

# VCSEL-Based Atmospheric Trace Gas Sensor Using First Harmonic Detection

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**Abstract**—This paper presents a measurement system based on the first harmonic in tunable diode laser absorption spectroscopy using a vertical-cavity surface-emitting laser to measure the atmospheric CO<sub>2</sub> and H<sub>2</sub>O concentrations. The developed system separates the residual amplitude modulation signal from the harmonics and then eliminates it. A digital signal processing is developed to autonomously infer the wavelength and light intensities of the laser. The gas concentrations are determined without extra calibration. The long-term measurements are taken to validate the precision and accuracy of the system. Based on the Allan variance analysis, the broad wavelength scanning enhances the measurement precision, and the first-harmonic detection can achieve about two times as high precision as the traditional second-harmonic detection. The field measurements implemented in early spring of 2018 in Munich were compared with the commercial nondispersive infrared (NDIR) sensor. The outcomes have revealed that our system has high accuracy for the gas concentration measurements and high consistency with the NDIR sensor. The diurnal variations of CO<sub>2</sub> concentration have demonstrated that CO<sub>2</sub> concentration in urban areas is affected by the biosphere and meteorological conditions and the daily anthropogenic activities. Furthermore, the air trajectory analysis based on the HYSPLIT model has found that the CO<sub>2</sub> emission sources primarily come from the southeast of Munich. The developed system described in this paper has a great potential for *in situ* trace gas concentration measurements, the analysis on the polluted gas distributions, and the verification of the pollutant transport model in urban areas.

**Index Terms**—Trace gas concentration, tunable diode laser absorption spectroscopy (TDLAS), wavelength modulation spectroscopy (WMS), first harmonic, vertical-cavity surface-emitting laser (VCSEL).

## I. INTRODUCTION

GREENHOUSE gases (GHG) have a significant negative impact on the climate change. Research has indicated that carbon dioxide (CO<sub>2</sub>), one of the dominant GHG, has

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increased by about 2 ppm (parts per million) per year in recent years. The cities and their surroundings sustain around 54% of the global population and contribute nearly 70% of the total anthropogenic CO<sub>2</sub> emissions [1]. Therefore, continuously measuring the CO<sub>2</sub> concentration is of great significance for controlling the carbon emissions and studying the diffusion of the pollutant in urban areas [2]–[4].

Tunable diode laser absorption spectroscopy (TDLAS) is a typical method for the *in-situ* trace gas measurements since the laser scans across the absorption line at an extremely small bandwidth, around 30 MHz or smaller, which is about one-tenth of the absorption linewidth [5]–[7]. Unlike the direct TDLAS is employed when absorbance is above 1%, the wavelength modulation spectroscopy (WMS) has wide applications in the trace gas measurements (absorbance less than 1%) and the harsh environments [8], [9]. The theory and mathematical definitions of WMS are outlined in Appendix A. However, due to the arbitrary variation in the phase shift in wavelength, the concentration-dependent harmonics are assigned to X and Y axes in the lock-in amplifier (LIA) at random. Hence, to obtain the complete harmonics, the most common methods are either manually setting the phase of reference signal or using the magnitude of two axes. The former method is inconvenient, while the latter is widely employed in applications [10]. The phase shift in wavelength is discussed in Appendix A.

The harmonics produced by the LIA consist of the absorption line shape and gas parameters information [11], [12]. The concentration-independent residual amplitude modulation (RAM) deforms the harmonics especially the first harmonic. In the well-known “calibration-free  $nf/1f$ ” method, the RAM in the first harmonic is used to normalize the other harmonics [13]–[15]. Nevertheless, the RAM is acquired from the absorption-free condition, it should be characterized carefully prior to the measurement or from a separate laser beam which makes the measurement inconvenient and complex [10]. Additionally, W. Johnstone et al. used the RAM to recover the absorption line shape based on the phasor decomposition method. However, this method is valid under small modulation index ( $m < 0.5$ ) when only the first harmonic is utilized, which leads to low harmonic signal-to-noise ratio (SNR); nonetheless, it can be used for any  $m$  values if the tuning coefficient is given and higher harmonics are employed [16]–[19]. An external optical fiber and the balanced detection were applied to null RAM in the intensity modulated experiment, which increased the complexity in operation and signal

83 processing [20]–[22]. Hangauer *et al.* [11] utilized multi-  
 84 harmonic to reconstruct the transmission and Peng *et al.* [23]  
 85 employed odd-harmonic to recover the absorbance shape,  
 86 the  $m$  was extended to higher values ( $m > 2.0$ ) in their  
 87 approaches.

88 Compared with the conventional distributed-  
 89 feedback (DFB) laser, the vertical-cavity surface-emitting  
 90 laser (VCSEL) has many unique features, such as low power  
 91 consumption, fast and wide wavelength tuning range to cover  
 92 several absorption lines. Thus, the wide tuning VCSEL can  
 93 be used to simultaneously measure different gases [24]–[27].  
 94 The first harmonic has the highest SNR among all harmonics,  
 95 thus, theoretically it should have a highest precision in gas  
 96 sensing. However, due to the strong RAM, the first harmonic  
 97 is distinctly deformed as a non-linear offset with a gradient  
 98 particularly in the wide tuning situations (see black line in  
 99 Fig. 4(b)). Therefore, the magnitude of X and Y components  
 100 in the first harmonic cannot be employed directly to infer the  
 101 gas concentration. It is crucial to build up a simple system  
 102 and eliminate the RAM in the continuous gas measurement  
 103 when using the first harmonic detection.

104 In J. Chen and A. Hangauer’s research, the broad scanning  
 105 range was employed for the wavelength calibration while  
 106 the narrow scanning was for gas concentration measurements  
 107 using the linear least square curve fitting (LLSCF) algorithm  
 108 [28], [29]. They concluded that the second harmonic detection  
 109 had higher precision than the first harmonic detection [11].  
 110 On the contrary, Lan *et al.* [30] focused on using the wide  
 111 tuning VCSEL multi-harmonic for gas concentration measure-  
 112 ment and found that the first harmonic could achieve better  
 113 performance than the second harmonic in gas detection. It has  
 114 shown that multi-harmonic detection including first harmonic  
 115 can enhance the precision of the system. However, the previous  
 116 study did not focus on the removal of RAM in first harmonic  
 117 and the development of a compact system using first harmonic  
 118 for urban GHG measurements.

