* 38(3), 549-570, 10.1007/s10712-017-9409-3, 2017

Basic considerations on the IHRF/IHRF coordinates

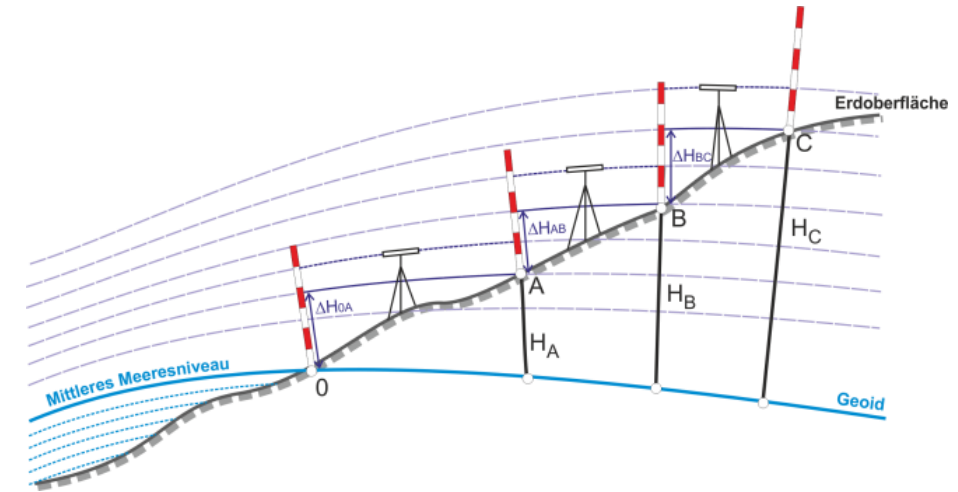
- 1) The IHRF/IHRF is
 - a combination of a geometric component given by the **coordinate vector \mathbf{X}** in the ITRS/IHRF and
 - a physical component given by the determination of **potential values W** at \mathbf{X} .
- 2) The determination of \mathbf{X} follows the **IERS Conventions** and will not be further considered here.
- 3) According to the **GGOS Terms of Reference**, the expected accuracy of W is
 - Positions: $\approx \pm 3 \times 10^{-2} \text{ m}^2\text{s}^{-2}$ (about **3 mm**)
 - Velocities: $\approx \pm 3 \times 10^{-3} \text{ m}^2\text{s}^{-2}/\text{a}$ (about **0.3 mm/a**)
- 4) For the moment, our goal is $\pm 1 \times 10^{-1} \text{ m}^2\text{s}^{-2}$ (about **1 cm**)
- 5) The IHRF/IHRF coordinates include the determination of time variations. For the moment, we consider **static coordinates only**.

Possibilities for the determination of potential values

1) Geopotential numbers inferred from levelling and gravity reductions:

$$W_P = (W_0^{local} + \delta W) - C_P; \quad \delta W = W_0^{IHRF} - W_0^{local}; \quad C_P = \int_0^P g \, dn$$

- Vertical datum unification is required to determine δW
- Reliability depends on the limitations of the existing height systems, in particular
 - the strong accumulation of systematic errors in levelling, and
 - the impossibility of referring the levelled heights to a specific epoch
- This approach is useful for the transformation of the existing height systems to the IHRF, but it may be unsuitable for the precise realisation of the IHRF.



Possibilities for the determination of potential values

2) Global Gravity Models of high degree (GGM-HD)

like the EGM2008 model (Pavlis et al., 2012, 2013) or the EIGEN-C series (e.g., Förste et al., 2012; 2014)

$$W(X, Y, Z) = \frac{GM}{r} \left[1 + \sum_{n=1}^{\infty} \left(\frac{a}{r} \right)^n \sum_{m=0}^n [C_{nm} \cos m\lambda + S_{nm} \sin m\lambda] P_{nm}(\cos\theta) \right] + \frac{1}{2} \omega^2 r^2 \cos(90^\circ - \theta)$$

- Expected accuracy (Rummel et al., 2014)
 - well surveyed regions: $\pm 0.4 \text{ m}^2\text{s}^{-2}$ to $\pm 0.6 \text{ m}^2\text{s}^{-2}$ (equivalent to $\pm 4 \text{ cm}$ to $\pm 6 \text{ cm}$)
 - sparsely surveyed regions: from $\pm 2 \text{ m}^2\text{s}^{-2}$... $\pm 4 \text{ m}^2\text{s}^{-2}$ ($\pm 20 \text{ cm}$ to $\pm 40 \text{ cm}$) to $\pm 10 \text{ m}^2\text{s}^{-2}$ ($\pm 1 \text{ m}$)
- This approach represents the “ideal way” to estimate potential values and hopefully, we will get a better accuracy in the next future. Ongoing studies with high expectation of improvement:
 - Combination of GGM with gravity effects of global topography (e.g. Gruber and Willberg, Signal and error assessment of GOCE-based high resolution gravity models, IUGG19-0157)
 - EGM2020

Possibilities for the determination of potential values

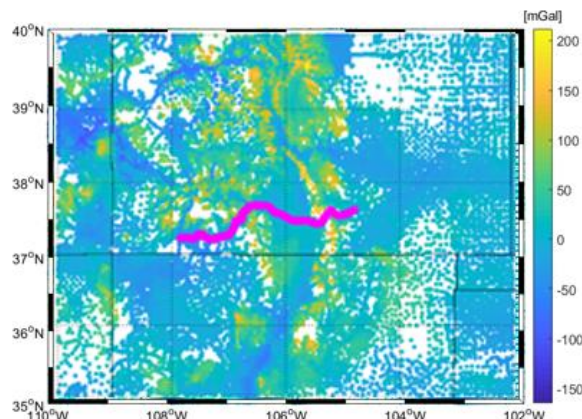
3) Disturbing potential

$$W_P = U_P + T_P \quad ; \quad T_P = T_{P,satellite-only} + T_{P,residual} + T_{P,terrain}$$

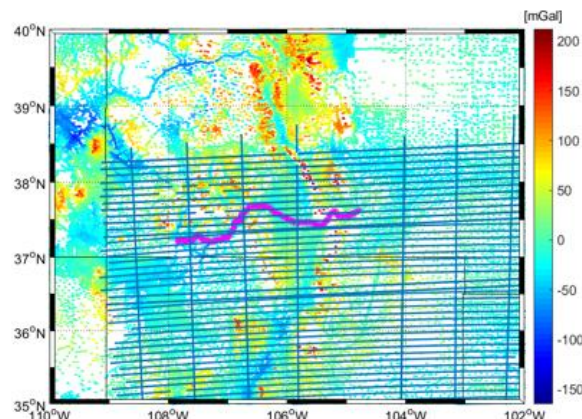
- GGM based on SLR, GRACE and GOCE are **very precise** ($\pm 1 \dots \pm 2$ cm @ 100 km)
- Mean omission error globally: $\approx \pm 45$ cm
- Goal is to **reduce these ± 45 cm to ± 1 cm** (only possible using terrestrial gravity data and considering topographic effects)
- The potential values realising the ITRS coordinates must be determined at the reference stations; i.e., at the Earth's surface and not at the geoid
 - With Molodensky's approach, the determination of W_P is straightforward
 - With Stokes' approach, the potential values should be 'moved' to the Earth's surface using the same hypotheses applied to reduce the observed gravity values to the geoid
- The determination of T_P demands a series of approximations, which influence the results; i.e., **different methodologies produce different potential values**

Comparison of computation methods

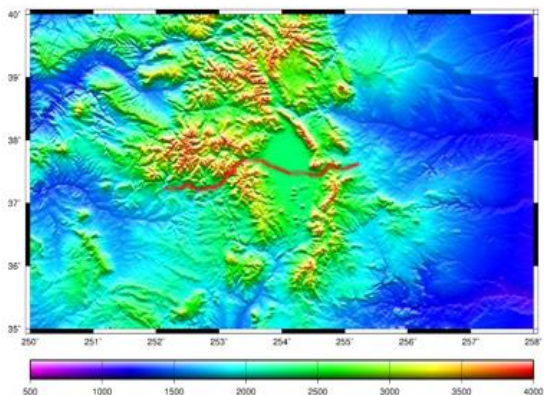
Colorado experiment: to compute geoid, quasi-geoid and potential values using exactly the same input data, a set of basic standards, and the own methodologies (software) of colleagues involved in the gravity field modelling.



