

Technische Universität München

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Development of a Theoretical Workflow for Metabolic Engineering and its Application to Terpenoid Production in *Escherichia coli*

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千里之行,始於足下

A journey of a thousand miles begins with a single step *Laozi*

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Abstract

Metabolic Engineering is an emerging science aiming at the development of cellular factories for the overproduction of valuable chemicals. Target molecules can be either naturally produced by endogenous metabolic pathways, or the host metabolism should be complemented by a non-inherent metabolic pathway to enable their heterologous production. Over the past decades, mathematical modeling of cellular metabolism for strain and process optimization has given rise to a more rational, model-based Metabolic Engineering science. However, theoretical workflows providing advice on limitations and proper application of the vast number of available mathematical tools are still scarce. Initially, we review the application of mathematical methods to increase the production of succinate in engineered strains. Succinate is an important building block whose biotechnological production has gained much attention in the last decade. From this initial work, we conclude that direct experimental implementation of model predictions (in silico knowledge) is not a straightforward process yet. One of the many reasons is the intrinsic complexity of living systems, which cannot be fully captured by the simplicity of widely used stoichiometric models of metabolism. Additionally, incongruences in the modeling process and the reporting of experimental results hamper a proper assessment of the prediction power of current modeling approaches. Motivated by these observations, we developed a theoretical workflow for metabolic engineering, highlighting capabilities and limitations of each method. The workflow considers the application of not only constraint-based methods like Flux Balance Analysis (FBA), which have been traditionally used to understand optimality principles shaping bacterial metabolism, but also of kinetic-based methods whose spread has been hindered so far by limitations related to model parametrization and to high demand on computational power required to analyze genome-scale kinetic models. While developing the workflow, we paid special attention to consider the so-called metabolic burden, a phenomenon presented in "loaded" cells and characterized by the reduction of both biomass yield and critical growth rate for acetate secretion. The suggested protocol was mainly applied to generate *in silico knowledge*, aimed to guide future experimental efforts towards optimization of taxadiene production in *Escherichia coli* (E. coli) at the strain and process level. Taxadiene is a precursor molecule for the anticancer drug taxol and its biotechnological production has gained much attention due to the low yields of the traditional extraction process from the bark of the pacific vew tree. During the development of a flexible taxadiene producing strain, simultaneous utilization of glucose and xylose by E. coli was also analyzed. By applying various tools described in the protocol, metabolic load and effects arising from simultaneous sugar uptake were assessed, especially focusing on the production potential of each strain. This analysis should allow the selection of strain candidates for further optimization.

1. Introduction

Terpenes are naturally synthesized compounds formed by the ligation of activated isoprene molecules isopentenyl diphosphate (IPP) and its isomer dimethylallyl diphosphate (DMAPP). In nature, IPP and DMAPP can be synthetized through two different metabolic routes: the mevalonate (MVA) or the 2-C-methyl-D-erythritol 4-phosphate (MEP) pathway. Terpenoids, i.e. functionalized terpenes, have a wide range of applications in the food, cosmetic and pharmaceutical industry. Lycopene, taxol and artemisinin are some of the most prominent examples of terpenoid molecules. Taxol, more specifically, is a potent plant-derived drug, showing anticancer activity against various cancer types. It was first isolated from the slow-growing pacific yew tree (*Taxus brevifolia*) and its early production method required the processing of two to four adult trees to provide dosage for one single patient [140]. Due to its structural complexity (see Figure 1.1.A), total chemical synthesis approaches often require many steps and exhibit low total yields [101]. Current large scale production methods encompass semi-synthetic approaches based on a plant derived precursor (baccatin III, extracted from the needles of the European yew tree Taxus baccata [140]) and plant cell cultures [43]. Since these methods still depend on plantbased processes, they exhibit an inherent limited scalability and productivity. Moreover, they offer only marginal economic benefits and are associated with several environmentally hazardous processing steps. By contrast, biotechnological taxol production has been identified as a sustainable and economically interesting alternative to established production methods. Potential advantages of the this approach include:

- 1. High productivity and scalability due to rapid microbial growth rate.
- 2. Conservation and preservation of natural resources because, in contrast to *Taxus* brevifolia, bacterial host cells like *E. coli* can be sustainably produced in high quantities.
- 3. Access to novel taxol derivatives by applying tools of synthetic biology and metabolic engineering.

As schematically shown in Figure 1.1.B, the project $\mathbf{SysBioTerp}$ aims at the successive production of taxol derivatives using an *E. coli*-based production platform. Taxadiene is the first committed intermediate in the synthesis of taxol and therefore, the first molecule to be produced and characterized. Sequential functionalization steps include acetylation, hydroxylation, oxidation and benzylation. Since it has been reported that taxol derivatives might have beneficial effects on human health, biological activity of novel taxoids produced by metabolically engineered *E. coli* strains should be assessed in a final bio-screening step.

Due to the project complexity and scale, different research groups were involved, each one working on different aspects of the project. The study at hand was performed at the

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Figure 1.1.: Motivation & Project's Aim Motivation and project's aim is shown. A. Taxol is a potent plant-derived drug used to treat a number of types of cancer, including ovarian, breast, lung, cervical, and pancreatic cancer. Before current production methods were developed, producing enough taxol to provide dosage for one patient required the processing of two to four adult, slow-growing *Taxus brevifolia* trees. B. The SysBioTerp project aims at the development of a *E. coli*-based taxoid production platform, thus contributing to the development of sustainable and environmentally friendly production processes. Additionally, produced taxoids should undergo a bioactivity screening. More specifically, anticancer and antimicrobial activity of each novel taxoid should be determined.

specialty division for systems biotechnology (SBT). The task of our group was the datadriven development and implementation of modeling approaches on both the process and microbial metabolism level. From this task, three goals are derived:

- 1. Reduction of metabolic burden caused by heterologous enzyme overexpression. Metabolic burden is a phenomenon observed in microorganisms supporting plasmid-based enzyme overexpression. It is characterized by a reduction of the overall cellular fitness, which leads to a reduction of cellular growth rate, a reduction of biomass yield and early acetate secretion [11,15,58]. Since the native *E. coli* metabolism has to be expanded and re-directed by expressing a number of native and heterologous enzymes to allow for taxoid production, it is expected that metabolic burden will be a major factor limiting the production capabilities of the selected host *E. coli*. In a first step, detrimental effect of enzyme overexpression on cellular fitness should be experimentally characterized. Then, model-driven strategies aiming at the minimization of the metabolic burden should be developed and if possible, experimentally validated.
- 2. Development of production strains through rational design. Over the past years, the emerging science of Metabolic Engineering [7, 139] has allowed the construction of

microbial cellular factories for the overproduction of many relevant target molecules. The development of genome-scale metabolic reconstructions, which are mathematical representations of the cellular metabolism, together with strain-design algorithms, which employ metabolic reconstructions to identify genetic perturbations leading to the overproduction of the target molecule, has given rise to the development of a more rational, model-based Metabolic Engineering. Consequently, state of the art mathematical tools and modeling approaches should be applied to guide the process of strain development, which should ultimately lead to the construction of an optimal taxoid production strain.

3. Optimization of bio-reactor parameters for maximal process performance. It is expected that optimal reactor parameters (production temperature, time point of culture induction, aeration level, etc.) that maximize performance indicators, such as yield or productivity, will be highly strain dependent and must therefore be independently identified for each new production strain. Aiming at the reduction of this time-consuming and costly experimental work, modeling approaches should be applied to guide and accelerate experimental process optimization.



Figure 1.2.: Modeling Workflow. Interdependencies between our three main goals, minimization of metabolic burden, strain development and process optimization, should be consistently addressed during the modeling process in order to generate integral optimization strategies leading to maximal overall process performance. Data provided by our cooperation partners for model construction mainly consisted of concentration time courses for biomass, substrate, acetate and product. Additionally, cellular metabolism of selected strains was elucidated by means of ¹³C labeling experiments. Applied modeling approaches encompassed both stoichiometric- and kinetic-based methods.

Figure 1.2 shows schematically each of these three goals and the interactions between them. Clearly, all three task - minimization of metabolic burden, strain development and process optimization - are interdependent. For instance, optimal process parameters will necessarily depend on the production strain genotype. Additionally, strategies aiming at reducing the metabolic burden caused by enzyme overexpression will certainly depend on the extend and identity of the enzymes being overexpressed, which in turn is substantially defined by the target molecule. These dependencies should be consistently addressed during the modeling process in order to generate integral optimization strategies leading to

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maximal process performance.

The work at hand is not the first model-driven optimization approach ever developed. The same holds true for mathematical tools to be developed. Indeed, the number of existing strain-design algorithms is vast [87]. However, with very few exceptions [170], existing mathematical approaches have been mainly focused on single aspects - strain design, process optimization or minimization of metabolic burden-. Additionally, theoretical workflows providing advice on limitations and proper application of these mathematical tools are still scarce. Consequently, newly developed as well as existing computational methods should be framed into a theoretical workflow addressing the issue of model-driven process optimization in an integral fashion, considering all three previously mentioned aspects and their interdependecies.

This thesis is divided into three parts. We start describing the theoretical methods used in this work and propose a workflow for Metabolic Engineering. The results obtained from the application of this workflow to the terpenoid production in $E.\ coli$ are described in the second and third part. Part I. Theory

2. Metabolic Modeling & Strain Engineering

Modeling the cellular metabolism provides a deep understanding of the cellular response to environmental or genetic perturbations and enables the rational design of cellular factories. The aim of strain engineering is to redirect the metabolism of these cell factories in order to maximize the bio-synthesis of natural or non-natural target products. This is achieved through genetic modifications of the host genotype or through adequate culture conditions, i.e. medium composition, culture temperature, etc. Modeling the cellular metabolism can be a challenging task. Additionally, the proper approach greatly depends on the level of detail required for the specific application. Over the past decades, many mathematical approaches have been proposed. Each method is based on different assumptions and consequently, allows for different types of predictions. In general, the cellular metabolism can be mathematically described by setting up a mass balance for all metabolites in the cell:

$$\frac{dc}{dt} = \mathbf{S} \ r - \mu \ c, \tag{2.1}$$

where r is the vector of fluxes through the reactions, μ is the growth rate, c is a vector of intracellular metabolite concentrations and **S** represents the stoichiometric matrix of the reaction network. The first term represents the rates of consumption or production of a specific metabolite, while the second describes the dilution rate caused by cell growth. Since the dilution rate is normally much lower than the reaction rates, the Equation (2.1) can be simplified to:

$$\frac{dc}{dt} = \mathbf{S} \ r. \tag{2.2}$$

At steady state, there is no accumulation of metabolites in the cell and Equation (2.2) can be further simplified to:

$$0 = \mathbf{S} \ r. \tag{2.3}$$

In the following sections, the three most commonly used modeling approaches for analyzing Equation (2.3) are presented, namely kinetic-, constraint- and elementary modes-based methods.

2.1. Constraint-based Methods

Since the stoichiometric matrix \mathbf{S} of a real biological network is typically non-square, containing more unknown rates than equations, it does not have an inverse. Consequently, a flux vector r satisfying Equation (2.3) is not *unique*. Additional constraints on the flux vector r can be applied to further reduce the number of allowable flux distributions [31]. Limits on the range of individual flux values can be used for this purpose: thermodynamic constraints expressed as reaction reversibility can thus be included by setting one of the boundaries of an irreversible reaction to zero [53]. In a similar way, maximum flux values can be estimated based on enzymatic capacity limitations [13], or for the case of exchange reactions (i.e. reactions that transfer mass between the culture medium and the cell), experimentally determined maximal uptake or production rates can be used. Regulation of gene expression can also be considered in cases where the regulatory effects have a great influcence on cellular behavior [32]. Usually, these constraints are not sufficient to reduce the solution space to a single solution. Constraint-based models have been popularly used to calculate a flux vector r that represents the cellular phenotype at steady-state using different approaches. Flux Balance Analysis (FBA) has been the most widely applied method. It consists of a linear programming formulation that, by imposing an objective function, enables the calculation of a flux distribution that maximizes or minimizes that objective. Typically, the objective function used coincides with an assumed cellular objective, such as growth. Other commonly used cellular objectives include the sum of all intracellular fluxes or ATP generation [128]. Mathematically, the FBA formulation reads:

Maximize
$$Z = c r$$

subject to:
 $\mathbf{S} r = 0$
 $lb \leq r \leq ub,$ (2.4)

where Z is the objective function resulting from a linear combination of selected reactions of the flux vector r, as determined by the vector c. lb and ub are lower and upper flux boundaries, respectively.