119 This article focuses on utilizing the first harmonic for  
 120 atmospheric gas sensing based on the VCSEL’s wide tuning  
 121 range. A measurement system was developed to autonomously  
 122 eliminate the RAM signal in the harmonics, calibrate the wave-  
 123 length and laser light intensities, and measure the *in-situ* CO<sub>2</sub>  
 124 and H<sub>2</sub>O concentrations. Then, Allan-Werle Variance Analysis  
 125 was deployed to analyze the precision of our measurement  
 126 system. The field measurement compared with the commercial  
 127 nondispersive infrared (NDIR) sensor was carried out in early  
 128 spring of 2018 in Munich. The analysis on the CO<sub>2</sub> diurnal  
 129 variation demonstrated that the CO<sub>2</sub> concentration in urban  
 130 areas is affected not only by biosphere and meteorological  
 131 conditions but also by the daily anthropogenic activities. The  
 132 backward trajectory analysis based on HYSPLIT model was  
 133 implemented to identify CO<sub>2</sub> sources in urban areas.

## 134 II. EXPERIMENTAL FOUNDATION

### 135 A. First Harmonic Detection

136 The basic principle of WMS has been introduced in several  
 137 articles [11], [12], [31]. According to Eqs. 6 and 8 in Appen-  
 138 dix A, for optically thin samples (absorbance  $\ll 10\%$ ),  $A_0 \approx 1$   
 139 and  $A_1, A_2, A_3, A_4, \dots \ll A_0$ , which are assumed as 0. Thus,

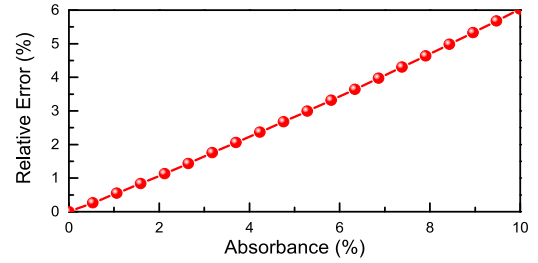


Fig. 1. The error analysis of concentration measurement when the  $S_{0f}$  is served as  $S_{0f} \approx \bar{I}_0$  to normalize the harmonics.

the zeroth harmonic picked out via LIA is:  $S_{0f} = \frac{I_{0\theta}^X}{I_0} \approx \bar{I}_0$ .  
 The  $S_{0f}$  can be served as the central light intensity ( $\bar{I}_0$ ) when  
 the absorbance is weak [32].

When normalized with respect to  $S_{0f}$ , the X and Y com-  
 ponents of first harmonic,  $X_{1f}$  and  $Y_{1f}$ , are simplified as:

$$\begin{cases} X_{1f} = A_1 + \frac{I_1}{I_0} \cos \psi \\ Y_{1f} = \frac{I_1}{I_0} \sin \psi. \end{cases} \quad (1)$$

It can be learned from Eq. 1 that  $X_{1f}$  consists of two parts: the  
 harmonic signal ( $A_1$ ), which includes gas parameters, and the  
 cosine  $\psi$  of RAM; while  $Y_{1f}$  is concentration-independent and  
 only contains the sine  $\psi$  of RAM. The  $\psi$  can be determined  
 when  $Y_{1f}$ ,  $\bar{I}_0$  and  $I_1$  are given. Then, the measured  $\psi$  is  
 employed to eliminate RAM when it is substituted into the  
 $X_{1f}$  expression:

$$\bar{X}_{1f} = X_{1f} - \frac{Y_{1f}}{\tan \psi} = A_1 = PS(T)LcH_1, \quad (2)$$

where  $H_1$  are the first order Fourier components of the spectral  
 line shape. Thus, the  $\bar{X}_{1f}$  is pure concentration-dependent and  
 can be used to infer gas concentration when  $P$  and  $T$  are given:

$$c = \frac{\bar{X}_{1f}}{PS(T)LH_1}. \quad (3)$$

From Eq. 3, the gas concentration can be obtained without the  
 extra calibration against the standard reference gas. Thus, this  
 method gets rid of the calibration proces.

Figure 1 is the error analysis of the concentration mea-  
 surement when  $S_{0f}$  is used as  $\bar{I}_0$  to normalize the harmonic  
 signals. As can be seen from Fig. 1, the relative errors  
 increase as the increment of the absorbance. To ensure the  
 measurement error within 1%, the absorbance should not  
 exceed 2%. Therefore, for the trace gas measurement when  
 absorbance  $\ll 10\%$ , the approximation of  $S_{0f} \approx \bar{I}_0$  will not  
 introduce a large measurement error.

### 139 B. Experimental Setup

The diagram of the experimental setup is shown in Fig. 2. A  
 VCSEL (VL-2004-1-SQ-A5) [33] is used as the light source  
 whose wavelength is controlled by a laser driver (Arroyo  
 Instruments 6301). The absorption signal is reflected by a  
 concave mirror with 75 mm of focus length and collected  
 into an InGaAs amplified photodetector (PD, PDA10DT-EC).  
 Subsequently, the detected signal is recorded and digitized

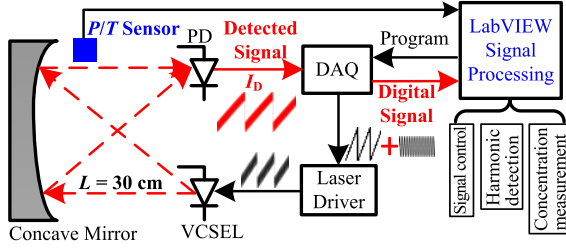


Fig. 2. Experimental setup for trace gas concentration measurement.

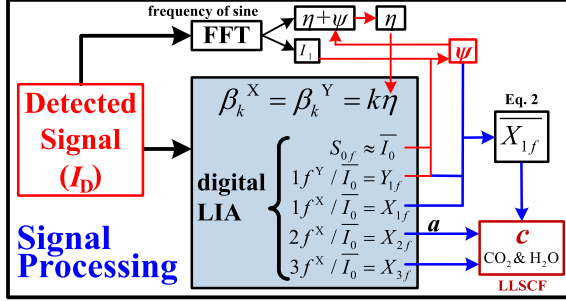


Fig. 3. Signal processing of harmonic detection and gas concentration measurement. The red arrows are the process to determine  $\psi$  in an iterative procedure. The shade part is the digital lock-in amplifier (LIA).

177 via a high-speed memory data acquisition card (DAQ, NI  
 178 USB-6361, resolution: 16 bits, and sampling rate: 2MS/s).  
 179 The digitized data is sent into the signal processing to further  
 180 calculate gas concentration. In this process, the DAQ  
 181 is deployed not only to record the detected signal but also  
 182 as a signal generator to provide the ramp and sinusoidal  
 183 signals such that the laser wavelength is modulated. A sensor  
 184 using the Raspberry Pi system is set nearby to synchronously  
 185 measure  $P$  and  $T$ . The signal processing is explained in the  
 186 following Sect. II-C.