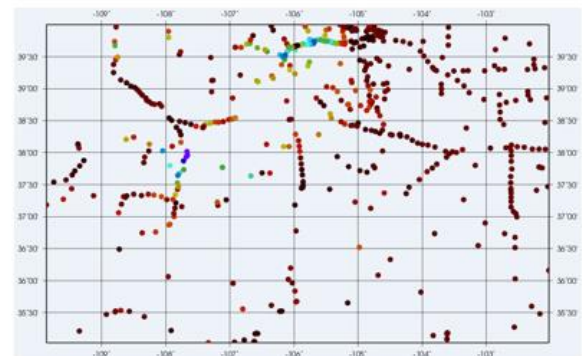
Surface gravity data (59,303 points)



Airborne gravity data
(41 lines E-W, 7 lines N-S)



Terrain model: SMRT V4.1



NGS *historical* GPS/levelling (510 points)

- Initiated in July 2017
- Data provided by US NGS
- Standards prepared by L Sánchez, J Ågren, J Huang, YM Wang, R Forsberg
- Three computations (two iterations) finished in June 2019
- Fifteen (final) contributing solutions
- Computation methods and comparison of geoid and quasi-geoid models in [Sessions G02h and G02i](#)

Colorado experiment: contributing solutions



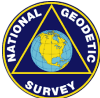
Faculty of Engineering, Minia University, [Egypt](#)



İstanbul Teknik Üniversitesi, Istanbul, [Turkey](#)



Department of Geodesy and Surveying, Aristotle University of Thessaloniki, Thessaloniki, [Greece](#)



National Geodetic Survey, [USA](#)



Natural Resources Canada, [Canada](#)



Lantmäteriet, Swedish mapping, cadastral and land registration authority, [Sweden](#)



School of Earth and Planetary Sciences and The Institute for Geoscience Research, Curtin University, [Australia](#)



Escola Politécnica, Universidade de São Paulo; Centro de Estudos de Geodesia, [Brazil](#)



Deutsches Geodätisches Forschungsinstitut, Technische Universität München, [Germany](#)



Ingenieurinstitut für Astronomische und Physikalische Geodäsie, Technische Universität München, [Germany](#)



Chinese Academy of Surveying and Mapping, [China](#)



Politecnico de Milano, [Italy](#)



Faculty of Geodesy, University of Zagreb, [Croatia](#) - Research Institute of Geodesy, Topography and Cartography, [Czech Republic](#)



National Space Institute, Technical University of Denmark, [Denmark](#)



Geography and Crustal Dynamics Research Center, Geospatial Information Authority of Japan, [Japan](#)

Colorado experiment: summary of approaches and models

- Least squares modification of Stokes' formula with additive corrections (2)
- Least squares modification of Stokes' formula with additive corrections and biased Stokes' kernel modification
- Stokes' formula with Wong-Gore modification and 1D-FFT (2)
- Spherical radial basis functions
- Least squares collocation
- Fast collocation based on gravity gridded data
- Degree weighted Stokes' integral
- Modified degree-banded Stokes' kernel (2)
- Spherical FFT with modified Wong-Core Stokes' kernel
- UNB Stokes-Helmert scheme
- UNB Stokes-Helmert scheme with hybrid-Meissl-Molodensky modified spheroidal Stokes' kernel
- NGS Molodensky approach, Spherical Harmonics Analysis (SHA)
- GGMs: GOCO05s, XGM2016, XGM2018, xGEOID17B, EIGEN-6C4, EGM2008
- Topographic effects based on SRTM V4.1, EARTH2014, COLH19M05, ERTM2160
- 12 solutions based on height anomalies, 3 solutions based on geoid undulations

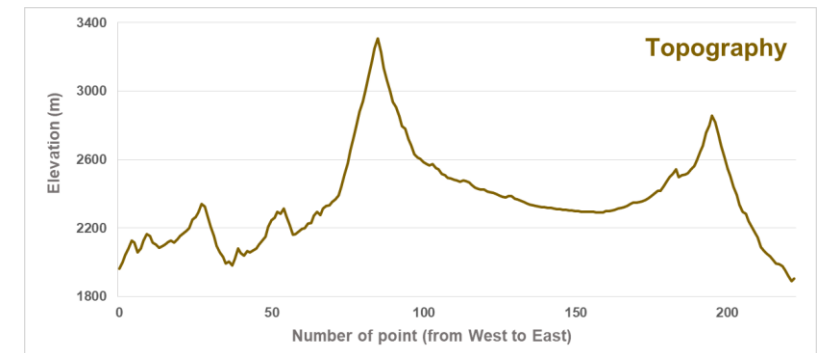
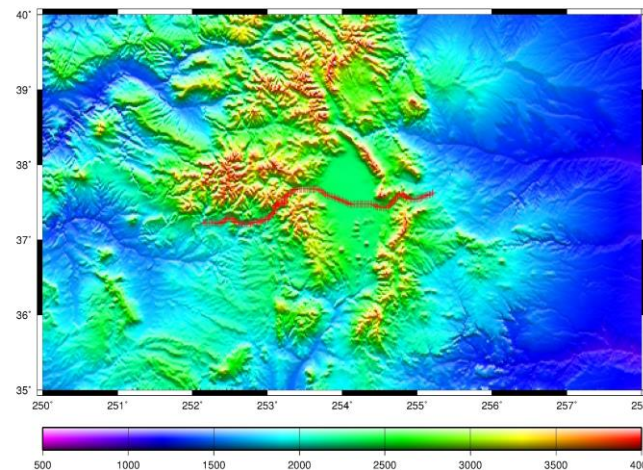
Colorado experiment: comparison of potential values

- 1) The comparison is carried out at 223 GSVS17 marks (Geoid Slope Validation Survey 2017) selected by NGS
- 2) Participants in the experiment got φ , λ , h ; levelling is not available (yet)
- 3) The potential values provided by the different solutions are converted to **geopotential numbers** with respect to the IHRM W_0 value

$$C(P) = W_0 - W(P) \quad ; \quad W_0 = 62\,636\,853.4 \text{ m}^2\text{s}^{-2}$$

- 4) and further transformed to **normal heights** (to see the differences in meters):

$$H^*(P) = C(P)/\gamma(P)$$



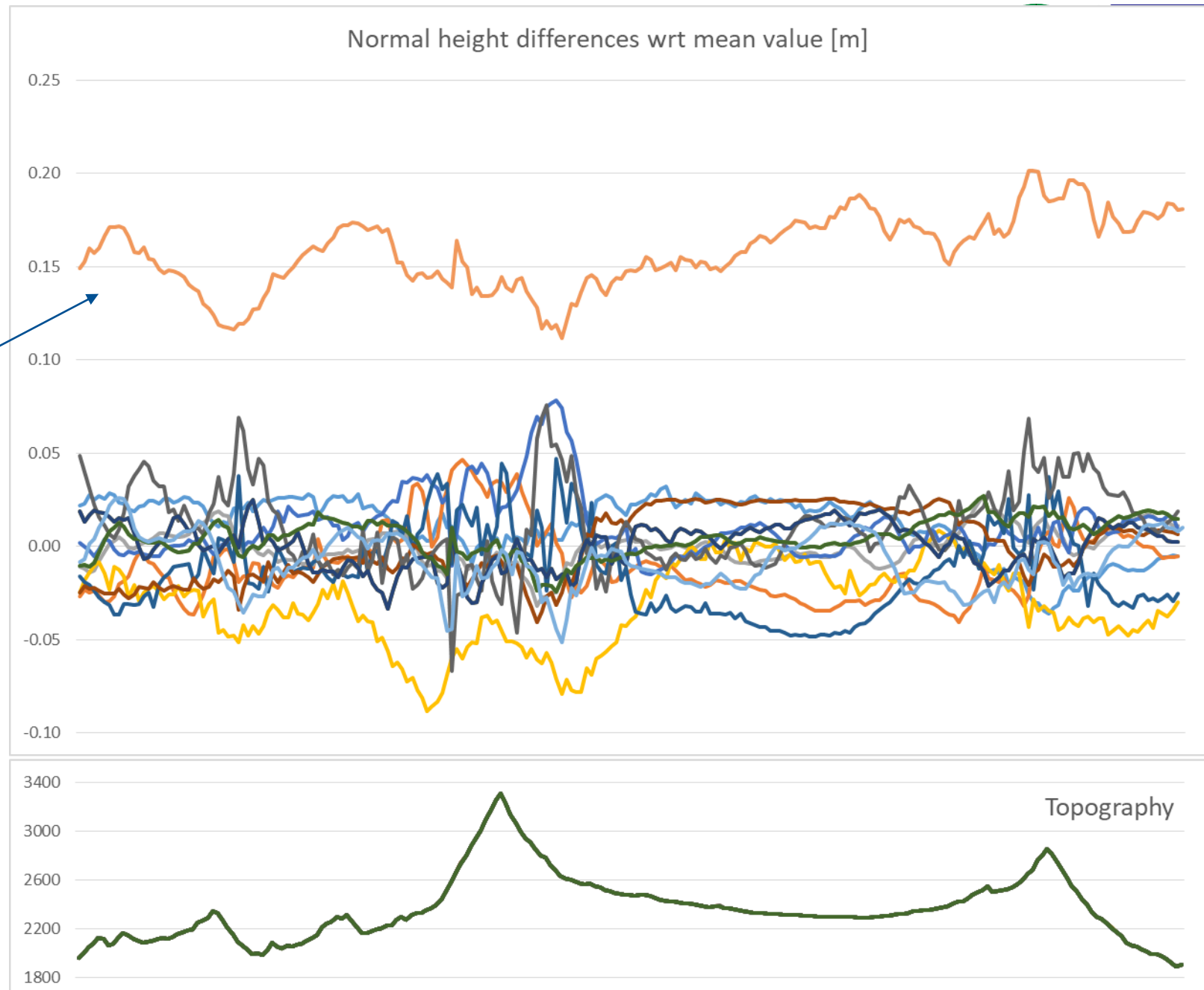
Colorado experiment: comparison of potential values