Due to redundancies in the architecture of the cellular metabolism, alternate optimal solutions can exist. Mahadevan et al. [88] introduced the concept of Flux Variability Analysis (FVA) to characterize this issue. The approach begins with determining the optimal value of the objective function by solving the linear optimization problem outlined in Equation 2.4. From this solution, the range of variability that can exist in each flux in the network due to alternate optimal solutions can be calculated through a series of optimization problems. In each problem, the value of the original objective ($Z_{optimal}$) is fixed and each reaction in the network is maximized (Equation 2.5) and minimized (Equation 2.6) to determine the feasible range of flux values for each reaction. The mathematical formulation of the FVA reads:

Maximize
$$r_i$$

subject to:
 $c \ r = Z_{optimal}$ (2.5)
 $\mathbf{S} \ r = 0$
 $lb \leqslant r \leqslant ub$,

Minimize
$$r_i$$

subject to:
 $c \ r = Z_{optimal}$ (2.6)
 $\mathbf{S} \ r = 0$
 $lb \leqslant r \leqslant ub,$

If for a given reaction it holds that $r_{max} = r_{min}$ (r_{max} and r_{min} are obtained from Equations 2.5 and 2.6 respectively), then no variability is allowed for that reaction and a unique flux value associated to that reaction is required to obtain $Z_{optimal}$.

Constraint-based approaches have been very popular within the modeling community. This popularity can be partly attributed to the simplicity of the mathematical tools required (linear programming), but also to the availability of metabolic reconstructions for many industrially relevant microorganisms [66]. For the specific case of *E. coli*, much work has been done during the past decade towards the development of a comprehensive genome-scale metabolic reconstruction. More specifically, Table 2.1 presents an overview of efforts made by the laboratory of Bernhard Palsson at UC San Diego. Traditionally, metabolic reconstructions have been limited to a stoichiometric description of the cellular metabolism (**S** matrix in Equation 2.3). However, models have been growing in coverage to consider additional aspects of cellular metabolism such as macromolecular expression [102] and protein 3D structures [97]. In this work, we extensively used the *E. coli* core model [107] as well as the *i*JO1366 genome-scale metabolic reconstruction [106].

Table 2.1.: Genome-Scale Metabolic Reconstructions for *E. coli*. The *E. coli* core model was extensively used in this work. It encompasses central metabolic pathways like glycolysis, pentose phospahte pathway, tricarboxylic acid cycle and pyruvate metabolism. As the metabolic reconstructions grow in scope, it is possible to simulate more complex genotypes. However, the analysis of associated flux distributions become more challenging. The model *i*JO1366 was the last genome-scale reconstruction considering only a stoichiometric description of the metabolism. All subsequent models consider additional features such as macromolecular expression and protein 3D structures.

| | <i>E. coli</i> core [107] | <i>i</i> JR904 [114] | <i>i</i> AF1260 [41] | iJO1366 [106] | <i>i</i> ML1515 [97] |
|--------------------|---------------------------|----------------------|----------------------|---------------|----------------------|
| Included genes | 137 | 904 | 1260 | 1366 | 1515 |
| Reactions | 95 | 931 | 2077 | 2251 | 2719 |
| Exchange reactions | 20 | 143 | 298 | 329 | 338 |
| Metabolites | 72 | 761 | 1039 | 1136 | 1192 |

iML1515 additionally contains 1515 protein 3D stuctures and 1888 unique protein domains

2.1.1. Dynamic Flux Balance Analysis

Equation 2.4 allows the calculation of steady state flux distributions for a given objective function and set of constraints. Assuming that microorganisms are able to rapidly reach steady state in response to changes in the extracellular environment (bio-reactor), it is possible to couple the FBA formulation with a set of differential equations describing the reactor dynamics to simulate time courses of extracellular species within the bio-reactor. This approach is termed dynamic Flux Balance Analysis (dFBA) and is schematically represented in Figure 2.1.



Figure 2.1.: Dynamic Flux Balance Analysis. Reactor dynamics can be coupled with bacterial metabolism to simulate concentration time courses of chemical species present in the bioreactor. The coupling is done through the cellular growth rate μ and exchange rates r_{Si}^{e} . Refer to Equations 2.11 and 2.12

Equations 2.8, 2.11 and 2.12 fully describe the dynamics of reactor volume, biomass concentration and concentration of extracellular metabolites in the bioreactor, respectively. Symbols used in these equations can be found in Table 2.2. Note that the coupling between reactor dynamics and cellular metabolism occurs through the growth rate μ and exchange rates r_{Si}^e .

The equation describing the dynamic of reactor volume is determined as follows. We first set up a mass balance equation for the bio-reactor:

$$\frac{dm_R}{dt} = \sum q_{in,j}\rho - q_{out} \rho \qquad (2.7)$$

If the density ρ can be assumed to be constant and since $m_R = V_R \rho$, it follows that:

$$\frac{dV_R}{dt} = \sum q_{in,j} - q_{out} \tag{2.8}$$

In order to model the biomass dynamics, it is assumed that any feed to the bio-reactor do not contain cells. The differential equation describing the change of biomass in the reactor reads:

$$\frac{dm_B}{dt} = \mu \ m_B - q_{out} \ c_B \tag{2.9}$$

Table 2.2.: Overview of Variables Used to Describe Reactor Dynamics. In order to set up mass balance equations discussed in the main text, multiple volumetric feeds are assumed (one for each substrate). By contrast, one single volumetric efflux is considered. Note that c_{Si} refers to the concentration of metabolite *i* in the reactor, while c_{Si}^{in} corresponds to the concentration of metabolite *i* in the corresponding volumetric feed. gDW is used to describe the concentration of biomass and refers to gram dry weight.

| Name | Symbol | Units |
|---|---------------|------------------|
| Density | ρ | g/l |
| Reactor volume | V_R | 1 |
| Growth rate | μ | $1/\mathrm{h}$ |
| Volumetic feed | $q_{in,j}$ | l/h |
| Volumetric efflux | q_{out} | l/h |
| Mass in reactor | m_R | g |
| Biomass | m_B | g |
| Mass of component i | m_{Si} | g |
| Biomass concentration | c_B | $\mathrm{gDW/l}$ |
| Concentration of component i in the reactor | c_{Si} | g/l |
| Concentration of component i in the feed | c_{Si}^{in} | g/l |
| Molecular weight of component i | w_{Si} | m g/mol |
| Exchange reaction for component i | r^e_{Si} | mol/gDW h |

For convenience, the biomass dynamics is now expressed in terms of biomass concentration. This is done by expressing the biomass in the reactor as a function of the biomass concentration and the reactor volume:

$$\frac{dm_B}{dt} = \frac{d(V_R \ c_B)}{dt} = V_R \frac{dc_B}{dt} + \frac{dV_R}{dt} \ c_B \tag{2.10}$$

Substituting Equation 2.10 and 2.8 into Equation 2.9 and solving for biomass concentration leads to:

$$V_R \frac{dc_B}{dt} + \frac{dV_R}{dt} c_B = \mu \ m_B - q_{out} \ c_B$$

$$\frac{dc_B}{dt} = \mu \ c_B - \frac{\sum q_{in,j}}{V_R} \ c_B$$
(2.11)

The mass balance for chemical species (substrates/products) in the liquid phase is derived in a similar way as for the biomass. In this case, exchange reactions r_{Si}^e between the cell and culture media have to be considered. Exchange rates will have a positive sign for products secreted by the cell, whereas a negative sign refers to substrates absorbed by the cell.

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$$\frac{dm_{Si}}{dt} = q_{in,j} \ c_{Si}^{in} - q_{out} \ c_{si} + r_{Si}^{e} \ c_{B} \ V_{R} \ w_{Si}$$

$$\frac{dc_{Si}}{dt} = \frac{q_{in,j}}{V_{R}} c_{Si}^{in} - \frac{\sum q_{in,j}}{V_{R}} \ c_{Si} + r_{Si}^{e} \ c_{B} \ w_{Si}$$
(2.12)

The mass balance equations derived for biomass, reactor volume and components in the liquid phase can be used to describe the dynamics of a continuous $(q_{in,j} \neq 0; q_{out} \neq 0)$, a batch $(q_{in,j} = q_{out} = 0)$, or a fed-batch process $(q_{in,j} \neq 0, q_{out} = 0)$.

2.1.2. Experimental Determination of Reaction Rates

As stated before, experimentally determined reaction rates can be used to constrain the space of allowable flux distributions satisfying the linear programming problem defined by Equation 2.4. By doing so, the biological significance of the obtained flux distributions can be increased. Since ordinary measurements of concentration time courses in the fermentation broth allows the estimation of exchange rates (rates describing the exchange of mass between the cell and the culture medium, that is substrate uptake, product and by-product secretion rates), these are normally used to constraint the solution of Equation 2.4. Additionally, more complex data, such as the obtained in ¹³C labeling experiments can also be used to estimate a number of intracellular rates. The methodology used in this work to calculate both exchange and intracellular rates from experimental data will be discussed in this section.

Determination of Exchange Rates

Concentration time courses for the substrate (or substrates) and the product are usually available for modeling studies, because this data are routinely obtained during experimental strain characterization to assess the production performance of a given strain. Time courses for by-products like acetate, ethanol, pyruvate, lactate, etc. might also be available, since their signals are normally contained in the chromatogram used to quantify the main carbon source if a standard High Performance Liquid Chromatography (HPLC) method is used for sugar quantification. Figures 2.2.A and 2.3.A show exemplary concentration time courses for biomass and glucose, respectively. In the case of biomass, Optical Density (OD) measurements along with a conversion factor have been traditionally used to determine the biomass concentration in the culture in units of gram dry weight (gDW) per liter. It has been shown that the gDW/OD conversion factor strongly depends on the genetic background of the strain [83]. In this study, strain-specific conversion factors were used to obtain biomass concentration in units of gDW/l. For the specific case shown in Figure 2.2.A, a conversion factor of 0.54 was used to calculate the biomass concentration in units of gDW/l.

The first step to calculate any exchange rate is the determination of the cellular growth rate μ . As shown in Equation 2.13, μ is a proportionality constant used to describe the increase of the biomass concentration over time as a function of the biomass concentration in a certain point in time:

$$\frac{dc_B}{dt} = \mu \ c_B \tag{2.13}$$

As defined in section 2.1.1, c_B refers to the biomass concentration. Equation 2.13 is obtained by setting $\sum q_{in,j}$ to zero in Equation 2.11. This is true for a batch process or when the total volumetric feed $\sum q_{in,j}$ is low compared to the total volume of the reactor. By assuming that μ is not a function of time, Equation 2.13 can be integrated to obtain:

$$ln(c_{B,f}) = \mu(t_f - t_o) + ln(c_{B,o}).$$
(2.14)

 t_o and t_f refer to the initial and final time points, while $c_{B,o}$ and $c_{B,f}$ represent the corresponding biomass concentration. Note that the assumption of constant μ is generally valid during the exponential growth phase. By plotting the natural logarithm of experimentally measured biomass concentration as a function of time, it is possible to calculate μ as the slope of the resulting straight line. Figure 2.2.B shows this procedure for the biomass concentration time course shown in Figure 2.2.A. In this case, the analyzed culture had a growth rate of 0.49 1/h.



Figure 2.2.: Experimental Determination of Cellular Growth Rates. A. OD time course B. Natural logarithm of OD measurements as a function of time. The slope of the straight line corresponds to the cellular growth rate μ .

Once μ has been estimated from the experimental OD time course, exchange rates r_{Si}^e can be calculated. As indicated before, strain characterization normally occurs in batch processes (shaking flask). By setting $q_{in,j}$ and $\sum q_{in,j}$ to zero, Equation 2.12 can be simplified to:

$$\frac{dc_{Si}}{dt} = r_{Si}^e c_B w_{Si}.$$
(2.15)

Flux distributions are normally calculated in units of mmol/gDW h. By dividing Equation 2.15 by w_{Si} (molecular weight), it is possible to change the units of the balance equation for the metabolite Si from g/l to mol/l (or mmol/l). Combining Equations 2.15 and 2.13 and solving the resulting equation for r_{Si}^e one obtains:

$$r_{Si}^e = \mu \frac{dc_{Si}}{dc_B}.$$
(2.16)

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Equation 2.16 states that the exchange rate for metabolite r_{Si}^e can be obtained by multiplying the cellular growth rate μ by the slope of the curve obtained when plotting c_{Si} against c_B . Figure 2.3.B exemplarily shows this procedure. The glucose uptake rate $r_{Glucose}^e$ can be then calculated as: (-11.75mmol/gDW)(0.491/h) = -5.75mmol/gDWh. Note that the slopes in Figures 2.2.B and 2.3.B were calculated using least-squares regression.



Figure 2.3.: Experimental Determination of Glucose Uptake Rate. A. Concentration time course for glucose. B. Glucose concentration is plotted against biomass concentration. Note that the biomass concentration was obtained by multiplying OD measurements by a conversion factor of 0.54 gDW/OD. The slope of this straight line corresponds to the term $\frac{dc_{Si}}{dc_B}$ of Equation 2.16.