### 187 C. Autonomous Measurement System

188 A digital signal processing (LabVIEW) is developed to calcu-  
 189 late the intermediate parameters as mentioned in Sect. II-A  
 190 and Appendix A, and to obtain gas concentrations. The first  
 191 part of the processing is the signal controlling and acquisition.  
 192 The LabVIEW programs DAQ to generate the low-frequency  
 193 ramp (10 Hz, 1.2 V) and high-frequency sinusoidal (6 kHz,  
 194 60 mV) signals to modulate the VCSEL in a wide range, and  
 195 then to record the absorption signal into LabVIEW, which is  
 196 shown as black line in Fig. 4(a). In this case, the modulation  
 197 indices ( $m$ ) of each line are around 3.0 which ensures the  
 198 high SNR of the first, second and third harmonics (Fig. 5,  
 199 Appendix B).

200 The second part is the harmonic detection. As indicated in  
 201 Fig. 3, a digital LIA is developed to produce the zeroth to third  
 202 harmonics. Note that the zeroth harmonic can be produced in  
 203 our developed LIA by setting the frequency of the reference  
 204 signal to 0. The red dotted line in Fig. 4(a) is the central  
 205 light intensity ( $\bar{I}_0$ ). In WMS, the zeroth harmonic ( $S_{0f}$ ) can be  
 206 treated as:  $S_{0f} \approx \bar{I}_0$  when the absorbance is weak (absorbance  
 207  $\ll 10\%$ ). The  $S_{0f}$  is averaged from the 10 sequential scans  
 208 (10 Hz) to improve SNR and used to normalize the other  
 209 harmonics. Figure 4(b) exhibits the curves of the normalized  
 210  $X_{1f}$  and  $Y_{1f}$ . The peak positions of each absorption lines (the

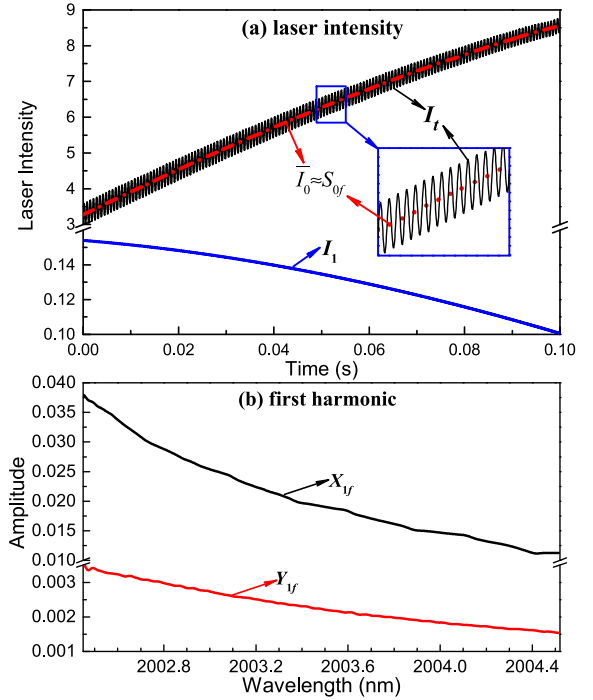


Fig. 4. (a) The detected signal via the photodetector ( $I_D$ ) and its central light intensity ( $\bar{I}_0$ , red dotted line). The  $S_{0f}$  can be served as  $S_{0f} \approx \bar{I}_0$  when the absorbance is weak. The modulation intensity ( $I_1$ ) is obtained from an FFT subroutine. (b) The normalized X and Y components of first harmonic in a scanning cycle, where  $X_{1f}$  includes the RAM.

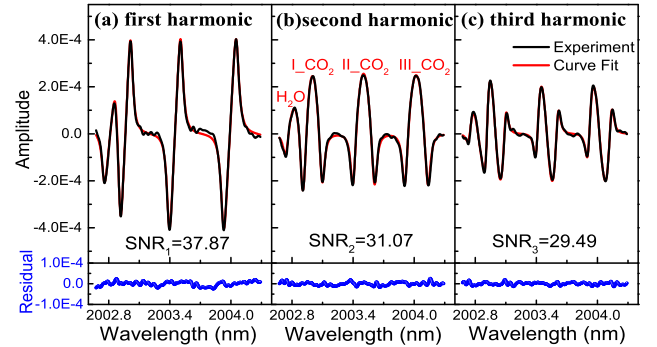


Fig. 5. Wide-scanned concentration-dependent harmonic signals obtained from Fig. 4(a); (a) first harmonic without RAM, (b) second harmonic, and (c) third harmonic. The red lines are the calculation curves based on the LLSCF. The bottoms are the residuals of curve fit results. The concentrations of  $\text{CO}_2$  and  $\text{H}_2\text{O}$  are 411.8 ppm and 5.56%, respectively.

211 absorption line centers are 2002.829 nm ( $\text{H}_2\text{O}$ ), 2002.998 nm,  
 212 2003.503 nm, and 2004.019 nm, respectively) in the normal-  
 213 ized  $X_{2f}$  (Fig. 5(b)) are picked as the absorption line centers,  
 214 thus, the wavelength versus the ramp signal is calibrated  
 215 and the modulation depths ( $a$ ) are determined (Appendix C).  
 216 A Fast Fourier Transform (FFT) subroutine is established to  
 217 measure the modulation intensity ( $I_1$ , as blue line in Fig. 4(a))  
 218 and light intensity phase ( $\eta + \psi$ ) when the extracted frequency  
 219 is set the same as sine signal (6 kHz). An iterative procedure  
 220 is created to determine the phase shift ( $\psi$ ) as follows: a very  
 221 first  $\psi_1 = 0^\circ$  is used to subtract  $\psi$  in the phase ( $\eta + \psi$ ) and  
 222 get  $\eta_1$ . Then, the phase of the reference signal is set as  $\beta_1^Y = \eta_1$   
 223 to receive  $Y_{1f}$ . Afterwards, according to  $\bar{I}_0$ ,  $I_1$  and  $Y_{1f}$ , a new  
 224  $\psi_2$  is obtained. The process is reiterated until  $\psi$  is constant.  
 225 In our system, when the sine frequency is 6 kHz,  $\psi = 6.7^\circ$ .

226 Thereby, when given  $\bar{I}_0$ ,  $I_1$ ,  $\psi$ , and  $\eta$ , the  $X_{kf}$  and  $Y_{kf}$  are  
 227 obtained by setting the reference phase signal to:  $\beta_k^X = \beta_k^Y =$   
 228  $k\eta$  (see Appendix A). The concentration-dependent  $\bar{X}_{1f}$  is  
 229 acquired according to Eq. 2.