Normal height difference [cm]
(individual contribution – mean)

Outlier 1
Mean : 15.7 ± 1.9 cm
Range: 8.9 (11.2 ... 20.0)

Zero-degree term: 17.85 cm

$$\zeta_0 = \frac{(GM_{\text{GGM}} - GM_{\text{GRS80}})}{r_P \cdot \gamma_Q} - \frac{\Delta W_0}{\gamma_Q}$$



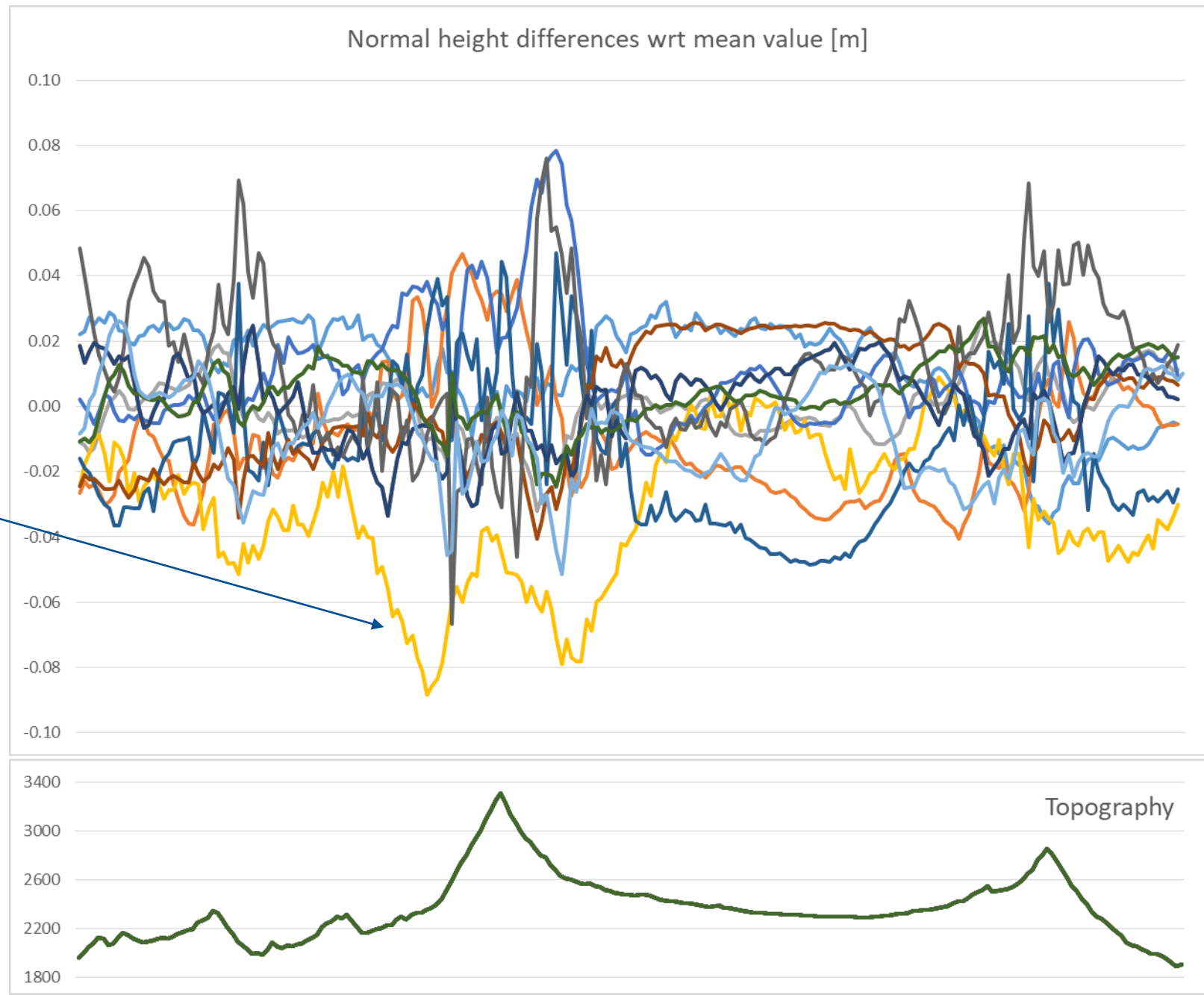
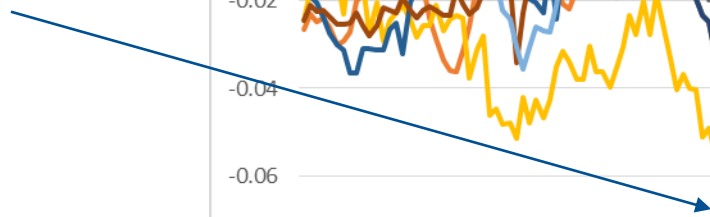
Colorado experiment: comparison of potential values

Normal height difference [cm]
(individual contribution – mean)