Determination of Intracellular Rates: ¹³C-Metabolic Flux Analysis

Even though exchange rates can be easily calculated from respective concentration time courses for a number of by-products, they do not provide enough constraints to precisely estimate all fluxes in complex biological systems containing reversible reactions, parallel pathways and internal cycles [5, 127, 157]. ¹³C-Metabolic Flux Analysis (¹³C-MFA) offers a means for the *indirect* estimation of a number of intracellular fluxes [157]. Typically, cells are grown on ¹³C-labeled substrates until the isotope label is distributed throughout the network. The cell reaches isotopic steady state when the labeling patterns do not change over time. At this point, cells are harvested and Mass Spectromety (MS) or Nuclear Magnetic Resonance (NMR) analysis are implemented to detect the 13 C patterns of either protein-bound amino acids or free metabolic intermediates. The analysis of proteinbound amino acids is preferred because protein is stable and abundant. On the other hand, free metabolic intermediates provides the richest source of information, but high turnover and very low concentrations of intermediates poses serious technical challenges to sample preparation, separation and analytical sensitivity [167]. Specific labeling patterns occur in the metabolic intermediates (free intermediates or protein-bound amino acids) as a function of the particular distribution of fluxes in an organism [157]. Indirect estimation means in the context of ¹³C-MFA that intracellular fluxes must be extracted from measured labeling patters using a model-based approach. Comprehensive mathematical models that describe the relationship between metabolite labeling patterns and fluxes are used to simulate isotopic abundances of all metabolites in a network for any set of steady state fluxes. Various mathematical approaches have been developed to describe the relationship between flux distribution and labeling patterns. Usually, these models consist of the complete set of isotopomer (isotope isomer [157]) balances, which may be derived

using a matrix based method as described by Schmidt et al. [126]. Alternative modeling strategies have been proposed based on the concept of cumomer balances [158], bundomer balances [150] and Elementary Metabolite Units (EMU) [6]. Regardless of the approach used, the flux distribution responsible for the measured labeling pattern is identified by minimizing the difference between observed and simulated isotope spectra. In essence, flux determination is a large-scale nonlinear parameter estimation problem:

Minimize
$$\Phi = (x(r) - x^{obs})^T \Sigma_x^{-1} (x(r) - x^{obs})$$

subject to:
 $\mathbf{S} \ r = 0$ (2.17)

where the objective function Φ is the covariance-weighted sum of squared residuals, x(r) is the vector of simulated measurements (which is a function of the flux vector r), x^{obs} is the vector of experimental data containing both labeling measurements and exchange rates measurements, and Σ_x is the covariance matrix, which contains variances of the measurements on the diagonal. Note that the stoichiometric matrix **S** is a $m \times k$ matrix, where m refers to the number of metabolites and k to the number of reactions.

During the iterative optimization process of Equation 2.17, not all flux values in the vector r can be freely chosen by the solver. In fact, there are only $k - rank(\mathbf{S})$ independent variables, also referred to as free fluxes [126,158]. Independent fluxes can be obtained from the general solution of Equation 2.3:

$$r = \mathbf{N} \ u \tag{2.18}$$

Where, N is the null space matrix of **S** and u is the vector of independent fluxes. In order to reduce computational time, one can introduce Equation 2.18 into Equation 2.17 to obtain a new optimization problem in terms of the free fluxes vector u:

Minimize
$$\Phi = (x(u) - x^{obs})^T \Sigma_x^{-1} (x(u) - x^{obs})$$

subject to:
 $\mathbf{N} \ u \ge 0$ (2.19)

Reversible reactions are usually simulated as two independent reactions. Consequently, the constraint $N \ u \ge 0$ requires that all fluxes are non-negative.

Calculating Confidence Intervals for Reactions

Confidence intervals for intracellular fluxes obtained from Equation 2.19 are useful to estimate the precision of a certain reaction flux given a certain set of labeling data. Confidence intervals have been calculated from estimated local standard deviations, but it has been shown that these intervals may not accurately describe the true uncertainty due to inherent nonlinearities of isotopomer balances [5]. In this work, we calculate confidence intervals for fluxes using the approach developed by Antoniewicz et al. [5], in which for each reaction, the sensitivity of the minimized sum of squared residuals is determined as a function of the flux value. The approach starts by stating that the difference between the objective function evaluated at the optimal solution \hat{u} and the objective function when one flux is

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fixed follows a χ^2 -distribution with one degree of freedom:

$$(\Phi(u)|_{r_i=r_{i0}} - \Phi(\hat{u})) \sim \chi^2(1),$$
 (2.20)

where $\Phi(u)|_{r_i=r_{i0}}$ indicates the value of the objective function when the flux *i* is fixed at r_{i0} and the other degrees of freedom are used to minimize the objective function. The $1 - \alpha$ confidence interval for flux *i* is given by the flux values for which following statement is true:

$$\Phi(u)|_{r_i=r_{i0}} \le \left(\Phi(\hat{u}) + \chi^2_{1-\alpha}(1)\right). \tag{2.21}$$

Note that α reffers to the probability of error. The threshold values for $\chi^2_{1-\alpha}(1)$ corresponding to 80%, 90%, 95% and 99% confidence intervals of fluxes are 1.64, 2.71, 3.84 and 6.63, respectively [5]. Thus, in order to obtain accurate confidence intervals we need to determine the minimized sum of squared residuals as a function of the flux value. Small sensitivities of the objective function with respect to changes in a certain flux indicate that that flux cannot be estimated precisely. Conversely, large sensitivities indicate that the flux is well determined [5]. Figure 2.4 illustrate the three-step implementation of this approach for the estimation of the reaction flux of the reaction catalyzed by the enyzme pyruvate dehydrogenase (PDH) and its confidence interval.

- 1. Generate multiple initial flux distributions by sampling free fluxes. Then, solve the optimization problem described by Equation 2.19. Note that not all flux distributions will converge to the same value of the objective function. The optimal flux distribution is the one exhibiting the lowest objective function among all sampled initial flux distributions [48]. See Figure 2.4.A
- 2. In order to estimate the confidence interval for a given reaction, increase and decrease the flux through that reaction starting from the optimal solution obtained in the previous point. For each perturbed flux distribution, solve the optimization problem described by Equation 2.19. See Figure 2.4.B
- 3. Values for the upper and lower bound of the confidence interval can be identified by applying Equation 2.21. See Figure 2.4.C

All confidence intervals reported in this work were calculated using an α of 5% (95% confindence intervals). The number of sampled initial flux distributions varied between 500 and 1000.

2.2. Elementary modes-based Methods

As discussed before, the number of flux vectors r satisfying Equation (2.3) is infinite. Elementary mode analysis calculates all the solutions of Equation (2.3) by adding a nondecomposability or genetic independence constraint to the reaction directionality constraint introduced by the FBA formulation. Genetic independence implies that enzymes catalyzing the reactions in one solution, represented by flux vector r_1 are not a subset of another flux vector r_2 [68, 130]. If this condition is satisfied, the flux vectors r_1 and r_2 belong to the set of elementary modes e. Through this definition all feasible flux distributions r can be



Figure 2.4.: Constraint-based Assessment of Production Capabilities. A. Due to the non-convex nature of the objective function, the problem must be solved several times using different sets of free fluxes. Each one of the 1000 data points in the figure represents a flux distribution. The flux distribution reaching the minimum value of the objective function is considered to be the solution of the problem described by Equation 2.19. B. The sensitivity of the objective function with respect to the flux through the reaction PDH is calculated as explained in the main text. C. 95 and 99% confidence intervals for the PDH reaction is calculated using Equation 2.21 and are given in the Figure. Lower and upper boundaries were calculated by linear interpolation. Note that the flux through the PDH providing the best match to the labeling data corresponds to 21.95 mmol/gDW h.

represented by non-negative linear combinations of the elementary modes:

$$r = \sum_{i=1}^{n} a_i \ e_i \qquad a_i \ge 0.$$
 (2.22)

In contrast to constraint-based approaches, no assumptions on a cellular objective function are required for flux calculation using elementary mode-based methods. As a consequence, these approaches are classified as unbiased, while constraint-based approaches are classified as biased. Other unbiased approaches for the analysis of metabolic networks include Monte Carlo sampling and extreme pathway analysis [122, 125]. Elementary mode based methods have typically been limited to the analysis of small networks, because the enumeration of all elementary modes is computationally expensive. However recent advances in computational algorithms have extended the applicability of elementary mode based methods to the genome scale [18]. Refer to the original publication for more details on the mathematical definition of elementary modes and their identification [130].

An interesting characteristic of the definition of the elementary modes is that they can be interpreted in terms of biochemical functions [130]. Knowing the set of elementary modes existing in a metabolic network allows, among other things, the identification of the pathway with the highest product yield and the assessment of network stability and functionality after gene deletions [129,147]. The concepts of elementary modes were successfully applied for the first time to engineer a bacterial strain by Liao et al. [76], who engineered an *E. coli* strain for the high-efficient production of aromatic amino acid precursors.

2.3. Kinetic-based Methods

Kinetic models can describe the rates of intracellular reactions as a function of enzyme dependent kinetic parameters as well as metabolite and enzyme concentrations participating in the reaction. The rate expressions are then used to describe concentration changes by a set of ordinary differential equations. In terms of Equation (2.2), this means that the rate vector r has the form: r = f(p, c), where p represents kinetic parameters and c metabolite concentrations.

Usually, kinetic approaches have been used to describe the dynamics of small to medium size systems, such as the central metabolism of $E. \ coli \ [14,22,69]$. Despite the high potential of kinetic based methods for strain development, the construction of large-scale kinetic models has been hindered by many difficulties mainly related to unambiguous parameter estimation. This is due to the need for big sets of kinetic parameters and the fact, that the values of individual kinetic parameters and even the form of the kinetic rate laws may need to be adjusted in response to genetic or environmental perturbations [63]. These difficulties have been tackled by many authors [4,21,82,146] and call for alternative modeling strategies which require less parameters or no parameters at all: 'Qualitative and quantitative understanding and corresponding methodologies for designing desired properties of many complex systems have been successfully achieved in the fields of chemistry, physics, and the associted engineering disciplines without knowing all aspects of systems structure and certainly without knowing all parameter values involved. The same must be possible for biology.' [8]. Two approaches popularly used in metabolic engineering that requires no exhaustive knowledge of kinetic parameter values and rely only on the knowledge of the stoichiometry of the reactions in the network, i.e. the stoichiometric matrix \mathbf{S} , were already presented in sections 2.2 and 2.1. In this section, we summarize some of the main aspects of the pioneering work done by the laboratory of James Liao at the University of California (UC) Los Angeles to overcome the issues related to unknown parameter values in large-scale kinetic models. In Chapter 5, 6 and 9, we demonstrate the prediction power of some of these tools and develop new applications based on the theoretical foundation of the Ensemble Modeling approach of metabolic networks [71, 74, 144, 146].

2.3.1. Ensemble Modeling Approach of Metabolic Networks

In a first paper, Tran et al. [146] applied the idea of Ensemble Modeling (EM) to the central metabolism of $E. \ coli$. The approach builds an ensemble of dynamic models that reach the same reference steady state in terms of flux distribution and metabolite concentrations. Within the ensemble, all models share the same kinetic structure but differ in the specific parameter values. Rate laws for each reaction can be assigned to match known mechanisms and regulations [146] or can be automatically generated based in rules involving the number of substrates, products and reversibilities [71, 74, 144] by applying the concept of modular rate laws developed by Liebermeister et al. [78, 79].

The idea of building an ensemble of models instead of using one single model to describe complex dynamic systems is not entirely new. In fact, ensemble forecasting is commonly used in numerical weather prediction [12, 23, 96, 168], where an ensemble of typically 50 models are used to account for mainly two sources of uncertainty, namely errors introduced

by the use of imperfect initial conditions and errors related to imperfections in the model formulation, such as the approximate mathematical methods to solve the equations [12]. Figure 2.5 illustrates the application of ensemble forecasting for path prediction of the hurricane Irma, one of the strongest hurricanes ever observed in the Atlantic. For a given time point, a set of models is parameterized based on the actual hurricane location and satellite data available at that moment (see point ① in Figure 2.5). Then, a set of trajectories is generated, each representing the potential path of the hurricane. In the ideal case, the future location of the hurricane is contained within the prediction of the ensemble (see point ② in Figure 2.5).



Figure 2.5.: Application of Ensemble Forecasting for Path Prediction of Hurricane Irma. A set of models is parameterized based on experimentally measured initial conditions (point ①). Typically, weather models employ up to 10⁷ observations per day to derive physically consistent initial conditions [12]. Each model generates a forecast regarding the path of the hurricane. In the ideal case, the future path of the hurricane is contained within the ensemble prediction (point ②).

In the case of metabolic systems, the ensemble can be parameterized using experimental steady state flux data determined for a certain strain. As discussed in Section 2.1.2, exchange fluxes can be easily determined from measured concentration time courses for metabolites absorbed or secreted by the cell. Using experimentally determined exchange fluxes to constrain the FBA formulation described by Equation 2.4, it is possible to generate a first estimate for the intracellular flux distribution. If more advanced equipment and expertise is available, labeling experiments along with the computational methods previously described can be applied to obtain more accurate estimates of the intracellular flux distribution. Since labeling data obtained using one single tracer - usually uniformly labeled ^{13}C ([U- ^{13}C]) glucose - does not suffice to precisely resolve all fluxes in the central metabolism, more advanced techniques, like parallel labeling experiments [75] can be applied. In any case, uncertainties related to the reference flux distribution can be addressed by constructing different ensembles of metabolic models, each using a representative reference flux distribution to populate the ensemble. In order to obtain ensembles with biological significance, a variety of objective functions may be applied (depending on culture conditions) to obtain reference flux distributions [128]. This approach is briefly illustrated in Section 9.3, where two similar objective functions are used to populate two different ensembles and generate predictions.