230 In the third part, the harmonics with different scanning  
 231 ranges are extracted to infer gas concentrations based on the  
 232 LLSCF algorithm [34], [35]. The spectral parameters of the  
 233 absorption lines are acquired from the HITRAN databases and  
 234 utilized for calculating  $H_k$  [36]. The curve fitting results of the  
 235 first, second and third harmonics with three CO<sub>2</sub> absorption  
 236 lines and one H<sub>2</sub>O absorption line are displayed in Fig. 5. The  
 237 residuals in the bottom are in an order of  $1 \times 10^{-5}$ , indicating  
 238 the high accuracy of the system.

239 Throughout the process, the wavelength and light intensities,  
 240 and the harmonics are autonomously calibrated in the absence  
 241 of the standard optical components such as etalon, beam splitter,  
 242 and the absorption-free laser path. The entire procedure  
 243 takes about 0.5s which enables the real-time measurement.  
 244 As Eq. 3 demonstrates, the gas concentrations are obtained  
 245 without the standard reference gas. Therefore, this system  
 246 is an autonomous calibration system for *in-situ* trace gas  
 247 measurements. The absorbance of about 2‰ for the GHG  
 248 sensing ensures that the assumption of  $S_{0f} \approx \bar{I}_0$  is valid in  
 249 the system. The  $P$  and  $T$  compensations are carried out in  
 250 the measurements. The air-broadening is dominant while the  
 251 self-broadening uncertainty (<1%) can be ignored in Pressure  
 252 Broadening in the trace gas measurements [15]. Furthermore,  
 253 the  $\bar{I}_0$  is on-the-fly measured in every scanning cycle, the fluctu-  
 254 ations of the light intensity can be instantaneously eliminated  
 255 during the measurement. This system thus can be utilized even  
 256 in vibration situations where the laser path is difficult to fix.

257 Using VCSEL, the wide tuning range which covers several  
 258 gas species in a cycle enables not only the wavelength cali-  
 259 bration but also several gas concentrations to be measured  
 260 simultaneously. From Fig. 5, the first harmonic without RAM  
 261 has the highest magnitude and highest SNR of 37.87, meaning  
 262 that it has the best noise performance among all harmonics.  
 263 However, compared the black line in Fig. 4(b) and the curves  
 264 in Fig. 5(a), which included and excluded the RAM, the RAM  
 265 in the original first harmonic is a distinct non-linear offset  
 266 with gradient that submerges the harmonic signal. The RAM  
 267 is complicated and difficult to determine in the wide tuning  
 268 VCSEL. Consequently, it is important for VCSEL to eliminate  
 269 RAM in the wide tuning range for first harmonic detection.  
 270 Furthermore, the second order modulation intensity ( $I_2$ ) is  
 271 much smaller than  $I_1$  (0.3% of  $I_1$ ) so that the RAM in  
 272 the second harmonic can be treated as a slope and an offset,  
 273 as presented in [29]. The higher order modulation intensities  
 274 can be neglected since they are even smaller.

### 275 III. EXPERIMENTAL RESULT AND ANALYSIS

#### 276 A. Allan-Werle Variance Analysis

277 Allan-Werle Variance is a method to identify and quantify  
 278 the different noise terms that exist in the inertial sensor data,  
 279 and calculate the detection limit of the sensor in the time  
 280 domain [37], [38]. As displayed in Fig. 6, when the Allan  
 281 Deviation ( $\sigma_{\text{Allan}}$ ) is minimum ( $\sigma_{\text{Allan}}^{\text{min}}$ ), the optimum integrat-  
 282 ing time ( $\tau_{\text{opt}}$ ) and the detection limit are determined. Allan

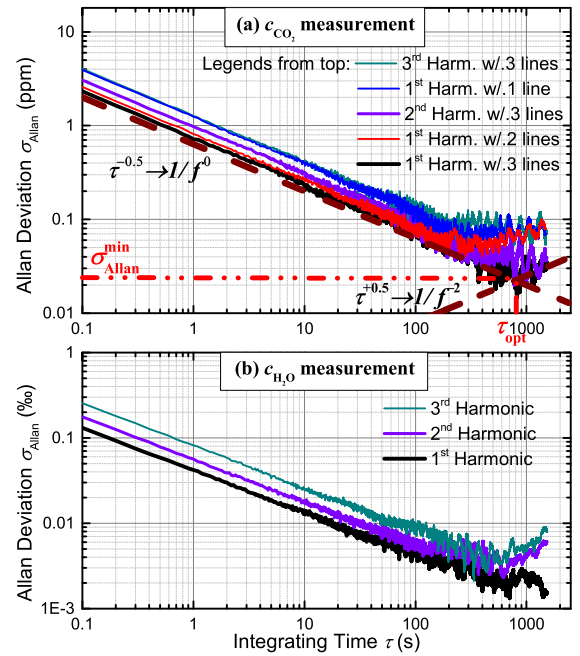


Fig. 6. Allan Deviations of the first, second and third harmonics with different absorption lines for CO<sub>2</sub> and H<sub>2</sub>O concentration measurements. The wine-red lines represent slopes of  $-0.5$  and  $0.5$ , which correspond to the power densities  $S(f) = f^0$  (white noise) and  $S(f) = f^{-2}$  (Brownian noise), respectively.

TABLE I

ALLAN ANALYSIS FOR CO<sub>2</sub> & H<sub>2</sub>O CONCENTRATION MEASUREMENTS

Gas	$S_{nf}$ w/. lines	$\sigma_{\text{Allan}}@1\text{s}$	$\sigma_{\text{Allan}}@1\text{min}$	$\sigma_{\text{Allan}}^{\text{min}}@ \tau_{\text{opt}}(\text{s})$
CO <sub>2</sub>	1 <sup>st</sup> w/. 1	1.24ppm	0.16ppm	0.07ppm@300
	1 <sup>st</sup> w/. 2	0.81ppm	0.11ppm	0.06ppm@300
	1 <sup>st</sup> w/. 3	0.72ppm	0.10ppm	0.027ppm@800
	2 <sup>nd</sup> w/. 3	0.97ppm	0.12ppm	0.05ppm@400
	3 <sup>rd</sup> w/. 3	1.27ppm	0.18ppm	0.09ppm@200
H <sub>2</sub> O	1 <sup>st</sup> w/. 1	0.042‰	0.006‰	0.002‰@600
	2 <sup>nd</sup> w/. 1	0.057‰	0.007‰	0.004‰@400
	3 <sup>rd</sup> w/. 1	0.082‰	0.011‰	0.005‰@200