Outlier 2

Mean : -3.2 ± 2.1 cm

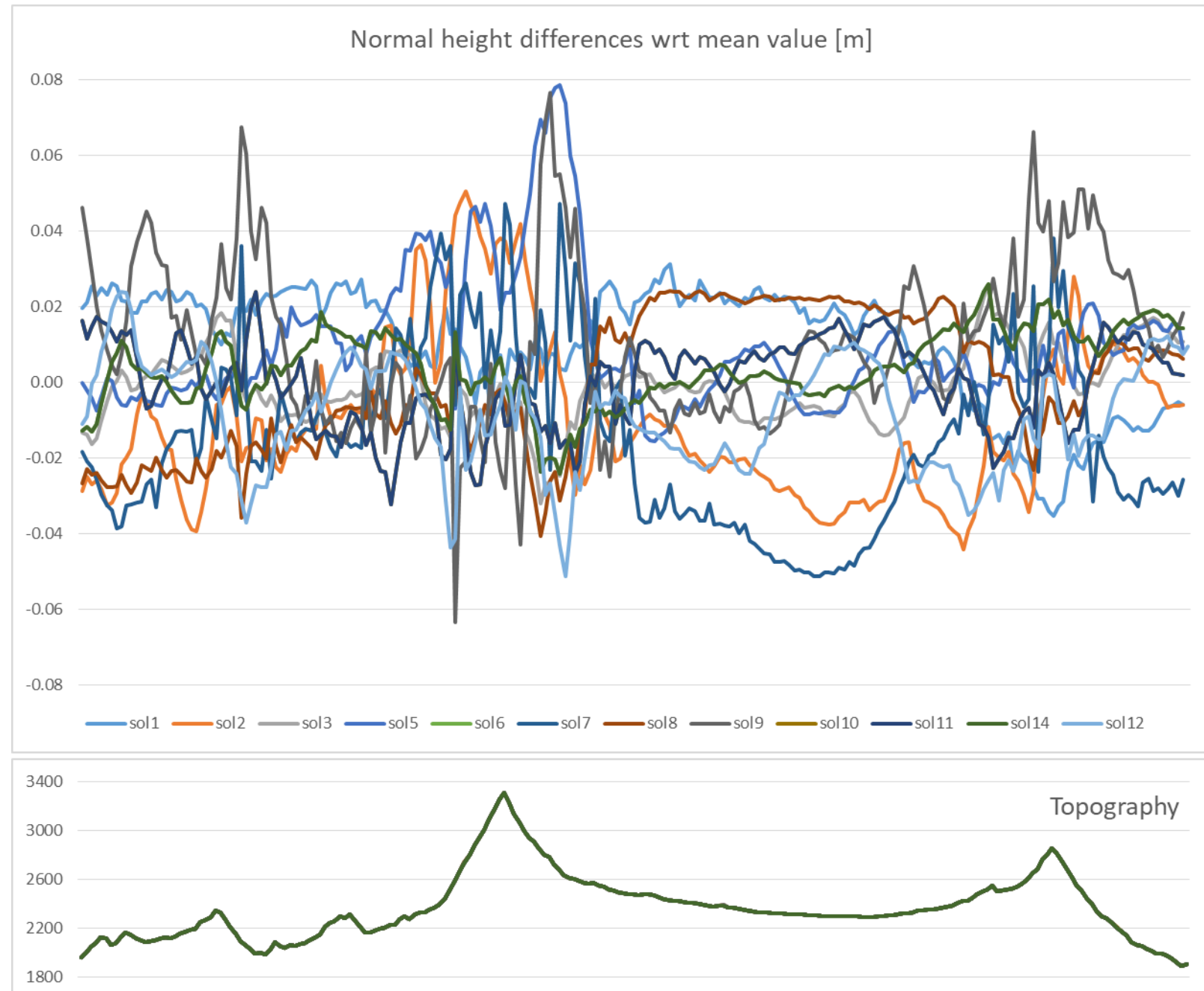
Range: 9.3 (-8.7 ... 0.6)



Colorado experiment: comparison of potential values

Normal height difference [cm]
(individual contribution – mean)

	Mean	±	STD	Range
sol1	1.0	±	1.6	6.6 (-3.5 ... 3.1)
sol2	-1.0	±	2.1	9.5 (-4.4 ... 5.1)
sol3	-0.1	±	1.0	5.8 (-3.2 ... 2.6)
sol5	1.0	±	1.8	9.4 (-1.6 ... 7.9)
sol6	0.4	±	1.0	5.3 (-2.7 ... 2.6)
sol7	-1.4	±	2.3	9.9 (-5.1 ... 4.7)
sol8	0.0	±	1.8	6.5 (-4.1 ... 2.4)
sol9	1.1	±	2.2	14.0 (-6.3 ... 7.7)
sol10	0.0	±	1.2	7.5 (-3.2 ... 4.3)
sol11	0.0	±	1.1	5.6 (-3.2 ... 2.4)
sol12	-0.9	±	1.4	7.5 (-5.1 ... 2.4)
sol14	0.4	±	1.0	5.0 (-2.4 ... 2.6)



Learnings from the Colorado experiment

- 1) **Validation of gravity field (geoid) modelling** additional to GNSS/levelling
- 2) Twelve(!) solutions agree within **1 cm to 2 cm** in terms of standard deviation with respect to the mean value
- 3) We **are waiting for the levelling results** along the test profile to make comparisons with independent data
- 4) Discrepancies between the different solutions are **highly correlated with the topography**
 - Handling of terrain gravity effects (model and strategy)
- 5) Difficulties reported by the colleagues contributing to the experiment
 - Processing of the **airborne gravity data**
 - Handling of the **zero-degree term**
- 6) A major confusion is the reference ellipsoid: which should be used **GRS80 or WGS84?**
 - **Are we needing a new reference ellipsoid?**

Learnings from the Colorado experiment: how to determine potential values as IHRF/IHRF coordinates

- 1) When Molodensky is followed, the determination of $W(P)$ is straightforward: $W(P)=U(P)+T(P)$
- 2) When a quasi-geoid model is available

$$W(P) = U(P) + \gamma \cdot \zeta(P) + \Delta W_0$$

- 3) When a geoid model is available

- Convert the geoid to quasi-geoid (consistently with the hypotheses applied for the geoid computation) and use

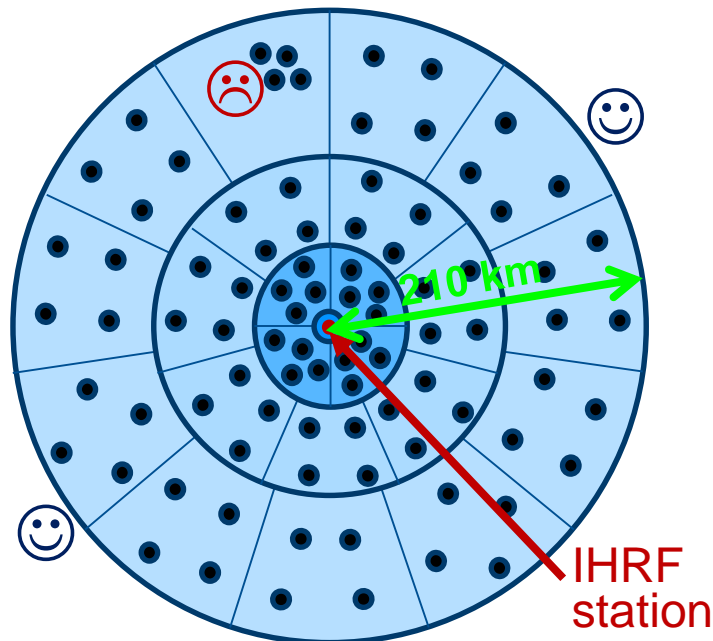
$$W(P) = U(P) + \gamma \cdot \zeta(P) + \Delta W_0$$

- 4) The zero-degree term is the key parameter to refer to the IHRF/IHRF

$$\zeta_0 = \frac{(GM_{GGM} - GM_{GRS80})}{r_P \cdot \gamma_Q} - \frac{\Delta W_0}{\gamma_Q} \quad N_0 = \frac{(GM_{GGM} - GM_{GRS80})}{r_{P_0} \cdot \gamma_{Q_0}} - \frac{\Delta W_0}{\gamma_{Q_0}} \quad \Delta W_0 = W_0 - U_0$$

Learnings of the Colorado experiment: how to determine potential values as IHRF/IHRF coordinates

- 5) The GGM should be based at least on the combination of SLR, GRACE and GOCE data ($n \geq 200$)
- 6) To get an accuracy of about 1 cm in the (quasi-)geoid, observed gravity values are required with a mean spatial resolution of about 4 km
- 7) The availability of these data is a main criterion to select reference stations for the IHRF



Template according to the gravity effect on the geoid ($\Delta g = 1 \cdot 10^{-6} \text{ ms}^{-2} \rightarrow 1 \text{ mm}$)

Distance	Compartments	# of points flat/mountain
10 km	1	4/8
50 km	4	20/30
110 km	7	30/45
210 km	11	50/75
Sum	23	104/158

Criteria for the IHRF reference network configuration

1) Hierarchy:

- A **global network** → worldwide distribution, including
- A **core network** → to ensure sustainability and long term stability
- **Regional and national densifications** → local accessibility

2) Collocated with:

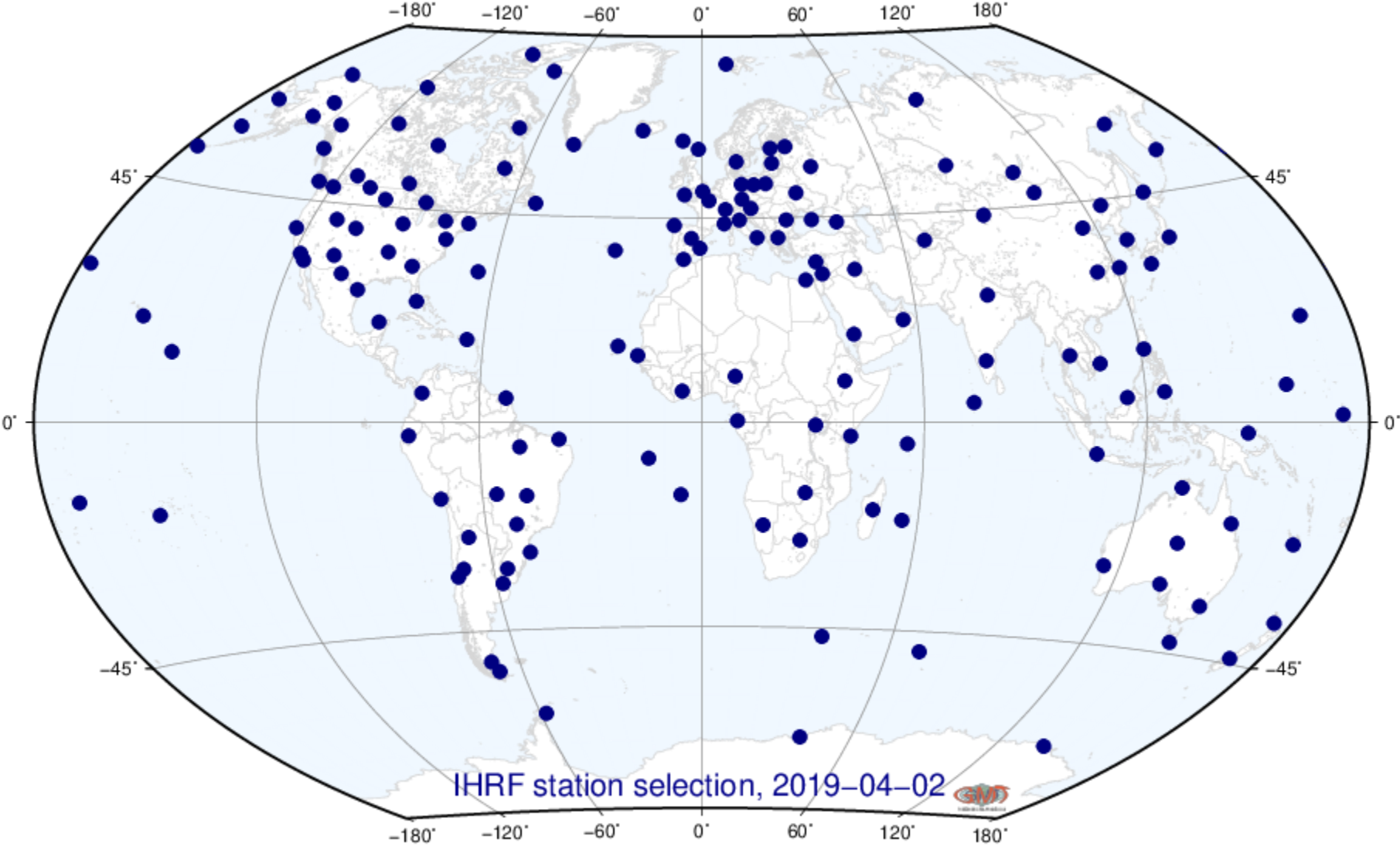
- fundamental **geodetic observatories** → connection between \mathbf{X} , W , g and time realisation (reference clocks) → to support the GGRF;
- **continuously operating reference stations** → to detect deformations of the reference frame (preference for ITRF and regional reference stations, like SIRGAS, EPN, APREF, etc.);
- **reference tide gauges and national vertical networks** → to facilitate the vertical datum unification;
- reference stations of the new **International Gravity Reference Frame - IGRF** (see IAG Resolution 2, Prague 2015).

3) Main requirement: **availability of terrestrial gravity data around the IHRS reference stations for high-resolution gravity field modelling (i.e., precise estimation of W).**

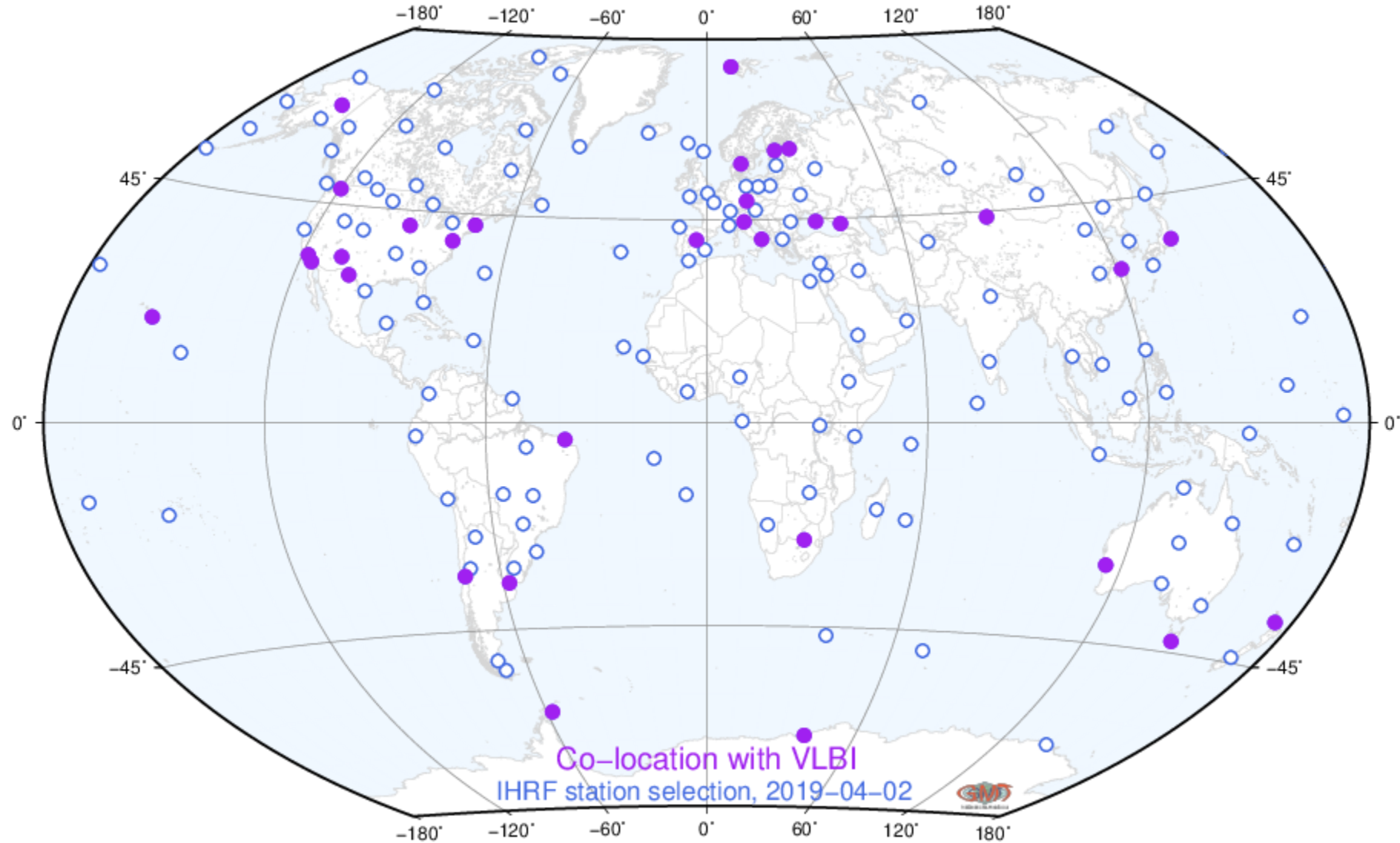
Station selection

- 1) With the support of the [GGOS Bureau for Networks and Observations](#), a preliminary selection based on [VLBI](#), [SLR](#) and [DORIS](#) reference sites co-located with [GNSS](#) was prepared (Oct 2016).
- 2) Based on these preliminary selection, national/regional experts were asked to
 - evaluate whether these sites are suitable to be included in the IHRF: Are gravity data around these sites available? If not, is it possible to survey gravity around them?
 - propose additional geodetic sites to improve the density and distribution of the IHRF stations in their regions/countries
- 3) With support of the IAG JWG 2.1.1: [Establishment of a global absolute gravity reference system](#) (chair: H. Wziontek), further stations co-located with absolute gravity stations were identified.
- 4) A first proposal for the IHRF reference network was ready in Apr 2017.
- 5) Since that time some new stations have been added, others have been decommissioned.
- 6) It is expected that this network is extended by means of regional/national densifications.