Once a biologically feasible ensemble has been constructed, mathematical methods can

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be applied to assess the effect of genetic perturbations on the cellular metabolism. At steady state, the concentration of intracellular metabolites does not change over time and we obtain:

$$\frac{dc}{dt} = \mathbf{S} \ r(c_{ss}, p) = F(c_{ss}, p) = 0, \qquad (2.23)$$

where c_{ss} refers to a vector of steady state metabolite concentrations. Equation 2.23 is analogous to Equations 2.2 and 2.3. The only difference is the definition of the function $F(c_{ss}, p)$. Since $F(c_{ss}, p) = 0$, it follows that the total derivative with respect to p is also zero:

$$\frac{dF}{dp} = \frac{\partial F}{\partial c_{ss}} \frac{dc_{ss}}{dp} + \frac{\partial F}{\partial p} = 0.$$
(2.24)

Solving Equation 2.24 for $\frac{dc_{ss}}{dp}$ yields:

$$\frac{dc_{ss}}{dp} = -\left(\frac{\partial F}{\partial c_{ss}}\right)^{-1} \frac{\partial F}{\partial p}.$$
(2.25)

Starting from a reference steady state, Equation 2.25 describes the effect of parameter perturbations (for instance enzyme concentration) on the vector of steady state metabolite concentrations c_{ss} . Since the calculation of the inverse of the matrix $\frac{\partial F}{\partial c_{ss}}$ is necessary to solve Equation 2.25, it is crucial to detect the point where this matrix becomes singular. Interestingly, this points is also a bifurcation point, beyond which the system no longer reaches a stable steady state [74].

So far, two methods have been developed that analyze different aspects of Equation 2.25. The first method is termed Ensemble Modeling for Robustness Analysis (EMRA) [74] and was designed to estimate the robustness of non-native pathways towards perturbations. By perturbing the activity of a certain enzyme in the pathway and calculating the percentage of models in the ensemble that remained stable, the robustness of the pathway/enzyme can be assessed. In the original publication [74], the robustness of two synthetic central metabolic pathways that achieve carbon conservation (non-oxidative glycolysis [17] and reverse glyoxylate cycle [90]) was compared. In a subsequent paper [144], experimental data of three different cell-free enzymatic systems were used to demonstrate the existing link between production performance (product end titer, productivity) and system robustness. As predicted by EMRA, unstable systems exhibited a lower production performance.

A second method, termed Kinetically Accessible Yield (KAY), uses the maximal flux value through a given pathway before the metabolic system loses stability (or any metabolite concentration becomes negative) to estimate experimentally measured product yields. In the original publication, Lafontaine Rivera et al. [71] used the KAY formulation to successfully predict the isobutanol yield of three different genotypes. Interestingly, the authors demonstrated that KAY can be calculated by either flux or kinetic parameter integration. In both cases, the calculated KAY value is the same [71]. Throughout this work, KAY values were calculated using flux integration. In this case, no specific knowledge of reaction kinetics of the production pathway is required. Instead, a single lumped reaction representing the whole production pathway is used as input.
Metabolic Reconstructions for the Ensemble Modeling Approach

One of the main advantages of the EM approach is that it allows for a kinetic-based analysis of available metabolic reconstructions (refer to Table 2.1). These reconstructions have been manually curated and are frequently updated, thus becoming more accurate and complete over the years. Instead of automatically generating the metabolic network from the EcoCyc [60,61] database, as done by Lafontaine Rivera et al. [71], we adapted already existing metabolic reconstructions to make them suitable inputs for the EM approach as follows:

- 1. Check exchange reactions. Exchange reactions are required to have positive flux values within the EM framework for both uptake and export reactions. By contrast, traditionally used metabolic reconstructions (refer to Table 2.1) exhibit negative flux values for uptake reactions and positive flux values for export reactions. Therefore, uptake reactions must be converted from the form "metabolite \rightarrow " into " \rightarrow metabolite". This can be simply done by multiplying the column *i* of the stoichiometric matrix **S** by -1. *i* refers to the reaction(s) responsible for the uptake of a given substrate(s).
- 2. Split reaction describing biomass production. Biomass formation is represented within the EM approach by a set of efflux reactions [71]. By contrast, cellular growth is mathematically described by one single reaction in traditionally used metabolic reconstructions. While a stoichiometric representation of a reaction involving over 100 substrates is straightforward, a kinetic representation of such a reaction would not be practical. For that reason, the metabolic reconstruction should be modified by splitting the biomass reaction into many reactions involving one single substrate. Alternative strategies, in which related substrates are grouped in a single reaction are also possible, for instance to represent DNA formation.

For all kinetic-based analyses, we used an extended version of the *E. coli* core metabolism [107]. Refer to Appendix B.1.1 for more details on model modification. Since the EM framework allows to incorporate known substrate-level regulation of enzyme activity, we used the regulatory interactions contained in Table 2.3 for the construction of rate laws for all ensembles. Additionally, we used the rate law described by Equation 2.26 to describe the flux through the phosphotransferase system (PTS) system, as suggested by Lafontaine Rivera et al. [71]. Note that the rate law described in the Equation 2.26 includes known regulatory interactions, such as flux control through the PEP/Pyruvate ratio [22, 33, 109] and product inhibition by glucose-6-phosphate [22, 29, 59].

$$r_{PTS} = \frac{V_{m,PTS \ C_{PEP}/C_{PYR} \ C_{GLC}}}{(k_{m,1} + k_{m,2} \ C_{PEP}/C_{PYR} + k_{m,3} \ C_{GLC} + C_{GLC} \ C_{PEP}/C_{PYR})(1 + C_{G6P}/k_{i,G6P})}.$$
 (2.26)

Parallelization Strategies in Large Multi-core Computers and Computer Clusters

EM-based analyses are computationally expensive. Luckily, the process of ensemble construction by parameter sampling and the analysis itself of each model within a given

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Table 2.3.: Substrate-level Enzyme Regulation Considered for the *E. coli* Core Model. Regulatory interactions were obtained from reference [71] and were used during the automatized rate law construction within the EM framework.

| Dethway | Enguno | Ponetion | Pogulatora |
|-------------------|--|----------------------|---------------------------|
| гашway | Antaldahada dahada annaa (antal tiri) | | |
| Pyruvate | Acetaidenyde denydrogenase (acetylating) | ACALD | AMP[I], NAD[2] |
| Metabolism | D-lactate dehydrogenase | LDH_D | ATP[I], PYR[4] |
| | Phosphotransacetylase | PTAr | ADP[I], ATP[I], NADH[I], |
| | | | NADPH[1], PEP[2], PYR[2] |
| Citric Acid | Citrate synthase | \mathbf{CS} | AKG[1], ACCOA[4], ATP[1], |
| Cycle | | | NADH[3] |
| Cycle | Fumarase | FUM | CIT[1] |
| | Isocitrate dehydrogenase (NADP) | ICDHyr | OAA[1], PEP[3] |
| | Fructose-bisphosphate aldolase | FBA | CIT[2], PEP[2] |
| | Fructose-bisphosphatase | FBP | ADP[1], AMP[1], PEP[1] |
| | Glyceraldehyde-3-phosphate dehydrogenase | GAPD | PEP[1] |
| Clycolycie / | Pyruvate dehydrogenase | PDH | NAD[1], NADH[1], PYR[1] |
| Chuconoogonosis | Phosphofructokinase | \mathbf{PFK} | ADP[4], ATP[3], FRDP[1], |
| Gluconeogenesis | | | F6P[4], PEP[3] |
| | Glucose-6-phosphate isomerase | PGI | PEP[1] |
| | Phosphoenolpyruvate synthase | PPS | AKG[1], ADP[1], AMP[1], |
| | | | OAA[1], PEP [1] |
| | Pyruvate kinase | PYK | AMP[4], ATP[1], F6P[4], |
| | | | SUCCOA[1] |
| | Hexokinase | HEX1 | PEP[1] |
| Pentose Phosphate | Glucose 6-phosphate dehydrogenase | G6PDH2r | NADH[1], NADPH[1] |
| Pathway | Ribose-5-phosphate isomerase | RPI | AMP[1] |
| Glutamate | Glutamine synthetase | GLNS | AMP[1] |
| Metabolism | Glutamate dehydrogenase (NADP) | GLUDy | GLN[1] |
| Apploratio | Isocitrate lyase | ICL | PEP[1], G3P[1] |
| reactions | Malic enzyme (NADP) | ME2 | ACCOA[3], ACTP[2], |
| reactions | | | FUM[1], G6P[2], NADH[3], |
| | | | NADP[1], OAA[3] |
| | Phosphoenolpyruvate carboxylase | PPC | ACCOA[4], FDP[4], MAL- |
| | | | L[3] |

Substrate-level enzyme regulation is coded as follows: [1]: competitive inhibition; [2]: non-competitive inhibition; [3]: allosteric inhibition; [4]: allosteric activation.

Substrate abbreviations as follows: AKG: 2-Oxoglutarate; PYR: Pyruvate; CIT: Citrate; OAA: Oxaloacetate; FRDP: D-Fructose 1,6-biphosphate; F6P: Fructose 6-phosphate; MAL-L: L-Malate; FUM: Fumarate; ACTP: Acetyl phosphate; G6P: Glucose 6-phosphate; G3P: Glyceraldehyde 3-phosphate; GLN: Glutamine; SUCCOA: Succinyl-CoA;

ensemble are highly parallelizable. This means that the computation time can be dramatically reduced through the implementation of either multi-core computers or computer clusters (See Figure 2.6). In this work, both parallelization strategies were applied to perform kinetic-based analysis. Therefore, we will briefly discuss both strategies using a Matlab implementation of the EM approach. In the case of large multi-core computers, parallelization can be achieved within the code, by simply replacing the *for*-command with a *par for*-command. By doing so, Matlab will automatically use all available cores to analyze the ensemble. When using computer clusters, a similar strategy can be applied. The only difference is that instead of running the EM code on a single computer, it is run on multiple multi-core nodes (see Figure 2.6). This is conveniently done by instructing Simple Linux Utility for Resource Management (SLURM) to run the EM code on k different nodes. Consequently, each node will independently sample and analyze n/k models. Here, n refer to the total number of models in the ensemble. There are two peculiarities of this approach that require special attention.



Figure 2.6.: **Parallelization Strategy in Linux Cluster. A.** Computational strategy for large multi-core computers. Parallelization is achieved easily by using the Matlab command *parfor* **B.** Computational strategy for computer clusters with multiple or single cores. Notice that the command *rng('shuffle')* is necessary to guarantee that each model has a unique set of kinetic parameters. Also, an additional step to merge individual results from each node into one single result might be necessary.

- 1. Control random number generation. Place the command rng('shuffle') before the ensemble is populated by randomly sampling the parameter space to ensure that each node is generating and analyzing unique models. Failure to do so will cause all nodes to sample exactly the same parameter values. As a consequence, the effective size of the ensemble will be reduced from n to n/k unique models.
- 2. Individual results need to be merged. When using the parallelization strategy shown in Figure 2.6 for computer clusters, an additional step is required to merge the results from k different nodes into one single result. Depending on the kind of analysis being performed, this step might require a large amount of Random Access Memory (RAM). Consider using the *hugemem* partition of the LRZ Linux Cluster, which offers up to 240 GBytes in a single shared memory node.