283 Deviations for CO<sub>2</sub> and H<sub>2</sub>O concentration measurements  
 284 are demonstrated in Fig. 6 and Table I. The measurement is  
 285 performed in a stable climate chamber with the surrounding  
 286 conditions of temperature:  $296 \pm 0.5$  K and pressure:  $0.95 \pm$   
 287  $0.01$  atm, and CO<sub>2</sub> and H<sub>2</sub>O concentrations of  $466.8 \pm 0.2$  ppm  
 288 and  $5.05 \pm 0.01\%$ , respectively. From Fig. 6(a), the plots of  
 289 the first harmonic detection illustrate that the more absorption  
 290 lines are included, the higher precise the measurement is.  
 291 That is, compared with the measurement result of the single  
 292 absorption line (II\_CO<sub>2</sub>, as annotated in Fig. 5(b)), the first  
 293 harmonic detection with double (II and III\_CO<sub>2</sub>) and triple  
 294 absorption lines (I, II and III\_CO<sub>2</sub>) have lower deviations.  
 295 For example, the  $\sigma_{\text{Allan}}$  of the double and the three absorption  
 296 lines are 0.81 ppm and 0.72 ppm with 1s averaged, respectively;  
 297 while the  $\sigma_{\text{Allan}}$  of the single line is 1.24 ppm. It concludes  
 298 that the first harmonic detection with extended scanning range  
 299 can improve the measurement precision.

300 When the RAM effect is eliminated, the first harmonic  
 301 detection has higher precision than that of the second and  
 302 third harmonic detections. That is, the Allan plots of the first  
 303 harmonic have lower white and Brownian noise levels during  
 304 the entire integrating time. Taking the H<sub>2</sub>O measurement as

305 an example, the first harmonic achieves  $6 \times 10^{-3}\%$  of the  
 306 deviation with 1min averaged, while the second and the third  
 307 harmonic detections only obtain  $7 \times 10^{-3}\%$  and  $0.011\%$  with  
 308 the same integrating time, respectively. In terms of the detec-  
 309 tion limits, the first harmonic with three absorption lines  
 310 obtains 0.027 ppm when the  $\tau_{\text{opt}}$  is 800s for CO<sub>2</sub> concentration  
 311 measurement, while the  $\sigma_{\text{Allan}}^{\text{min}}$  of the second harmonic is only  
 312 0.05 ppm with 400s averaged. In H<sub>2</sub>O detection, the  $\sigma_{\text{Allan}}^{\text{min}}$   
 313 of the first harmonic is  $2 \times 10^{-3}\%$  with 600s averaged, while  
 314 the  $\sigma_{\text{Allan}}^{\text{min}}$  of the second harmonic is  $4 \times 10^{-3}\%$  with 400s  
 315 averaged. That is to say, the first harmonic detection has  
 316 about two times better precision than the traditional second  
 317 harmonic detection. As shown in Fig. 4(b), the primitive  
 318 first harmonic curve is deformed in the wide scanning range  
 319 because of the existence of the RAM. The harmonic signal  
 320 is even submerged in the RAM and is hard to use for the  
 321 concentration measurement. However, when the RAM signal is  
 322 removed, the first harmonic detection has the best performance  
 323 among all harmonics. Therefore, the elimination of RAM in  
 324 the first harmonic is necessary and can effectively improve  
 325 precision in gas sensing.

326 In short, the Allan Deviation Analysis demonstrates that  
 327 when the RAM signal has been eliminated, the first harmonic  
 328 detection has the highest precision in the gas concentration  
 329 measurement. It can enhance the precision by nearly double  
 330 when compared with the traditional second harmonic detec-  
 331 tion. That is because the first harmonic signal has the largest  
 332 magnitude and SNR among all harmonics. As shown in Fig. 5,  
 333 the SNR of the first harmonic is 37.87 which is higher than  
 334 the second harmonic (31.07). The higher the order of the  
 335 harmonic is, the lower the amplitudes and SNR are. There-  
 336 fore, the low-order harmonics can achieve better precision  
 337 performance in measurement. Widening the scanning range  
 338 can not only measure various gas species simultaneously, but  
 339 also can obtain higher precision because more information in  
 340 the absorption lines are utilized. The experimental results also  
 341 indicate the high stability of the measurement system.

### 342 B. Accuracy of the Measurement

343 The comparison experiments are implemented to verify the  
 344 accuracy of our developed system, where a commercial NDIR  
 345 sensor (Li-Cor 840A CO<sub>2</sub>/H<sub>2</sub>O gas analyzer) is served as a  
 346 standard instrument as in [30]. However, due to the frequency  
 347 instability of the optical filter which is controlled by the piezo,  
 348 the NDIR sensor must be calibrated periodically according to  
 349 the application and utilization frequency [39]. The inlet gas  
 350 tube of the NDIR sensor is set close to the optical path of the  
 351 TDLAS system. These two sensors are operated separately and  
 352 simultaneously to acquire CO<sub>2</sub> and H<sub>2</sub>O concentrations.

353 Figure 7 illustrates the comparison results of CO<sub>2</sub> and  
 354 H<sub>2</sub>O concentrations dating from March 30 to April 11, 2018.  
 355 The outcomes of TDLAS are retrieved from the first har-  
 356 monic detection with 10 min averaged for which the  $\sigma_{\text{Allan}}$   
 357 are 0.03 ppm for CO<sub>2</sub> concentration and 0.02‰ for H<sub>2</sub>O  
 358 concentration, as illustrated in Fig. 6 and Table I. From  
 359 Fig. 7, we can learn that the measured concentrations from the  
 360 TDLAS system is closely aligned with the values measured  
 361 by the NDIR sensor, which reveals that these two sensors  
 362 have a high consistency with each other. As shown in the

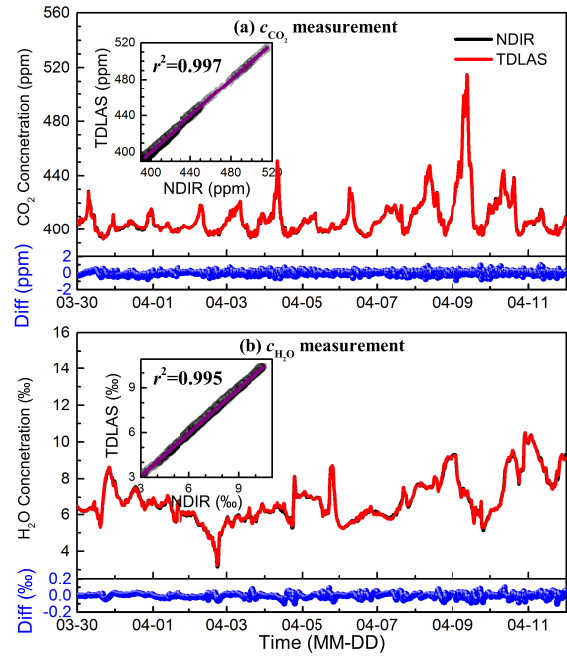


Fig. 7. CO<sub>2</sub> and H<sub>2</sub>O concentrations measured by TDLAS and NDIR sensors, the experimental data is averaged over 10 minutes.