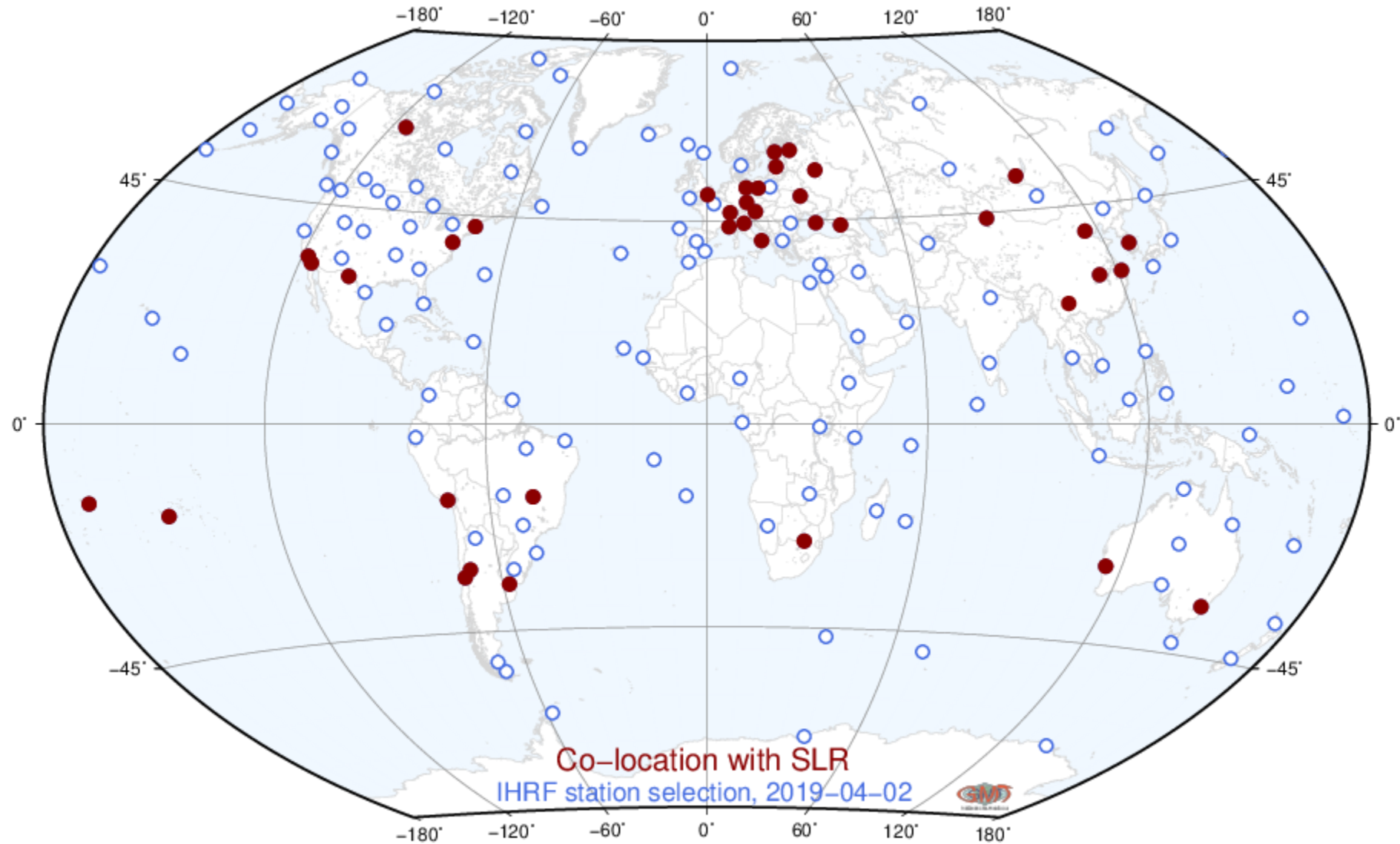
First proposal for the IHRF reference network (~170 stations)



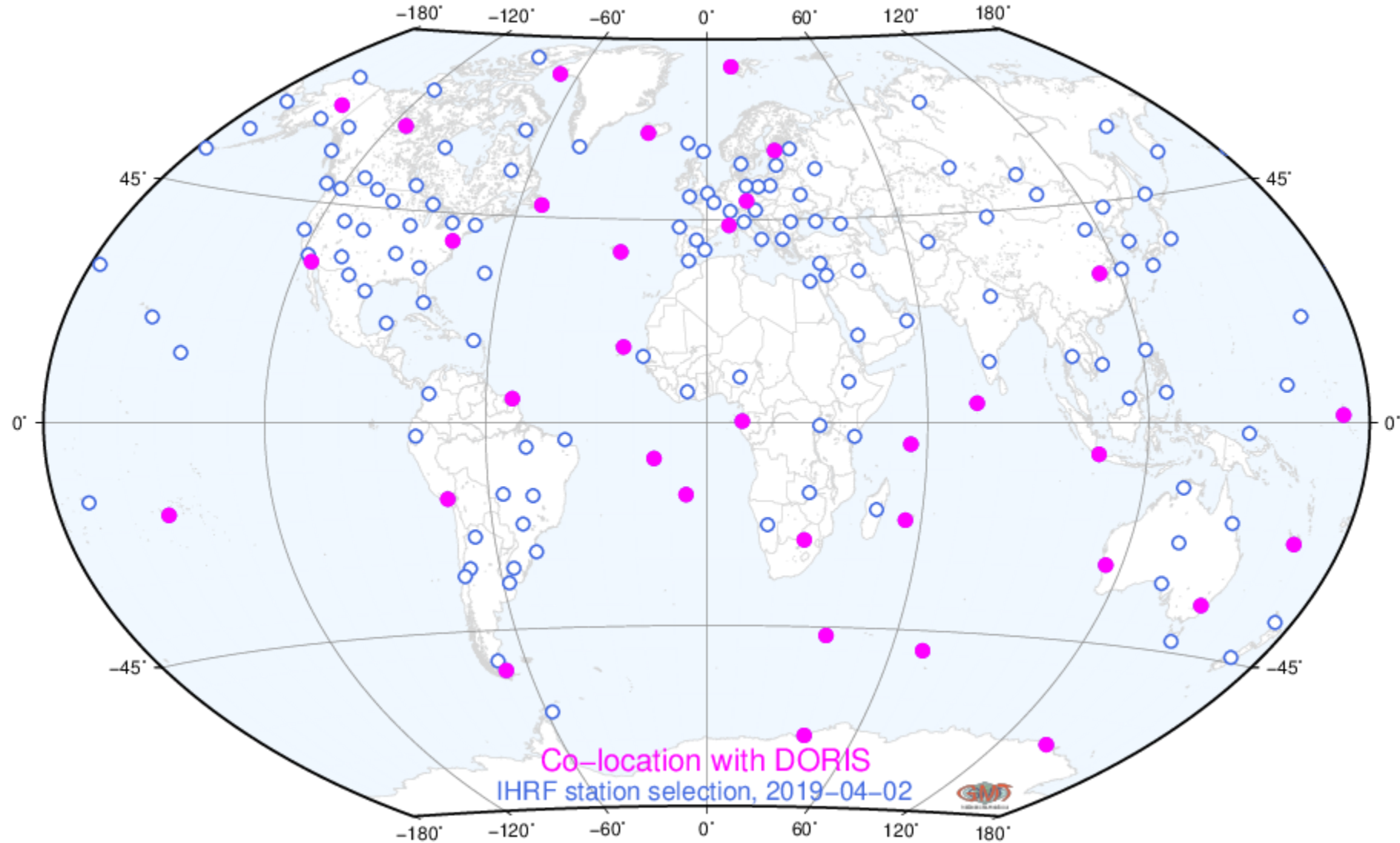
Co-location with VLBI (30 sites)