2.4. Strain Design Algorithms

One of the main goals of constructing mathematical models of cellular metabolism is the identification of non-intuitive genetic interventions aiming at the over-production of a target molecule. OptKnock [20] was one of the first algorithms developed to systematically identify gene knockout candidates for strain optimization. This strain design algorithm identifies growth-coupled, non-intuitive reaction deletions strategies by solving a bi-level optimization problem using the linear programming duality theory. Many strain design algorithms were developed based on the ideas introduced by OptKnock during the past decade. Table 2.4 presents an overview of some of those and other strain design algorithms. Interestingly, all these approaches used the overproduction of succinate as a case study. Since there is a large body of successful experimental optimization strategies to overproduce succinate in various strains, this knowledge has been repetitively used to test the predictions of newly introduced strain design algorithms. Table 2.4 was reproduced from [149]. For more information on additional strain design algorithms, refer to Machado et al. [87] or Maia et al. [89]

| Model type | Algorithm Name | Year | Organism | Description | Ref. |
|----------------------|-------------------|------|---------------|--|---------------|
| Kinetics- based | k-OptForce | 2014 | E. coli | k-OptForce integrates available kinetic informa- tion with stoichiometric metabolic models. It en- ables identification of both enzymatic parameter changes and reaction flux changes. Data for model parametrization can limit the prediction capabil- ities of the algorithm. | [28], [62] |
| | OptKnock | 2003 | E. coli | OptKnock identifies growth-coupled, non- intuitive gene deletion strategies for the over- production of target chemicals by solving a bi-level optimization problem using the linear programming duality theory. | [20] |
| Constraint- based | OptGene | 2005 | S. cerevisiae | OptGene is an evolutionary programming based algorithm that permits solving large gene knock- out problems in relatively short computational time. It allows the optimization of non-linear ob- jective functions, such as the productivity. | [108] |
| | GDLS | 2005 | E. coli | GDLS overcomes the computational burden of bi- level optimization problems, such as OptKnock, by employing an heuristic approach based on local search with multiple search paths. | [85] |

Table 2.4.: Theoretical Approaches Used in the *in silico* Strain Optimization for the Succinate Overproduction. A total of 26 theoretical studies were performed in the period of time from user 2002 to 2016

| Model type | Algorithm Name | Year | Organism | Description | Ref. |
|------------|-------------------|------|----------|---|-------|
| | MOFBA | 2009 | E. coli | MOFBA is a multiobjective flux balance analysis method. The non-inferior set estimation method is used to generate an approximation of the pareto curve for conflicting objectives. MOFBA re- duces the computation time required to obtain the pareto curve and its analysis. | [104] |
| | RobustKnock | 2010 | E. coli | RobustKnock accounts for the presence of com- peting pathways in the metabolic network. This method extends OptKnock to identify reactions that should be removed so that the production of the desired product becomes an obligatory byproduct of growth. | [143] |
| | OptForce | 2010 | E. coli | OptForce makes use of available flux measure- ments for the wild-type strain. The algorithm ultimately identifies sets of fluxes that must act- ively be forced through genetic manipulations in order to ensure the overproduction of the target molecule. | [112] |
| | SimOptStrain | 2011 | E. coli | SimOptStrain is a bi-level strain design approach that uses mixed-integer programming. The ap- proach simultaneously considers gene deletion and non-native reaction addition, which enabled the identification of novel strategies with higher pre- dicted production levels. | [64] |
| | EMILiO | 2011 | E. coli | EMILiO uses successive linear programming to in- crease the scope of strain design. The algorithm can quantitatively predict the optimal flux ranges that maximize production. EMILiO was used to generate over 200 strain designs for sucinate pro- duction. | [161] |
| | BAFBA | 2012 | E. coli | BAFBA is an hybrid approach of the Bees Al- gorithm and Flux Balance Analysis. The al- gorithm prevents falling into local minima while searching for optimal strain designs. | [25] |
| | GDMO | 2012 | E. coli | GDMO is a heuristic and combinatorial multi- objective optimization method that globally searches for genetic manipulations that optimize multiple cellular functions. The algorithm imple- ments a genetic algorithm to find pareto-optimal solutions. | [30] |
| | GDBB | 2012 | E. coli | GDBB is an approach developed to find near- optimal gene knockout strategies. It implements an adaptation of the branch and bound algorithm and can be applied to find near-optimal solutions in seconds to minutes instead of days or more. | [35] |
| | OptSwap | 2013 | E. coli | OptSwap is a computational method which identi- fies optimal modifications of the cofactor specifit- ies (NAD(H) and NADP(H)) of oxidoreductase enzymes and complementary reaction knockouts. | [65] |

Table 2.4 Continued from previous page

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| Model type | Algorithm Name | Year | Organism | Description | Ref. |
|------------|-------------------|------|---------------------------|---|-------|
| | ReacKnock | 2013 | E. coli | ReacKnock is a computational algorithm that uses the Karush-Kuhn-Tucker method to reformu- late a bilevel linear programming to a single level programming problem. The algorithm does not return a single solution but all alternative dele- tion strategies. | [159] |
| | MOMAKnock | 2013 | E. coli | MOMAKnock is a bi-level optimization frame- work that identifies knockout strategies under the MOMA flux distribution approximation, which considers that knockout mutants do not reach a steady state with maximum growth rates. | [115] |
| | DySScO | 2013 | E. coli | DySScO integrates dynamic flux balance analysis with existing strain design algorithms. This al- lows to consider process-level variables such as productivity and titer in the optimization process. | [170] |
| | FastPros | 2013 | E. coli | FastPros is an iterative screening algorithm that is based on shadow price analysis. It allows fast identification of strain designs with a large num- ber of reaction knockouts. | [105] |
| | DBFBA | 2014 | E. coli | DBFBA improves the performance of BAFBA by using a differential evolution algorithm. DBFBA has shorter computational time and identifies strain designs with higher production yields. DBFBA was validated with OptKnock. | [27] |
| | FSA | 2015 | E. coli | Flux-Sum Analysis (FSA) aims at identifying en- gineering targets from a metabolite-centric per- spective. The idea is to identify metabolites that will force the overproduction of a target molecule after attenuation or intensification of their corres- ponding turnover or "flux-sum". | [72] |
| | BHFBA | 2015 | E. coli | Bees Hill Flux Balance Analysis (BHFBA) is an hybrid of Hill climbing and the neighborhood searching strategy of BAFBA [25]. It integ- rates optKnock for automatic results validation. BHFBA maximizes the production yield of desired phenotypes while sustaining the growth rate. | [26] |
| | HyMeP | 2016 | Synechosystis sp. 6803 | Hybrid Metabolic Pathway Design (HyMeP) al- lows exogenous reactions to be considered in the optimization process. It selects individual can- didate reactions from the metabolic reactions in the Kyoto Encyclopedia of Genes and Genomes (KEGG) to construct a computerized metabolic model of a hybrid cell. | [137] |

Table 2.4 Continued from previous page

| Model type | Algorithm Name | Year | Organism | Description | Ref. |
|-------------------------------|-------------------|------|------------------------------|---|-------|
| | SolveME | 2016 | E. coli | A Metabolism and macromolecular Expression (ME) model describes not only the metabolic net- work but also the transcription and translation machinery associated with the genes considered in the model. ME models enable the computa- tion of proteome allocation at different conditions and predict the macromolecular composition of the cell. | [162] |
| Elementary Modes- based | CASOP | 2010 | E. coli | CASOP is based on reaction importance meas- ures derived from weighted elementary modes. The method allows the identification of knockout and overexpression candidates considering expli- citly the product yield and network capacity. | [51] |
| | CASOP GS | 2010 | E. coli | CASOP GS is an improvement of the CASOP method and allows it to be used in genome-scale networks. CASOP GS uses a sampling procedure of the elementary flux modes to estimate the CASOP-scores at the genome-scale. | [18] |
| | iStruF | 2013 | E. coli and S. cerevisiae | iStruF introduces the concept of structural fluxes as good predictors of <i>in vivo</i> flux measurements. The algorithm is able to find growth-coupled strain designs while considering optimal and sub- optimal routes and their efficiencies. | [138] |
| | SSDesign | 2014 | E. coli | The Solution Space Design (SSDesign) algorithm identifies growth-coupled and non-growth-coupled strain designs. SSDesign permits to visually set the desirable solution space in advance and iden- tifies the necessary knockouts. | [145] |

Table 2.4 Continued from previous page

For the sake of simplicity, we have categorized the algorithms presented in Table 2.4 into three main categories: kinetic-, constraint- and elementary modes-based methods. In reality, this distinction is not always practicable, since there are many algorithms combining different types of methods. For instance, thermodynamics-based methods can be embedded into constraint-based approaches to generate thermodynamically feasible flux distributions on a genome scale. This is done by considering an additional set of linear thermodynamic constraints [56]. More recently, a method called thermodynamic elementary flux modes analysis (tEFMA) was introduced to avoid the enumeration of thermodynamically infeasible elementary flux modes [46]. In this way, tEFMA strongly reduces memory usage and overall computational time of the enumeration process, while focusing on biologically relevant elementary flux modes.

The development of frameworks integrating constraint-, kinetic- and thermodynamic-based methods is becoming popular. For instance, the Ensemble Modeling (EM) approach

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[141,142,146], which introduced an elegant solution for difficulties related to unambiguous parameter estimation of large-scale kinetic models, has the potential to integrate constraintbased methods like FBA to identify biologically meaningful steady-state flux distributions, if no ¹³C-labeling data is available. Additionally, thermodynamic constraints can be applied not only to complement FBA calculations [56], but also to perform thermodynamically safe parameterization using independent parameter sets [77–79]. In this way, kinetic parameters will satisfy Haldane relationships and Wegscheider conditions, necessary to ensure thermodynamical consistency of the kinetic model [79]. In a more recent work, Sehr et al. [135] proposed a modeling workflow that integrates FBA with Thermodynamic Feasibility Analysis [94]. The results of both approaches are then translated to parameters for a dynamic model. The dynamic model is then formulated and analyzed according to Biochemical Systems Theory [118–120] and Mathematically Controlled Comparison [3, 121]. The authors used this approach to analyze three different case studies. We refer interested readers to the original publication for further details on mathematical implementation and results [135].

2.5. Computational Tools

As shown in Table 2.1, the size of the stoichiometric matrix **S** [metabolites x reactions] of commonly used metabolic reconstructions can rapidly increase as the metabolic reconstruction becomes more comprehensive. In order to effectively handle the size and complexity of genome-scale metabolic reconstructions, many computational approaches have been developed. Some prominent examples are listed in Table 2.5. Out of those methods, the COnstraint-Based Reconstruction and Analysis (COBRA) Toolbox has emerged as one of the preferred modeling tools. The COBRA toolbox consist of a compilation of various Matlab scripts designed to allow for a rapid implementation of basic and advanced analyses. The current functionality allows for network gap filling analysis, determination of intracellular flux distributions by analyzing ¹³C labeling data, implementation of strain design algorithms, omics-guided analysis, visualization of calculated flux distributions, among others.

Throughout this work, the functionality provided by the COBRA Toolbox v2.0 [124] was extensively implemented. For instance, FVA was used in Chapter 4 to identify changes in by-product secretion pattern as the substrate uptake rate was increased. In the same chapter, relative quality for various substrates was quantitatively assessed by calculating the maximal flux through the ATPM reaction of the *E. coli* core model [107]. In Chapter 5, the OptKnock implementation provided by the COBRA toolbox was used to analyze the effect of oxygen availability on genetic targets improving taxadiene production. In order to demonstrate the simplicity of application of the COBRA toolbox, we show how the maximal theoretical taxadiene yield on glucose can be calculated using some basic commands. The code shown encompasses the following steps:

- 1. Load a metabolic reconstruction. In this case, we use the *E. coli* core model. See code line 2.
- 2. Expand the scope of the metabolic reconstruction by adding a set of new reactions. In this case, 12 new reactions along with their corresponding substrates and products are added to the model. See code lines 6 to 46.

Table 2.5.: Commonly Used Computational Tools for the Analysis of Metabolic Networks. Due to the implementation of a large number of different constraint-based analysis, the COBRA toolbox has been widely used within the metabolic modeling community.

| | v | 0 | | | | |
|------------------------|--|-----------|--|--|--|--|
| Toolbox | Description | Reference | | | | |
| COBRA for Matlab | Matlab package for implementing COBRA | [55, 124] | | | | |
| | (constraint-based reconstruction and analysis) | | | | | |
| | methods to simulate, analyze and predict a variety of | | | | | |
| | metabolic phenotypes using genome-scale models. | | | | | |
| COBRA for Python | Python package that provides support for basic CO- | [34] | | | | |
| - | BRA methods. COBRApy includes parallel processing | | | | | |
| | support for computationally intensive processes. | | | | | |
| CellNetAnalyzer | Matlab toolbox that provides a graphical user interface | [67] | | | | |
| U U | and various computational methods and algorithms for | LJ | | | | |
| | exploring structural and functional properties of meta- | | | | | |
| | bolic, signaling and regulatory networks. | | | | | |
| SNA: Stoichiometric | | 5 | | | | |
| Network Analysis | Interactive, high-performance toolbox for analyzing | [148] | | | | |
| 1.000.0111 11101.9.010 | steady-state behavior of metabolic networks. The tool- | | | | | |
| | box is mainly implemented in Mathematica. | | | | | |
| YANA | Platform-independent, dedicated toolbox for meta- | [131] | | | | |
| | bolic networks with graphical user interface to calcu- | | | | | |
| | late, edit, visualize, centralize and compare elementary | | | | | |
| | flux modes. | | | | | |

- 3. Set an objective function. Since we are interested in calculating the maximal taxadiene yield, the taxadiene export reaction is set as objective function. See code line 49.
- 4. Constrain exchange reactions to reflect medium composition or experimentally determined rates. In this case, we set the glucose uptake rate to a value of 1 mmol/gDW h and allow the network an unlimited oxygen availability. See code line 52 and 53.
- 5. Calculate flux distribution optimizing the objective function set in step 3. Since we constrained the glucose uptake rate to a value of 1 mmol/gDW h, the maximal value of the objective function would correspond to the maximal theoretical taxadiene yield on glucose. See code line 57.

```
% Load E.coli core metabolic reconstruction
 2
3
   model=readCbModel('ecoli_core_model.xml');
   % Add Non-Mevalonate Pathway:
 4
 5
6
   % Reaction
                1.
                     dxs
   % Reaction 1. - dxs
model=addReaction(model,'dxs','pyr[c] + g3p[c] + h[c] -> dxyl5p[c] + co2[c]');
 8 % Reaction 2. ispC
9 model=addReaction(model,'ispC','dxyl5p[c] + nadph[c] + h[c] \rightarrow nadp[c] + 2me4p[c]');
   % Reaction 3. ispD
   model=addReaction(model, 'ispD', ' 2me4p[c] + atp[c] + h[c] -> 4c2me[c] + 2 pi[c] '); %Eigentlich
ist die Reaktion mit CTP.
12
13
14
15
   % Reaction 4. ispE
   model=addReaction(model, `ispE`, `4c2me[c] + atp[c] -> 2p4c2me[c] + adp[c] + h[c] `);
16
17 % Reaction 5. ispF
18 model=addReaction(model, 'ispF', ' 2p4c2me[c] -> 2mecdp[c] + amp[c] ');
19
20 % Reaction 6. ispG
   model=addReaction(model, `ispG', `2mecdp[c] + nadh[c] -> h2mb4p[c] + h2o[c] + nad[c] `);
21
23 % Reaction 7. ispH
```