363 bottom of the plots, the differences between these two sensors  
 364 are less than 1 ppm for CO<sub>2</sub> concentration and 0.1‰ for  
 365 H<sub>2</sub>O concentration (much less than 1% relative), indicating  
 366 the high accuracy of the developed system. Moreover, the  
 367 linear regressions between the TDLAS and NDIR sensors are  
 368 also demonstrated in Fig. 7, where the regression ranges are  
 369 390–520 ppm with absorbance of  $1.6 \times 10^{-3} - 2.1 \times 10^{-3}$  for  
 370 CO<sub>2</sub> and 3–11‰ with absorbance of  $5 \times 10^{-4} - 1.8 \times 10^{-3}$  for  
 371 H<sub>2</sub>O, respectively. The correlation coefficients ( $r^2$ ) of above  
 372 0.99 demonstrate the high coherence of the two systems.

373 Overall, the wide scanning first harmonic signal can be  
 374 utilized for measuring CO<sub>2</sub> and H<sub>2</sub>O concentrations when the  
 375 RAM is eliminated. The experimental results have confirmed  
 376 that the first harmonic detection has high accuracy in gas sen-  
 377 sing and has high consistency with the NDIR sensor. Further-  
 378 more, compared with the multi-harmonic detection, the sole  
 379 first harmonic detection achieves a more stable measurement  
 380 because less information is employed in the signal processing.  
 381 The results have indicated that the first harmonic detection is  
 382 more favorable in data processing and has wider applications  
 383 in real-time GHG measurement [30].

### 384 C. Diurnal Variation Analysis

385 To provide a better understanding about the CO<sub>2</sub> concentra-  
 386 tion variation in urban areas, the measurement results depicted  
 387 in Fig. 7 are separated over days and presented in Fig. 8,  
 388 where the foggy days from April 8 through 10 are excluded in  
 389 the discussion. During the measurement period, the forsythia  
 390 was blooming, meaning that most of the plant leaves had just  
 391 started sprouting and that the vegetation photosynthesis and  
 392 respiration from the biosphere were still not very strong. As  
 393 displayed in Fig. 8(a), the diurnal cycle is clearly discernible.  
 394 However, compared with the daily cycles in our previous work  
 395 in [30], the lowest CO<sub>2</sub> concentration in the study period

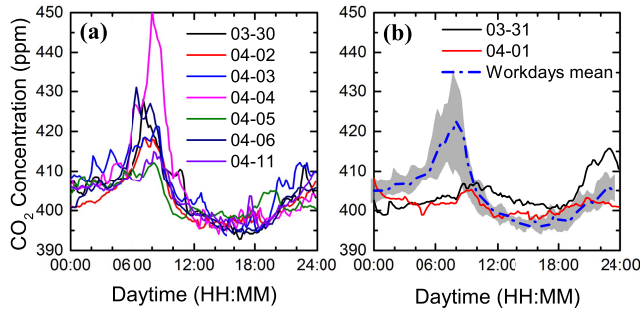


Fig. 8. Daily analysis of the CO<sub>2</sub> concentration measurement in (a) workdays and (b) weekends; the dash-dotted line in (b) is the averaged value of (a), the gray part displays the 68% confidence interval.

396 (395 ppm) is higher than that in September (380 ppm) but  
 397 lower than that in December (above 400 ppm). That is because  
 398 the photosynthesis in early spring is weaker than that in Sep-  
 399 tember but stronger than that in December in Munich. More-  
 400 over, the averaged atmospheric temperature during the study  
 401 period (about 8 °C) is lower than in September (15 °C) but  
 402 higher than in December (0 °C), leading to the height of the  
 403 planetary boundary layer (PBL) stay between the heights of  
 404 these two months. The sun heats up the ground surface in  
 405 the day, thus the PBL increases while the CO<sub>2</sub> concentration  
 406 decreases. At night, the opposite occurs: the drop of the PBL  
 407 increases the CO<sub>2</sub> concentration [40].

408 The ground-based CO<sub>2</sub> concentration is also influenced by  
 409 the anthropogenic activities. Compared with the data measured  
 410 on weekends, peak curves can be found in the morning from  
 411 06:00 to 10:00 on the workdays in Fig. 8(a). This is likely  
 412 caused by rush-hour traffic increases between these hours,  
 413 which results in increasing the CO<sub>2</sub> concentration. On the  
 414 weekends, when the weather was fair, there was no rush-hour  
 415 peak at these hours, as can be seen in Fig. 8(b) [41]. This  
 416 phenomenon indicates that the human activities have a great  
 417 influence on the CO<sub>2</sub> concentration in urban areas. Not only  
 418 the special events like the festival celebrations in our previous  
 419 study, but also the daily activities have a noticeable influence  
 420 on the air quality in urban areas [30]. The above analysis  
 421 demonstrates that the diurnal variation of CO<sub>2</sub> concentration  
 422 in urban areas is an integrative role combining the vegetation  
 423 photosynthesis and respiration, the PBL (atmospheric temper-  
 424 ature), and the daily anthropogenic activities of that area.