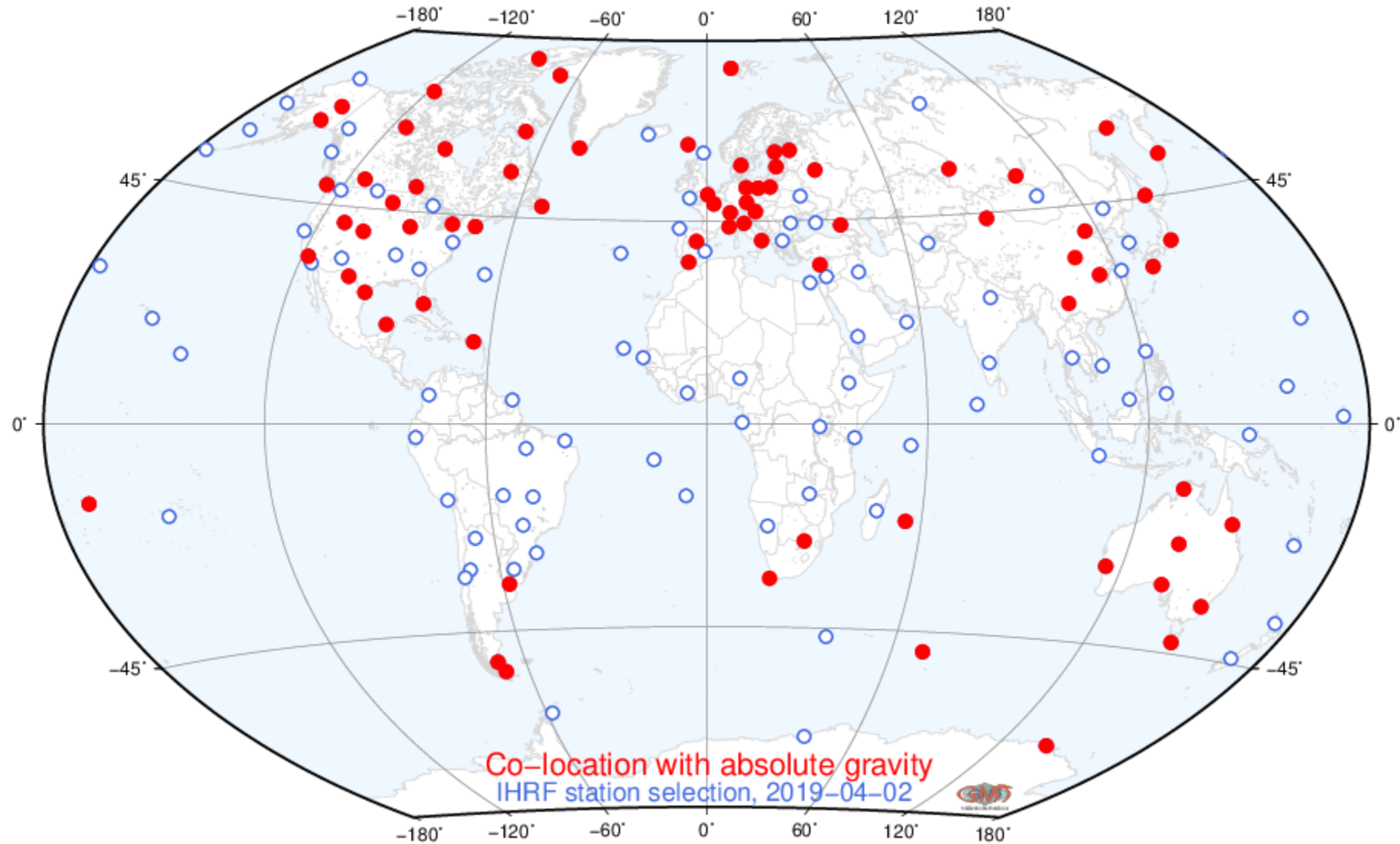
Co-location with SLR (40 sites)



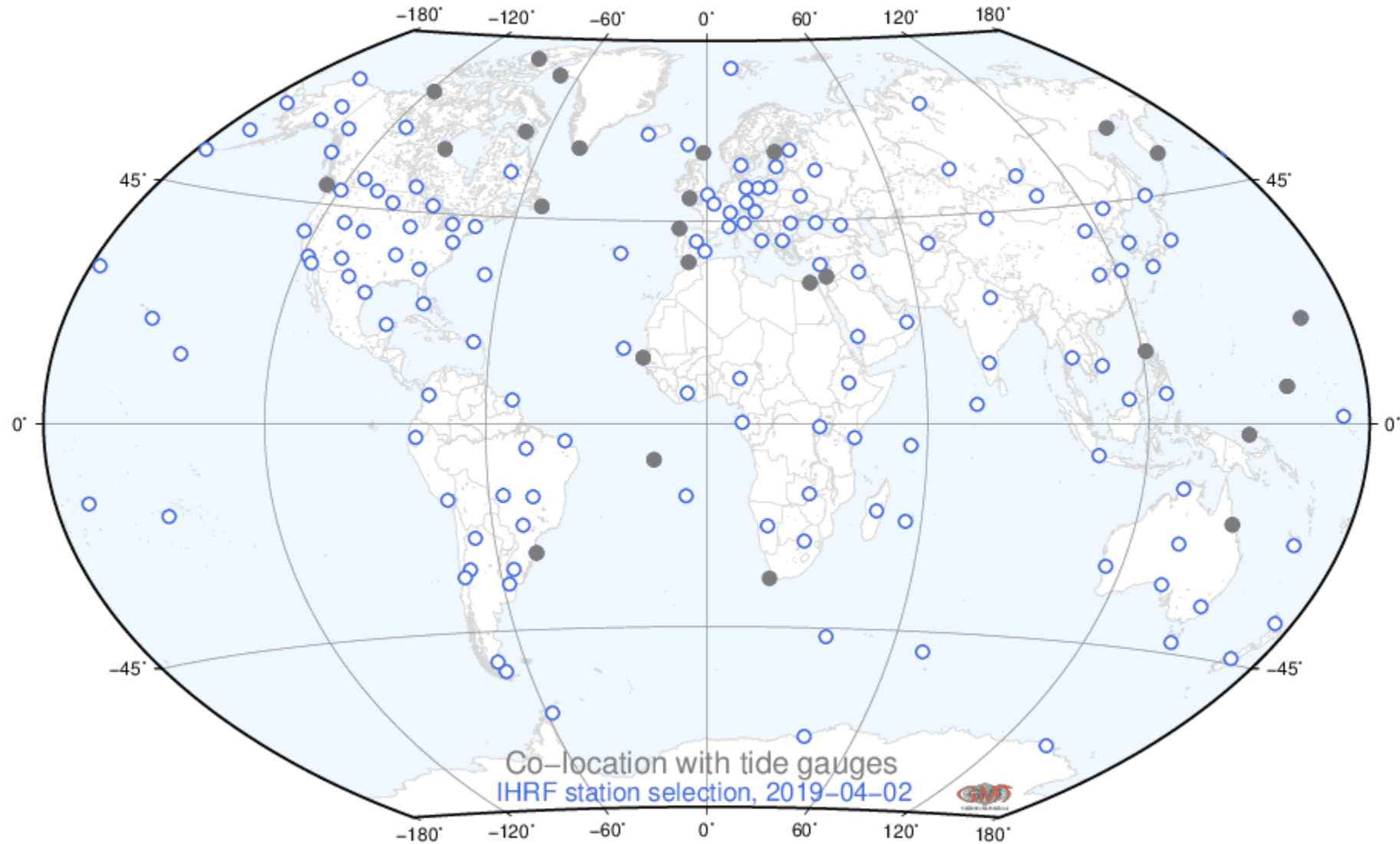
Co-location with DORIS (35 sites)