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```
24 model=addReaction(model, 'ispH', ' h2mb4p[c] + nadh[c] + h[c] -> dmpp[c] + h2o[c] + nad[c] ');
26 % Reaction 8. ispH2
27 \mod each (c) + h(c) - i pdp[c] + h2o[c] + nadh[c] + h[c] -> i pdp[c] + h2o[c] + nad[c] ');
29 % Reaction 9. idi
30
   model=addReaction(model, 'idi ', ' dmpp[c] <=> ipdp[c] ');
32 % Add Taxadiene Synthesis:
   %Reaction 10. - Geranyl diphosphate formation.
model=addReaction(model, 'DMATT', ' dmpp[c] + ipdp[c] -> grdp[c] + 2 pi[c] ');
33
34
   %Reaction 9. - Farnesyl diphosphate formation
model=addReaction(model,'GRTT',' grdp[c] + ipdp[c] -> frdp[c] + 2 pi[c] ');
36
37
38
   %Reaction 10. - GGPP formation
40
41
   model=addReaction(model, 'ggpps', 'frdp[c] + ipdp[c] -> ggpp[c] + 2 pi[c]');
41
42 %Reaction 11. - Taxadiene formation
43 model=addReaction(model,'txs','ggpp[c] -> txdn[c] + 2 pi[c]');
44
   %Reaction 12. - Taxadiene export
model=addReaction(model,'txdnx','txdn[c] -> '); %txdn[e]
45
46
48 % Set Taxadiene export as objective function.
49 model=changeObjective(model, 'txdnx');
50
   % Set availability of glucose and oxygen.
   model=changeRxnBounds(model, 'EX_glc(e)', -1, 'l');
model=changeRxnBounds(model, 'EX_o2(e)', -100, 'l');
52
53
54
   \% Solve the linear problem. Flux through taxadiene export reaction \% corresponds to molar yield on glucose. s=optimizeCbModel(model);
56
```

Although the COBRA toolbox offers an implementation for dFBA simulations, this code is not suitable for large-scale calculations due to its limited speed. Many computational tools have been introduced to perform dFBA analysis [47,92,124,169]. Among those, we used the Matlab-based DFBALAB [47] code to perform all dFBA simulations presented in Chapter 8 due to its velocity and simplicity of use. Similarly, even though COBRA also offers an implementation for ¹³C-MFA, it requires the use of the commercial nonlinear solver TOMLAB/SNOPT. For that reason, we implemented the 13CFlux2 software instead [155], which uses the large-scale nonlinear open source solver Interior Point OPTimizer (IPOPT) [153]. Refer to Appendix A.2.4 for an exemplary model used for ¹³C-MFA calculations using the 13CFlux2 software. As for all EM analyses implemented in this work, the Matlab code provided in the reference [71] was used.

3. Theoretical Workflow for Metabolic Engineering

One of the main objectives of this work was the development a theoretical workflow for Metabolic Engineering. Here, we propose such a workflow, incorporating state of the art constraint- and kinetic-based modeling approaches along with the concept of metabolic burden. Our workflow consist of two main steps. The first one covers model-guided development of production strains, while the second step targets model-driven process optimization, as shown in Figure 3.1. Even though the proposed workflow exhibits a sequential nature, with strain engineering preceding process development, other scenarios are also conceivable. For instance, process parameters, e.g., medium composition, production temperature, aeration levels, etc., could be previously fixed so that strain optimization should be performed to reach high strain performance under such conditions. The workflow was designed to reflect current trends of rational strain engineering and systems biotechnology [73, 117], characterized by cyclic steps of modeling (dry-lab) and experimental work (wet-lab). In line with the main structure of the workflow, this thesis consist of two results parts, one for strain engineering - Part II - and one for process optimization - Part III -, each being comprised of three chapters. Note that the application of the methods described in each chapter is not limited by its assignment to one of the two main topics, meaning that some model predictions can be applied to guide both strain and process optimization.

3.1. Model-guided Strain Engineering

The workflow starts with the selection of a metabolic reconstruction for the organism of interest. In the case of *E. coli*, different models of diverse scope and complexity are available. Some of the most commonly used are listed in Table 2.1. Once a metabolic reconstruction has been chosen, adapted or constructed, an initial in silico strain characterization can is performed. By calculating theoretical maximum product yield on single carbon sources or substrate mixtures, optimal medium composition for the synthesis of the desired product can be identified. Analogously, constraint-based approaches can also be applied to aid pathway selection, when more than one metabolic routes are available for the desired bio-transformation. The results of this initial in silico characterization can be applied to inform following steps: decide whether the selected host strain meets minimum requirements on product yield to allow for an economically viable process; guide the selection of initial process parameters for process optimization and, define experimental conditions in early steps of strain characterization. Refer to Chapter 7 for more details on the specific application of these methods to the taxadiene overproduction in E. coli. The results of an initial experimental strain characterization are then used to construct a strain-specific metabolic model. This is done by updating model boundaries of exchange reactions corresponding to substrate uptake, by-products secretion and if available, product

3. Theoretical Workflow for Metabolic Engineering

formation. Stoichiometric coefficients of the reaction describing biomass synthesis can also be updated if protein, DNA, RNA or lipids content measurements are available. Calculations regarding *in silico* medium optimization can be repeated and, if necessary, actual medium composition should be adjusted. Additionally, constraint- and kinetic-based strain design algorithms can be implemented to guide genetic interventions aiming at the overproduction of the molecule of interest. Refer to Chapters 5 and 6 for more details on the specific application of these methods to the taxadiene overproduction in E. coli. The next step is experimental strain construction and characterization. Here, genetic interventions suggested by strain design algorithms are experimentally implemented and the resulting strain is characterized to assess its production performance. If the mutant strain meets performance requirements, it is categorized as optimal production strain and the process of strain engineering can be concluded. In the case that strain production performance is not satisfactory, predictive power of the algorithms and methods used for strain design needs to be reviewed. This can be done by thoroughly comparing model predictions with actual strain behavior. The idea is to identify and correct potential model flaws causing discrepancies between in silico and in vivo behavior. Once model and methods have been reviewed, new predictions are generated. The process of hypothesis generation and experimental validation is repeated until generated mutant strains meet minimal production performance and an optimal production strain is generated.

3.2. Model-guided Process Optimization

In the first step of the model-driven process optimization workflow, the production performance of a given production strain is experimentally assessed in a fermentation system for the first time, using a non-optimal initial set of process parameters (e.g., medium composition, production temperature, time point of system induction, growth rate/dilution rate, etc.). The choice of concrete process parameter values can be guided by theoretical tools described in this work. More specifically, the cellular growth rate during the production phase can be selected to consider theoretical aspects related to minimization of metabolic burden (refer to Chapter 4) and/or optimal biomass yield resulting in a maximal product yield (refer to **Chapter 9**). Empirical models can also be applied for process optimization, as demonstrated in Chapter 8. In this case, a simple model, based on the dynamic flux balance framework, allowed the identification of optimal production temperature and time point of induction, which in silico increased the maximal taxadiene productivity by 25%. Additionally, theoretical studies regarding optimal carbon source can be used to guide the process of medium composition optimization, as described in Chapter 7. If observed strain performance does not fulfill minimal production requirements, an iterative process, similar to the one applied for strain optimization, can be applied, in which metabolic models are updated so that their predictions match experimental data. Strain performance is then characterized using an improved set of process parameters and the optimization cycle is repeated until strain performance meets minimum production requirements.



Figure 3.1.: Workflow for Model-based Metabolic Engineering. The proposed workflow covers both model-guided strain engineering and modeldriven process optimization. Cutting edge constraint- and kinetic-based modeling approaches are implemented in each stage. The workflow was designed to reflect current trends of rational strain engineering and systems biotechnology, characterized by cyclic steps of modeling (dry-lab) and experimental work (wet-lab).

Part II. Results: Strain Engineering



The second part of this thesis is composed of three chapters, which cover topics related to model-driven strain optimization. Chapter 4 analyzes the effect of plasmid-based foreign gene expression on strain performance. It is known that loaded cells, i.e., supporting heterologous gene expression, exhibit a decreased growth rate and biomass yield. This phenomenon is commonly termed Metabolic or Protein Burden. We start by describing the concept of acetate and biomass yield lines and by showing how it can be used to monitor the effect of the load on cellular metabolism. Subsequently, we extend this concept and apply it to develop strategies to overcome the metabolic burden caused by heterologous gene overexpression. In Chapter 5, we analyze ¹³C labeling data for different taxadiene production strains and use them to generate reference flux distributions for each strain, which are subsequently used as input to a kinetic-based approach we termed optEM. OptEM allowed the identification of genetic targets for strain engineering. Finally, in Chapter 6 we analyze simultaneous utilization of glucose and xylose by E. coli. To this end, six different strains exhibiting two different genetic backgrounds were experimentally characterized. All strains were subsequently assessed regarding production potential, metabolic burden and sugar co-uptake level by applying constraint- and kinetic-based approaches.

In order to analyze the detrimental effect that gene over-expression has on strain performance, our cooperation partner Sabine Wagner at Fachgebiet Systembiotechnologie (SBT) designed, constructed and experimentally characterized three strains, each of which exhibited a different protein load, as shown in Figure 4.1. Strain cultivation was conducted in shaking flasks. Five different carbon sources were used to obtain a relatively wide range of growth rates, ranging from approximately $0.2 \ 1/h$ for acetate, to almost $0.5 \ 1/h$ for glucose. We used a constraint-based approach to qualitatively reproduce observed acetate secretion patterns in the three strains. As previously described [11], acetate lines can be used as an indicator of cellular fitness. We found a connection between biomass yield lines and acetate lines. The point where the slope of the biomass yield line is decreased for the first time defines a threshold beyond which cellular growth is always accompanied by acetate secretion under aerobic conditions. By analyzing acetate secretion patterns of strains exhibiting different burden levels, we hypothesize that cells growing below a certain threshold can fulfill the imposed burden, while simultaneously growing with wild-type yields. Our *in silico* analysis also suggests that acetate lines do not have a unique slope as initially suggested, but are rather composed of at least two straight lines with different slopes.

4.1. Strains & Experimental Data

Main genetic features of the strains analyzed in this chapter are shown in Figure 4.1. The strains were designed by Sabine Wagner to exhibit an increasing protein burden. The fluorescent protein mCherry was used as a monitor of the cellular capacity, by placing the transcription of the mCherry gene under the control of a constitutive promotor. On the other hand, the protein eGFP was used to load the cell. Since both mCherry and eGFP are fluorescent proteins, their synthesis can be easily determined by measuring light emission at different wavelengths.

Five different carbon sources - glucose, mannose, fructose, galactose and acetate - were used to allow for the analysis of the metabolic burden (caused by plasmid-based heterologous gene expression) at different growth rates. Experimental strain characterization was conducted in shaking flask at 37°C and 200 revolutions per minute (rpm). Additional to light emission at mCherry- and eGFP-specific wavelengths, time courses for OD, substrate and acetate concentration were experimentally determined (see Appendix A.1.3 for raw data). Calculated rates for glucose as carbon source are exemplarily provided in Table 4.1. Refer to Appendix A.1.3, Table A.6 for a complete overview of the results.

In order to analyze the effect of gene over-expression on growth rate and biomass yield, we plot growth rates versus substrate uptake rates for all strains and substrates (Figure

| Strain ID | 31 | 3150 | 3152 |
|-----------------|-----------|-------------------------|-------------------------|
| Plasmid Content | 1 | 2 | 2 |
| | 6 | 60 | QQ |
| Antibiotics | Kanamycin | Kanamycin Gentamycin | Kanamycin Gentamycin |
| Inducer | 1 mM 3-MB | 1 mM 3-MB | 1 mM 3-MB |
| Protein Load | | | |

Figure 4.1.: Main Genotypic Characteristics of Strains Used for the Characterization of the Metabolic Burden. Plasmid present in strain 31 correspond to a medium copy number plasmid. Additional plasmid in strain 3150 is a high copy number plasmid. Amino acid sequences of proteins encoded in each plasmid are given in Appendix A.1.2. 3-methylbenzoate (3-MB) was used to induce eGFP expression in strain 3152. In order to guarantee identical medium composition for all strains, the culture medium was always supplemented with 1 mM 3-MB

 Table 4.1.: Experimentally Calculated Exchange Rates for Three Strains.

 Growth on Glucose.
 Rates for growth, substrate uptake and acetate secretion were calculated from measured time courses as described in Chapter 2.1.2.

| | | Strain | |
|-------------------------------------|--------|--------|-------|
| | 31 | 3150 | 3152 |
| $\mu, [1/\mathrm{h}]$ | 0.487 | 0.111 | 0.086 |
| $r_{uptake}, [\text{mmol/gDW h}]$ | 14.111 | 4.449 | 4.540 |
| $r_{acetate}, [\text{mmol/gDW h}]$ | 6.074 | 4.707 | 3.336 |