#### 425 D. Air Trajectory Analysis

426 Nowadays, combining measurements with simulations is a  
 427 conventional way to study and control carbon emissions in  
 428 urban areas. The HYSPLIT (Hybrid Single Particle Lagrangian  
 429 Integrated Trajectory) model is a common method to establish  
 430 locations of emission sources from the receptor site [42].  
 431 Combined with the measured gas concentration at the time  
 432 when the air parcel arrives at the measurement site, the air  
 433 backward trajectories depict the air movement and gas dis-  
 434 tribution on the calculated paths. The PSCF (Potential Source  
 435 Contribution Function) calculates the probability that describes  
 436 the spatial distribution of probable source locations. The PSCF  
 437 value is given as:  $PSCF = m_{ij}/n_{ij}$  in which  $n_{ij}$  is the total  
 438 number of trajectories that pass through the cell  $(i, j)$  and  $m_{ij}$   
 439 is the number of trajectories resulting in gas concentration

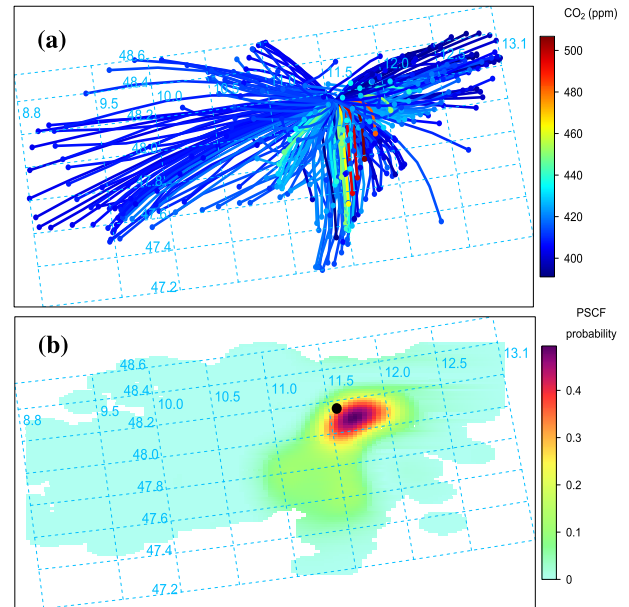


Fig. 9. (a) Six-hour backward air trajectories combined with the measured CO<sub>2</sub> concentration (Fig. 7). (b) PSCF plot with over 75<sup>th</sup> percentile (CO<sub>2</sub>: 420 ppm); the black circle is the measurement site.

440 that greater than a specific threshold (75<sup>th</sup> percentile of CO<sub>2</sub>  
 441 concentration in the study, 420 ppm) [43], [44].

442 As illustrated in Fig. 9, the backward trajectories are  
 443 calculated hourly combined with CO<sub>2</sub> concentration ending  
 444 at the measurement site (receptor) (48.151° N latitude and  
 445 11.568° E longitude) during the whole measurement period  
 446 (Fig. 7) and then processed by the Openair package in R [45].  
 447 Six-hour backward trajectories are selected because the time  
 448 is sufficient to determine the probable locations of both local  
 449 and regional sources in urban areas [46]. The trajectories are  
 450 divided into 0.05° × 0.05° cells and the PSCF plot is smoothed  
 451 as shown in Fig. 9(b), where the black circle is the position  
 452 of the measurement site located at Munich. The cells are  
 453 colored according to the PSCF values, with the dark-red part  
 454 illustrating the highest probability of the source location. The  
 455 measurement site is in the north of Munich city center, where  
 456 the Munich Central Station, the Old Town and shopping malls  
 457 locate at its southeast and are within a radius of 5 km.

458 As indicated in Fig. 9(a), the air mass was primarily from  
 459 the east, south and west directions, and few occurrence of  
 460 air was from the north during the study period. The air from  
 461 the south direction was much more polluted than that from  
 462 east and west. From Fig. 9(b), we can learn that the darkest  
 463 part is in the southeast of the measurement site, demonstrating  
 464 the main emission source from this area in the period, which  
 465 corresponds to the district with a high population density and  
 466 high CO<sub>2</sub> emissions. The preliminary air trajectory analysis  
 467 has exhibited that when combined with the air trajectory  
 468 model, the measurement results can be used for emission  
 469 assessment. Therefore, our developed system can be applied  
 470 in studying the CO<sub>2</sub> distribution and predicting the pollutant  
 471 emission sources in urban areas.

#### 472 IV. CONCLUSION

473 In conclusion, this paper developed a measurement system  
 474 to autonomously eliminate the RAM in the first harmonic,

and measure the gas concentrations using the broad scanning range VCSEL. At first, the method of first harmonic detection was proposed. Then, a digital signal processing pipeline was introduced to autonomously eliminate the RAM, calibrate the wavelength and light intensities, and infer gas concentrations. Subsequently, the CO<sub>2</sub> and H<sub>2</sub>O measurements were implemented in both the stable environment and the field areas to verify the precision and accuracy of the developed system. According to the Allan-Werle Variance Analysis, widening the wavelength tuning range can enhance the precision of the developed system. The precision of the first harmonic detection was nearly doubled compared with the traditional second harmonic detection. The field measurements carried out in early spring of 2018 in Munich were compared with the commercial NDIR sensor. The results indicated that our developed system displayed high accuracy and had high consistency with the NDIR sensor. Further analysis revealed that the diurnal variations of the atmospheric CO<sub>2</sub> concentration in urban areas are the comprehensive combination of the biosphere and meteorological conditions, and the local daily anthropogenic activities. The backward air trajectories were calculated based on the HYSPLIT model and PSCF method, the preliminarily results have shown that the CO<sub>2</sub> emission sources mainly come from the southeast of Munich. According to the experimental and analysis results, the developed system presented in this article has a great potential for measuring the *in-situ* GHG concentrations, analyzing the polluted gas distributions, and validating the pollutant transport model in urban areas.

#### APPENDIX A THEORY OF WMS

Wavelength modulation spectroscopy (WMS) is a method for sensitive absorbance measurements which uses a significantly faster sinusoidal signal riding on a slowly varying diode laser injection current. Instead of the transmission spectrum, the harmonic signals are obtained via the LIA. Due to its advantages of efficient noise suppression, for example, insensitive to  $1/f$  noise, WMS enables to increase the sensitivity, precision and SNR in the trace gas measurements and the harsh environments. In TDLAS-WMS, when the laser is tuned by the low-frequency ramp and high-frequency sinusoidal signals, the instantaneous wavenumber and light intensity are expressed as:

$$\begin{cases} v(t) = \bar{v} + a \cos(\omega t + \eta) \\ I_0(t) = \bar{I}_0 + I_1 \cos(\omega t + \eta + \psi), \end{cases} \quad (4)$$

where  $\bar{v}$  [cm<sup>-1</sup>] and  $\bar{I}_0$  denote the central wavenumber and central light intensity, they are the wavenumber and intensity of the central laser emission (without the sinusoidal modulation) which implemented by the slow ramp signal;  $a$  [cm<sup>-1</sup>] is the modulation depth and the modulation index is  $m = a/\gamma$  where  $\gamma$  is the linewidth;  $I_1$  is the modulation intensity;  $\omega$  [rad/s] is the modulation angular frequency;  $t$  [s] is the time;  $\psi$  is the phase shift between the wavelength and intensity modulation; and  $\eta$  is the phase shift in wavelength with respect to the tuning current. The  $\eta$  is an arbitrary value in each measurement since the start recording point of the waveform is