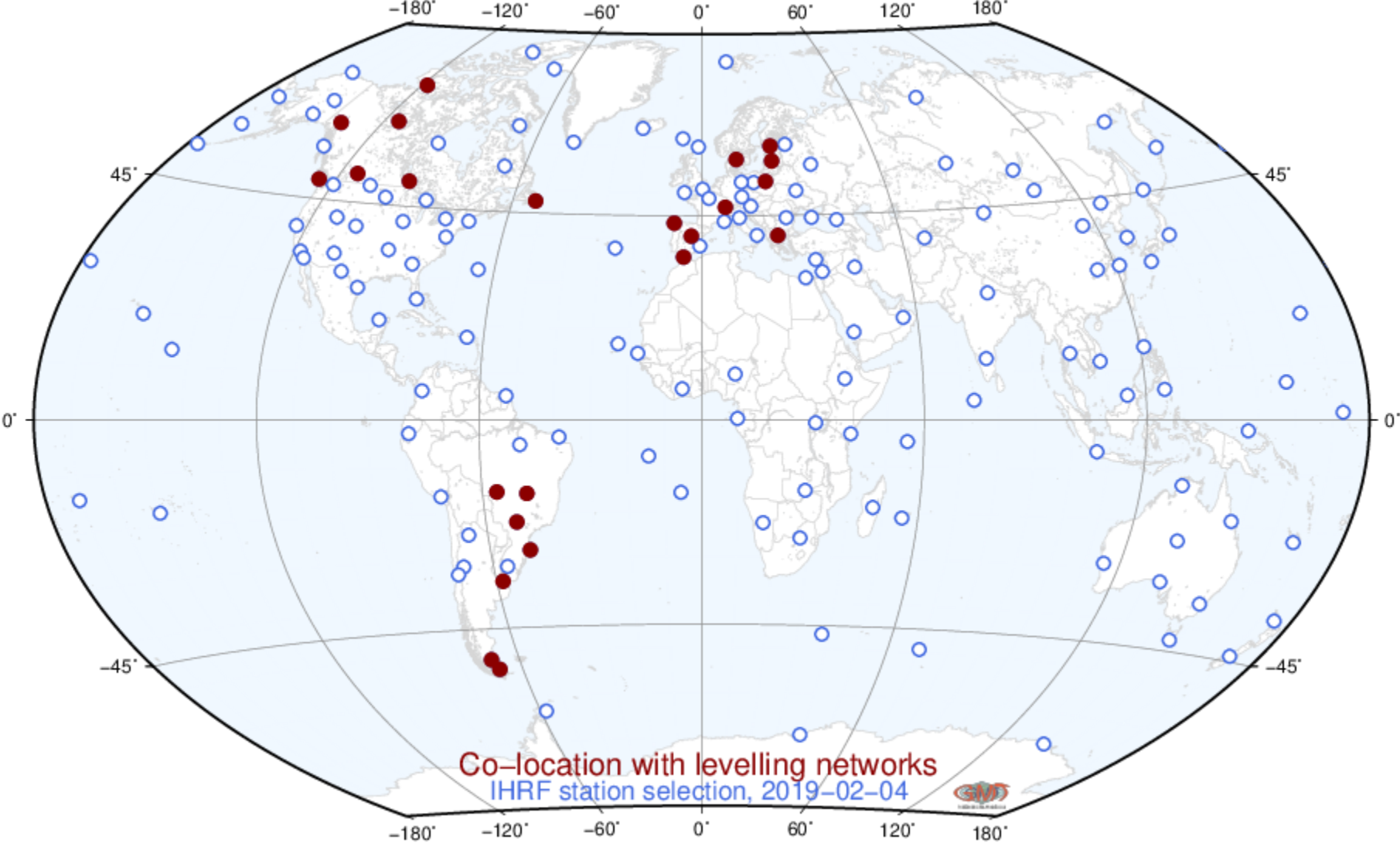
Co-location with absolute gravity (77 sites)



Co-location with tide gauges (26 sites)

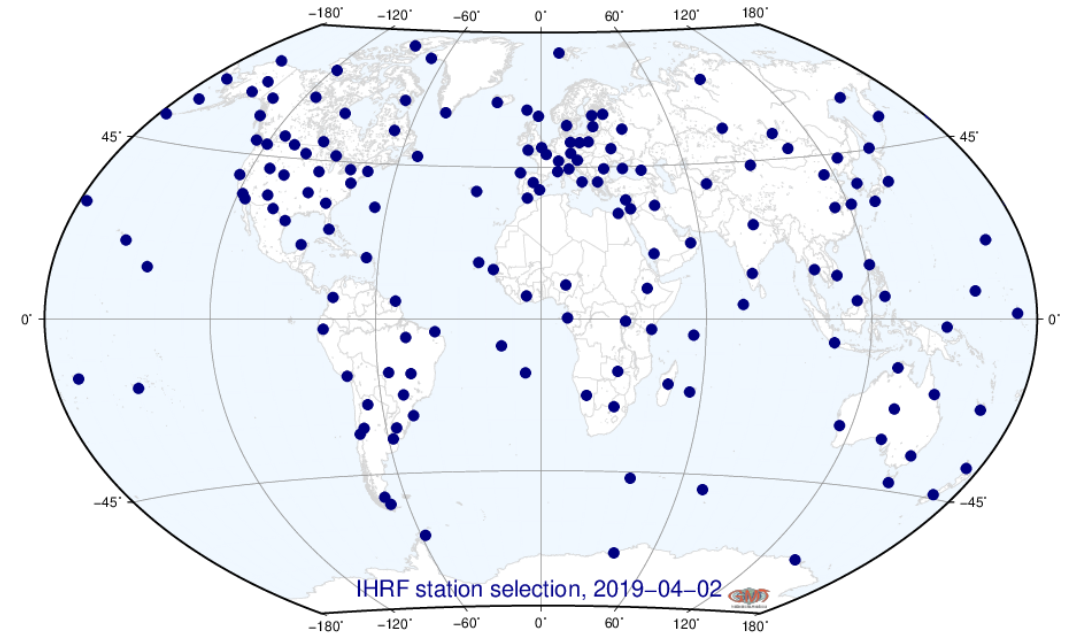


Co-location with levelling networks (23 sites)



First attempts to determine IHRS potential values at the IHRF reference stations

- 1) Based on disturbing potential values and provided by colleagues involved in the (quasi-geoid) determination (Europe, Canada, Brazil, Africa)
- 2) Based on national (quasi-)geoid models (Australia, New Zealand, China, Japan, Argentina, USA)
- 3) Based on the geoid model data bank of the International Service for the Geoid (ISG)
- 4) Based on GGM-HD + terrain gravity effects (also for comparison)



Main problems at present

- 1) Standards and methods used in the (quasi-)geoid determination are not (always) well-documented
- 2) Many (quasi-)geoid models are “fitted” to GNSS/levelling (i.e., unknown bias in recovered potential values)
- 3) An “accuracy assessment” is very difficult.

Outlook

- 1) To continue learning from the Colorado experiment
 - A special issue of the Journal of Geodesy is planned. All contributing solutions will be described in detail. This will allow to improve the document with the standards for the determination of potential values.
- 2) To compute a first static solution for the IHRF to evaluate the achievable accuracy under the present conditions (data availability, computation methods, etc.) and to identify key actions to improve the determination of the IHRF/IHRF coordinates.
- 3) To investigate the determination of potential changes with time \dot{W} .
- 4) To extend the realisation of the IHRF to marine areas.
- 5) To explore the possibilities to establish an 'IHRF element' within the IGFS to ensure the maintenance and availability of the IHRF:
 - Regular updates of the IHRF to take account for:
 - new stations;
 - coordinate changes with time $\dot{\mathbf{X}}$, \dot{W} ;
 - improvements in the estimation of \mathbf{X} and W (more observations, better standards, better models, better computation algorithms, etc.)

- 1) Splinter meeting for the IHRS/IHRF and the Colorado experiment
 - Today, July 12, at 6:00 pm in this room (510C)
- 2) GGOS session dedicated to the Focus Area Unified Height System **Session G06j**
 - **Tuesday, July 16, 4:30 – 6:00 pm, room 510BD**
 - Global gravity field modelling as a fundamental component for the precise height determination and the monitoring of the Earth System (R. Pail)
 - On the Need of Terrestrial Gravity Data and High-resolution Gravity Field Modelling for Realization of the International Height Reference System (J. Ågren)
 - Roadmap to a Mutually Consistent Set of On- and Offshore Vertical Reference Frames - the Dutch Approach (C. Slobbe)
 - The Treatment of the Permanent Tide in Geodetic Quantities: Past, Present, and the Future (J. Mäkinen)
 - 40 Years of the GRS80: Do We Need a New Ellipsoid? (I. Oshchepkov)
 - Geodesy and Earth Observation Based on Quantum Optics and Relativity (J. Müller)