4.2). For a fixed uptake rate of a given substrate, for instance galactose (symbol * in Figure 4.2), we observe a reduction of growth rate as the protein load is increased, as denoted by the grey arrow. One can explain this observation from a stoichiometric point of view. Heterologous protein production directly competes with cellular growth by reducing the amount of effective substrate available for biomass production. Thus, a reduction of the growth rate will be expected, if heterologous protein production increases at a given constant substrate uptake rate. Of course, mass balance is not the only explanation for the observed behavior. Heterologous protein production can also reduce cellular growth rate by reducing the effective amount of ribosomes available for production of host protein. Additionally and depending on the amino acid composition and identity of the foreign protein, cellular metabolism can be directly affected. For instance, the intracellular pool of a given amino acid can be dramatically reduced or toxic pathway intermediates can accumulate as a consequence of the enzymatic activity of the heterologous protein. In both cases, one would observe a reduction in the cellular growth rate.

Considering the results for strain 31, Figure 4.2 evidences an unexpected, inverse relationship between growth rate and substrate uptake rate: as the value of substrate uptake rate increases, the growth rate seems to decrease. Taking a closer look at Figure 4.2, one can conclude that this behavior mainly arises due to the data point for acetate (symbol +). This observation suggests that in order to properly analyze the correlation between substrate uptake rate, we need to standardize the substrate uptake rate,



Figure 4.2.: Growth Rate vs. Substrate Uptake Rate for Three Strains and Five Substrates. Black symbols correspond to strain 31, green symbols to strain 3150 and blue symbols to strain 3152. Substrate symbols are as follows: +: acetate, ◦: fructose, *: galactose, □: glucose, ◊: mannose.

to consider differences in the molecular weight and quality of the various substrates used.

4.2. Substrate Quality

A real-life analogy for the concept of substrate quality is presented to justify its introduction and to understand its utility. Let us imagine for a moment we are interested in analyzing the correlation between the Gross Domestic Product (GDP) of a given group of countries and the life expectancy of their citizens. One option to graphically analyze this relationship would be to plot the two variables for all countries and determine the slope of the resulting line. Figure 4.3.A shows this relationship for six different countries. Data were collected from the webpage of the World Bank for the year 2016.

Based on Figure 4.3.A, one would conclude that living in rich countries, where the GDP per capita is high, reduces life expectancy. From the figure, we also observe that Colombia appears to be the richest country. Since we know this is not the case, we conclude we first need to standardize the data, more specifically the currency of the GDP per capita, before we can perform any kind of analysis. Figure 4.3.B shows the data after converting the GDP per capita from each local currency to US dollars. After data standardization, we obtain the expected relationship between GDP and life expectancy: the richer the country, the higher the life expectancy. This real-life analogy points out the necessity of adequate conversion factors for each member of the data set. In this case, exchange rates allowed a correct data analysis by adjusting the value of the GDP per capita so that it became comparable within the group. Note that the conversion to another currency different from US\$ is also possible.



Figure 4.3.: Real-Life Analogy for Concept of Substrate Quality. A. Life expectancy vs. GDP in local currency. An inverse, unexpected relationship between these variables is observed. B. Life expectancy vs. GDP in US\$. As expected, there exist a direct relationship between the two variables

4.2.1. Conversion Factors for Substrate Uptake Standardization

After taking a closer look at the data for strain 31 (Figure 4.2, black symbols), we hypothesize that expressing the substrate uptake rate of each substrate in units of "mmol/gDW h" does not allow a correct data analysis. This is because energy and mass content (or number of carbon atoms) per millimol (mmol) differ for each substrate, especially when acetate is compared with the other substrates. Inspired by this observation, we define three different criteria to describe substrate quality: mass content, carbon content and energy content. In a following step, we set up a theoretical framework to assess the utility of each criterion. In this section, we refer to substrate quality as the potential of a given substrate to allow growth.

Determination of Energy Content Using Linear Programming

Conversion factors for the first two quality criteria (molecular weight and carbon content) are solely defined by the chemical identity of each substrate, i.e., they do not depend on culture conditions, for instance, oxygen availability. On the other hand, energy content is a function of both chemical identity of the substrate and oxygen availability. We make use of constraint-based modeling to calculate the energy content of each substrate for various oxygen availability levels by simply maximizing the flux through the ATPM reaction of the iJO1366 model [106]. This reaction describes the dephosphorylation of ATP: ATP + H₂O \longrightarrow ADP + Pi + H⁺. Calculations were performed using the COBRA toolbox and gurobi 5 as the linear solver. Refer to section 2.5 for an overview of the main commands. A constant uptake rate of 1 mmol/gDW h was set for each substrate, while the oxygen uptake rate was varied to obtain oxygen ratios ranging from zero to 20. Throughout this work, we will use the term *ATP content* to refer to the ratio between the flux through the ATPM reaction and the substrate uptake rate. Strictly speaking, this ratio rather refers to the number of high-energy phosphoanhydride bonds that can be



- Figure 4.4.: Energy Content As a Function of Oxygen Availability for Five Substrates. The *E. coli* metabolic reconstruction iJO1366 was used for all calculations. Energy content is represented by the potential of each substrate to generate energy in form of ATP. Note that anaerobic energy production from acetate is not possible.
- Table 4.2.: Conversion Factors for Three Quality Criteria. Conversion factors for energy content as quality criteria correspond to maximal ATP content for each substrate, as shown in Figure 4.4. Factors for carbon content correspond to the number of carbon atoms in each molecule and factors for mass content correspond to molecular weight of each substrate in units of g/mmol

| | Energy Content | Carbon Content | Mass Content |
|-----------|---------------------------|-------------------------|--------------------|
| | [mmol ATP/mmol Substrate] | [C-mmol/mmol Substrate] | [g/mmol Substrate] |
| Acetate | 6.25 | 2 | 0.06005 |
| Fructose | 23.5 | 6 | 0.18016 |
| Galactose | 23.25 | 6 | 0.18016 |
| Glucose | 23.5 | 6 | 0.18016 |
| Mannose | 23.5 | 6 | 0.18016 |

be generated from the given substrate [80]. However, since these phosphate bounds are contained in form of ATP, the term *ATP content* is equally precise.

Figure 4.4 shows the energy content of all five carbon sources. As expected, the ATP content strongly depends on the identity of the substrate and oxygen availability. For all substrates, the ATP content exhibits a saturation behavior as a function of the oxygen ratio. Fructose, galactose, glucose and mannose all reach the same ATP content at an oxygen ratio of 10 mmol O_2 / mmol substrate, while acetate reaches its maximal ATP content at a oxygen ratio of 2 mmol O_2 /mmol substrate. Assuming that the cell strives to maximize the amount of produced energy by aerobically metabolizing the absorbed substrate, the maximal ATP content should serve as a proper conversion factor when considering energy content as quality criterion. The validity of this assumption will be discussed in section 4.2.2. Table 4.2 contains all conversion factors for the previously defined quality criteria.

Note that for the three quality criteria considered, the conversion factor for acetate is always the lowest out of the five substrates tested. This suggests that the cell should absorb a comparatively higher amount of acetate (measured in mmol/gDW h) in order to

support a given growth rate. Considering energy as quality criterion, the cell will have to absorb acetate with a rate 3.76 times higher than the corresponding rate for glucose. This trend is visible for the strain 31 in Figure 4.2, with acetate exhibiting the highest uptake rate. However, this trend is not as clear in strains 3150 and 3152. Having defined three different quality criteria, the natural question following is: which of these criteria is the most suitable to perform standardization of the substrate uptake rate?

Assessing the Suitability of Different Quality Criteria

To answer this question, we designed a constraint-based algorithm to assess the suitability of the different quality criteria. The rationale is the following: if uptake rates of a given set of substrates can be correctly standardized by a potential quality criterion, then a given standardized value of substrate uptake rate should lead to a single growth rate, no matter the nature of the substrate. In other words, we require the biomass yield, calculated as the ratio between growth rate and *standardized* substrate uptake rate, to have the same numerical value for all substrates. The proposed algorithm consist of the following steps:

- 1. Select a quality criterion and determine its corresponding conversion factors. Refer to Table 4.2.
- 2. Define a numerical value for the standardized uptake rate. For instance, 117.5 mmol ATP/ gDW h.
- 3. Using corresponding conversion factors, convert the *standardized* uptake rate, into an uptake rate having units of "mmol substrate/gDW h". In this case, 117.5 mmol ATP/gDW h correspond to: 18.8 mmol acetate/gDW h; 5.05 mmol galactose/gDW h and 5 mmol/gDW h for all other substrates.
- 4. Set upper and lower boundaries for the uptake reaction of a defined substrate in a given stoichiometric model, for instance iJO1366, and calculate the maximal growth rate supported by this substrate using linear programming.
- 5. Repeat step 4. for all other substrates to generate a growth vector containing growth rates for all substrates.
- 6. Calculate the maximal error in the growth vector as $\frac{max(growthvector) min(growthvector)}{min(growthvector)}$
- 7. Repeat step 1. to 6. for each quality criterion and select the one with the lowest error.

After applying these steps, we obtain the results shown in Figure 4.5. Additionally to the previously mentioned quality criteria, this figure also contains the assessment of a negative control (Figure 4.5.A), where no standardization is used. From Figure 4.5 it results clear that energy content (expressed as ATP) represents the best quality criterion for uptake rate standardization, exhibiting an error of only 1.78%. The performance of mass and carbon content as quality criteria is identical under the tested conditions. An unlimited oxygen supply, id est (i.e.), completely aerobic metabolism, was used to calculate all growth rates shown in Figure 4.5. If the oxygen availability is reduced (from 20 mmol O2/ gDW h to 5 mmol O2/ gDW h), different results are obtained, as shown in Figure 4.6. While the error of the negative control is reduced to 189%, the error of the three quality criteria becomes identical and increases to 185%.



- Figure 4.5.: Assessment of Three Different Quality Criteria for Data Standardization. High Oxygen Availability. A maximal oxygen uptake rate of 20 mmol O₂/gDW h was used for all calculations. Uptake rates used to estimate growth rates via linear programming can be extracted from Table 4.3. All calculations were performed using the *E. coli* metabolic reconstruction iJO1366. At a relatively high oxygen to substrate ratio, standardization using energy content as quality criterion seems to be the most accurate approach for standardizing the substrate uptake rate. A. Negative control. All substrates had a substrate uptake rate of 5 mmol/gDW h. B. Standardization using carbon content as quality criterion C. Standardization using mass content as quality criterion D. Standardization using energy content as quality criterion.
- Table 4.3.: Substrate Uptake Rates Used to Assess Quality Criteria. Substrate uptake rates were calculated using conversion factors listed in Table 4.2 and assuming following input fluxes: Negative control: 5 mmol/gDW h for all substrates; Carbon content: 30 Cmmol/gDW h; Mass content: 0.9008 g/ gDW h; Energy content: 117.5 mmol ATP/gDW h. These reference fluxes were selected so that after conversion into molar flux, 5 mmol glucose/ gDW are obtained. All uptake rates are given in units of mmol substrate/ gDW h.

| | Negative | Carbon | Mass | Energy |
|-----------|----------|---------|----------|---------|
| | Control | Content | Content | Content |
| Acetate | 5 | 15 | 15.00030 | 18.8 |
| Fructose | 5 | 5 | 5 | 5 |
| Galactose | 5 | 5 | 5 | 5.0538 |
| Glucose | 5 | 5 | 5 | 5 |
| Mannose | 5 | 5 | 5 | 5 |



Figure 4.6.: Assessment of Three Different Quality Criteria for Data Standardization at Low Oxygen Availability. A maximal oxygen uptake rate of 5 mmol O₂/gDW h was used for all calculations. Uptake rates used to estimate growth rates via linear programming can be extracted from Table 4.3. All calculations were performed using the *E. coli* metabolic reconstruction iJO1366. At a relatively low oxygen to substrate ratio, none of the three standardization approaches tested seems to reduce the error, when compared to the error of the negative control. A. Negative control. All substrates had a substrate uptake rate of 5 mmol/gDW h. B. Standardization using carbon content as quality criterion C. Standardization using mass content as quality criterion D. Standardization using energy content as quality criterion.



Figure 4.7.: Standardized versus Raw Experimental Data. Black symbols correspond to strain 31, green symbols to strain 3150 and blue symbols to strain 3152. Substrate symbols are as follows: +: acetate, o: fructose, *: galactose, □: glucose, o: mannose. A. Raw experimental data B. Substrate uptake rate was standardized using mass content as quality criterion C. Substrate uptake rate was standardized using energy content (ATP) as quality criterion. Note that the relative position of the acetate data point is the only appreciable difference between standardization using mass (B.) or energy content (C.)

4.2.2. Data Standardization