unfixed. The light intensity phase is  $(\eta + \psi)$  and  $\theta$  is defined as  $\theta = \omega t + \eta$ . Based on the Beer-Lambert Law, the transmitted light intensity ( $I_D$ , detected) is:

$$\begin{aligned} I_D(t) &= I_0(t) \exp[-PS(T)Lc\varphi(v(t))] \\ &= \sum_{k=0}^{\infty} I_{k\theta}^X \cos k\theta - \sum_{k=0}^{\infty} I_{k\theta}^Y \sin k\theta, \end{aligned} \quad (5)$$

where  $P$  [atm],  $S(T)$  [cm<sup>-2</sup>/atm],  $T$  [K],  $L$  [cm], and  $c$  are the total gas pressure, line strength, temperature, absorbing path length, and gas concentration, respectively;  $\varphi$  [cm] is the line shape which is a function of  $v(t)$  and can be expressed as a Voigt profile [47];  $I_{k\theta}^X$  and  $I_{k\theta}^Y$  are the  $k$ -th ( $k = 0, 1, 2, 3, \dots$ ) Fourier components of the transmitted light intensity:

$$\begin{cases} I_{0\theta}^X = \bar{I}_0 A_0 + 0.5 I_1 A_1 \cos \psi, & I_{0\theta}^Y = 0 \\ I_{1\theta}^X = \bar{I}_0 A_1 + I_1 \cos \psi (A_0 + 0.5 A_2) \\ I_{1\theta}^Y = I_1 \sin \psi (A_0 - 0.5 A_2) \\ I_{k\theta}^X = \bar{I}_0 A_k + 0.5 I_1 \cos \psi (A_{k-1} + A_{k+1}) \\ I_{k\theta}^Y = 0.5 I_1 \sin \psi (A_{k-1} - A_{k+1}), & k = 2, 3, \dots, \end{cases} \quad (6)$$

where  $A_k$  are the  $k$ -th order Fourier components of the transmittance,  $A_k = PS(T)LcH_k$  in which the  $H_k$  is the  $k$ -th order Fourier components of the spectral line shape. In LIA, the  $k$ -th Fourier components can be fixed by the same frequency reference signals as:

$$\begin{cases} X: [I_{k\theta}^X \cos k\theta - I_{k\theta}^Y \sin k\theta] \cos(k\omega t + \beta_k^X) \\ Y: [I_{k\theta}^X \cos k\theta - I_{k\theta}^Y \sin k\theta] \sin(k\omega t + \beta_k^Y), & k = 0, 1, 2, \dots \end{cases} \quad (7)$$

From Eq. 7, it can be seen that the amplitudes of the harmonic in X and Y axes are decided by the relationship between the phase shift in wavelength ( $\eta$  or  $k\theta$ ) and the phases of the reference signal ( $\beta_k^X$  and  $\beta_k^Y$ ). Due to the arbitrary of  $\eta$ , the amplitudes of the harmonic in X and Y axes are variable in each measurement. Generally, the magnitude of the Fourier components is used as the complete harmonic signal:  $S_{kf} = \sqrt{I_{k\theta}^X{}^2 + I_{k\theta}^Y{}^2} \approx \bar{I}_0 A_k$  when the RAM can be neglected. However, this method is invalid in the first harmonic since the RAM is strong. Or when setting the phases of the reference signal:  $\beta_k^X = \beta_k^Y = k\eta$ , the  $k$ -th Fourier components can accumulate on their own axes as:

$$\begin{cases} X_{kf} = I_{k\theta}^X \\ Y_{kf} = I_{k\theta}^Y. \end{cases} \quad (8)$$

#### APPENDIX B MODULATION INDEX

The amplitudes of the first, second and third harmonics vary with the modulation index ( $m$ ) are calculated as shown in Fig. 10 and Table II, where the gas parameters are the same as Fig. 5. As indicated in the figure and table, when  $m = 2.0$  or  $2.2$ , the first and second harmonics would reach to their maximum values while the amplitude of the third harmonic is only 88% of its maximum. When  $m$  increases to 3.0, the percentage of the third harmonic will raise to

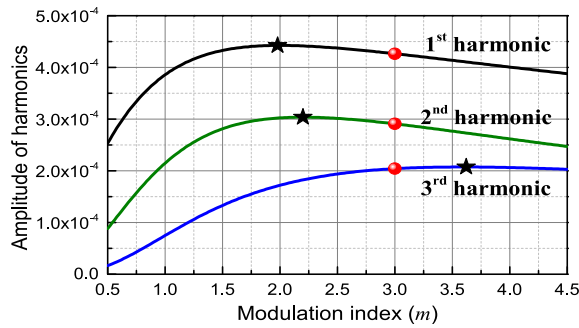


Fig. 10. The amplitudes of the first, second and third harmonics vary with modulation index ( $m$ ) from 0.5 to 4.5. The black stars denote the maximum at each harmonics and the red dots are the harmonic amplitudes at  $m = 3.0$ .

TABLE II

OVERVIEW OF THE HARMONICS AT DIFFERENT MODULATION INDICES, THE PERCENTAGE DATA ARE THE HARMONICS AMPLITUDES COMPARED WITH THEIR OWN MAXIMUM ( $m_{MAX}$ )

	$S_{1f}$	$S_{2f}$	$S_{3f}$
$m_{max}$	2.0	2.2	3.6
$m=2.2$ , percent of maximum	99.8%	100%	88.0%
$m=3.0$ , percent of maximum	96.4%	95.8%	98.4%

98.4%, while the amplitudes of the first and second harmonics are still  $>95\%$  of their maximums. When setting  $m = 3.0$ , the high SNR harmonics, especially the third harmonic, will be obtained.

#### APPENDIX C MODULATION DEPTH

According to Eq. 4, the instantaneous wavenumber can also be expressed as determined by the tuning current ( $i$ ):

$$v(i) = c_2(i - i_0)^2 + c_1(i - i_0) + c_0, \quad (9)$$

where  $i$  is transferred from the tuning voltage (ramp signal) and the voltage-to-current is determined by the laser controller (5 mA/V in the system);  $i_0$  is the fixed current which can be set as the current at the line centers. The coefficients ( $c_2$ ,  $c_1$ , and  $c_0$ ) can be inferred from the measured line centers. Then, the modulation depth can be calculated by:

$$a = \frac{dv(i)}{di} I_1 \zeta(\omega) = [2c_2(i - i_0) + c_1] I_1 \zeta(\omega), \quad (10)$$

where  $\zeta(\omega)$  is the frequency dependency of the current-to-wavenumber tuning coefficient, the value can be seen in [29] and [48].

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