As previously shown, oxygen availability, commonly expressed as oxygen to substrate ratio, has a big impact on numerical values of conversion factors, when energy content is used as quality criterion (refer to Figure 4.4). As it turned out, oxygen availability also impacts the performance of a given set of conversion factors, no matter which quality criteria was used (refer to Figure 4.5 and Figure 4.6). In order to understand the nature and implication of these observations, consider one more time the real life-analogy presented at the beginning of section 4.2. The relative value of a given currency to another, that is, its exchange rate, is normally determined by market forces of supply and demand, which in turn depend on plenty of factors. In an ever-changing world, exchange rates are constantly changing to represent the relative value of a given currency accurately. Trying to predict their exact behavior has proven to be a challenging, if not impossible endeavor. Contextualizing these observations, we infer that in the case of energy as quality criterion, conversion factors need to be adjusted in order to reflect the effect of variable factors like for instance, oxygen availability. However, oxygen availability is normally unknown, especially when culturing in shaking flasks. Additionally, it has been shown that factors like medium composition, specific growth rate or heterologous protein over-expression also have a profound effect on the overall cellular fitness, consequently affecting the amount of oxygen that the cell can absorb and effectively use to fully metabolize the absorbed substrate (refer to [11] and [110], Figure 6 therein). In other words, the calculation of conversion factors should not only be process-specific, but also strain-specific. Due to the impossibility of an accurate determination of conversion factors using energy content as quality criterion, we opt for choosing mass content as quality criterion.

Figure 4.7 (B and C) shows the effect that standardizing substrate uptake rate has on data interpretation. By changing the units in which substrate uptake rate is plotted, the correlation between growth rate and substrate uptake rate went from being negative to become positive. Note that although the numerical value for the uptake rate is changed for all substrates as a consequence of standardization, the data point for acetate underwent

the biggest change in its relative position. Acetate, exhibiting the highest uptake rate *before* standardization, became the substrate with the second lowest uptake rate *after* standardization. This behavior is valid for strain 31, however, strains 3150 and 3152 show a similar pattern.

4.3. Yield, Acetate and Formate Lines

From previous constraint-based analysis, in which the dependence of growth rates on glucose uptake rates at varying oxygen levels was investigated, we learned that at a constant oxygen availability, an increase in the glucose uptake rate is always followed by an increase in growth rate. Similarly, at a constant glucose uptake rate, a decrease in the oxygen ratio is accompanied with a reduction in the growth rate, as shown in Figure 4.8.B and .D. We refer to the lines shown in both figures as yield lines, since their slopes correspond to the biomass yield. A comparison between *experimentally* obtained yield lines for strains 31, 3150 and 3152 (Figure 4.8.A and .C) with *in silico* generated ones - using glucose as carbon source at different oxygen levels - evidences an intriguing similarity (compare Figure 4.8.A with .B and Figure 4.8.C with .D). Thus, we venture to hypothesize that heterologous protein over-expression in strains 3150 and 3152 might originate a load-induced oxygen limitation, which is experimentally evidenced as a downward displacement of the biomass yield lines.

One of the advantages of metabolic modeling is that it allows the analysis of complex responses of the cellular metabolism to changes in culture conditions. We used FVA in combination with a core metabolic model [107], describing the central metabolism of $E.\ coli$, to investigate the reason for the systematic reduction of biomass yield at higher substrate uptake rates observed in Figure 4.8.B and .D. For our analysis, we focused on one specific *in silico* yield line, shown in Figure 4.9. This yield line is divided into three phases, with each phase exhibiting decreasing slopes (biomass yield) as the substrate uptake rate increases. The analysis was performed as follows:

- 1. Select a combination of growth and substrate uptake rate lying in one of the three phases.
- 2. Fix the flux through those reactions in the model by adjusting lower and upper boundaries correspondingly.
- 3. For each reaction in the model, calculate the maximal and minimal flux supported, while fulfilling constraints set in the previous step.
- 4. Repeat step 1 to step 3 for the other two phases.
- 5. Compare flux distribution ranges for all three phases, paying special attention to by-product secretion patterns.

This analysis identified clear differences in the by-product secretion patterns of the three phases. While CO_2 is the sole by-product secreted in the first phase, its secretion is complemented by acetate in the second phase and by acetate and formate in the third phase (refer to Appendix A.1.4, Figures A.2 to A.4, for a detailed overview of results). The changing by-product secretion pattern can be understood as a consequence of decreasing



Figure 4.8.: Load-induced Oxygen Limitation. A. and C. correspond to standardized experimental data using mass and energy content as quality criteria, respectively. B. and D. correspond to *in silico* simulations using glucose as carbon source and the *E. coli* core model. Growth rates were calculated using constraint-based modeling with maximization of growth rate as the objective function for glucose uptake rates ranging from 0 to 14 mmol/gDW and three different oxygen levels. Black symbols correspond to strain 31, green symbols to strain 3150 and blue symbols to strain 3152. Substrate symbols are as follows: +: acetate, \circ : fructose, *: galactose, \Box : glucose, \diamond : mannose.



| Phase | Side-products |
|-------|-------------------------------------|
| I | CO ₂ |
| II | CO ₂ + Acetate |
| Ш | CO ₂ + Acetate + Formate |
| | |

Figure 4.9.: Relationship between Biomass Yield, Acetate and Formate Lines. In silico yield line for glucose as carbon source is shown. Maximal oxygen uptake rate was set to 7 mmol/gDW h. Yield line is divided into three phases, denoted by I, II and III. Each phase is characterized by a single biomass yield and by-product secretion pattern, as shown in the adjacent table.

oxygen to substrate ratios. This is because the substrate uptake rate increases from phase I to phase III, while the maximal oxygen uptake rate, allowed to the cell to use, is kept constant. Since the substrate uptake rate in phase I is comparatively low, the cell has enough oxygen to allow for a complete oxidation of the substrate to CO_2 via tricarboxylic acid (TCA) cycle and electron transport chain. As the substrate uptake rate keeps increasing, while the capacity of the electron transport chain is kept constant (since O_2 availability is kept constant), the cell cannot completely redirect the formed pyruvate to the TCA cycle and part of the pyruvate is fermented to form acetate in the second phase and acetate and formate in the third phase. Thus, we extend our analysis to the *in silico* acetate and formate secretion patterns.

Figure 4.10 directly compares in silico calculations with experimental data. Upper row correspond to in silico predictions, while lower row corresponds to experimental data. In silico calculations were performed using the *E. coli* core metabolic reconstruction along with the COBRA toolbox. Glucose uptake rate was varied from 0 to 14 mmol/gDW h, while just two oxygen levels were considered: 4 and 7 mmol/gDW h, corresponding to the black and green line of the upper row of Figure 4.10, respectively. Growth rate was used as the objective function and was maximized using linear programming. For a given pair of substrate uptake rate ($r_{substrate}$) and growth rate (μ), FVA analysis was used to estimate acetate secretion ($r_{acetate}$) by minimizing and maximizing flux through the acetate export reaction in the *E. coli* core model, while keeping $r_{substrate}$ and μ fixed. Formate secretion was estimated in a similar way, by maximizing and minimizing the flux through the formate export reaction, while keeping $r_{substrate}$, μ and minimal $r_{acetate}$ constant.

As previously inferred, transitions between different phases of the yield lines are accompanied by changes in the by-product secretion pattern. Consider for instance the black *in silico* yield line of Figure 4.10. As the growth rate increases, cellular metabolism undergoes a transition, from phase I to phase II. This is accompanied by a reduction in the biomass yield and acetate secretion for the first time (4.10.B, point ①). The growth rate in



Figure 4.10.: Qualitative Comparison Between Experimental Data and in silico Calculations. A. to C. represent in silico calculations. Upper boundary for oxygen uptake rate was constrained to 7 mmol/gDW h for the black lines and to 4 mmol/gDW h for the green lines. ① and ② corresponds to transitions from phase I to II and from phase II to III, respectively (see Figure 4.9). Thin lines correspond to maximal acetate secretion rates, while thick lines correspond to minimal acetate secretion rates. D. to F. represent experimental data. In line with a previous publication [11], we refer to the lines shown in B. and E. as acetate lines. Analogously, we introduce the concept of formate line to refer to the line shown in F. Legend: black symbols correspond to strain 31, green symbols to strain 3150 and blue symbols to strain 3152. Substrate symbols are as follow: +: acetate, o: fructose, *: galactose, □: glucose, o: mannose.

which this transition occurs is termed critical growth rate for acetate, $\mu_{acetate}$, and corresponds in this case to 0.19 1/h. As the growth rate continues to increase, acetate secretion keeps linearly increasing. At a certain point (2), cellular metabolism undergoes a second transition, accompanied again, by a reduction in the biomass yield and a change in the by-product secretion pattern. In this case, formate is secreted for the first time (4.10.C, (2)). Analogously, we refer to the growth rate in which the second transition occurs as the critical growth rate for formate, $\mu_{formate}$, which in this case corresponds to 0.28 1/h. Interestingly, the transition from phase II to phase III is not only characterized by a reduction in the biomass yield, but also by differing minimal and maximal acetate secretion values, as shown in Figure 4.10.C by the thin line. A similar behavior during phase transitions is observed for the green *in silico* yield line.

Initially, similarities between *experimental* and *in silico* yield lines at different oxygen levels led to the hypothesis formulation of load-induced oxygen limitation (Figure 4.8) and motivated the previous analysis of secretion patterns in silico. Figure 4.10.E und .F shows experimental acetate and formate secretion for all strains as a function of growth rate. A comparison between experimental and *in silico* secretion patterns reveals further. interesting resemblances. First, we observe a parallel, downwards displacement of the acetate line for strains 3150 and 3152, when compared to the parent strain 31 (Figure 4.10.E). Remarkably, the same behavior can be obtained in silico by reducing the maximal oxygen uptake rate, as shown in Figure 4.10.B for low acetate secretion rates. Second, the existence of formate lines is predicted by our *in silico* analysis, as shown in Figure 4.10.C. Experimentally, this can be qualitatively confirmed for strain 31, as shown in Figure 4.10.F. Missing formate lines for strains 3150 and 3152 could be explained by low growth rates exhibited by these strains. As a consequence, experimentally observed metabolic states might be limited to phase I and II. Since actual values for oxygen uptake rate and level for each of the three strains are unknown, mentioned similarities have only a qualitative nature. However, we believe that the proposed hypothesis of load-induced oxygen limitation is supported by our experimental observations and partly by experimental evidence presented by Peebo et al. [110], as discussed in Section 4.5.

4.4. Process-level Strategy to Reduce Detrimental Effects of Metabolic Burden

One of the objectives motivating the analysis of the metabolic burden generated by heterologous protein over-expression in *E. coli* was the development of strategies to reduce its negative effect on biomass yield and acetate secretion. Here, we propose a process-level strategy designed to recover the wild-type biomass yield by adjusting the growth rate during heterologous protein production. By using different substrates, it was possible to study gene over-expression at various growth rates in shaking flasks. Assuming that standardization of substrate uptake via molecular weight is reasonably accurate, it is possible to draw straight lines representing experimental yield and acetate lines for all strains as, shown in Figure 4.11.

Our *in silico* analysis suggests that yield lines of a given reference strain and a loaded strain should converge into one single yield line at a sufficiently low growth rate (see 4.10.A). In our specific case, yield lines of the two loaded strains (3150 and 3152) seem to converge with



Figure 4.11.: Process-level Strategy to Reduce Metabolic Burden. A. Experimental yield lines. B. Experimental acetate lines. Dashed lines were obtained using linear regression. Black symbols correspond to strain 31, green symbols to strain 3150 and blue symbols to strain 3152. The metabolic burden (Δ), defined as a reduction in $\mu_{Acetate}$, is a function of the load exerted on the strain. We predict that by modulating the load in strain 3152, burden-free eGFP expression (blue region) can occur at higher growth rates, when compared to current load level. Substrate symbols are as follows: +: acetate, \circ : fructose, *: galactose, \Box : glucose, \diamond : mannose. Critical growth rates for acetate secretion are: $\mu_{Acetate}^{31} = 0.33$, $\mu_{Acetate}^{3150} = 0.03$, $\mu_{Acetate}^{3152} = 0.022$ 1/h.

the reference strain (31) at the same point into one single yield line, as shown in Figure 4.11.A. The growth rate at which yield lines converge can also be obtained from Figure 4.11.B and corresponds to $\mu_{Acetate}$ of loaded strains. In theory, $\mu_{Acetate}$ for a given strain defines the transition from phase I to phase II, as discussed in section 4.3. Experimentally determined $\mu_{Acetate}$ for strains 3150 and 3152 (y-intercept of acetate lines shown in Figure 4.11.B) are in accordance with their respective transition phases, obtained from Figure 4.11.A. This observation provides further support for our load-induced oxygen limitation hypothesis. Additionally, in silico predictions generated by this analysis can be used to guide the design of a fed-batch process by providing a threshold for cellular growth rate that should not be exceeded during the production phase, once the plasmid-based system has been induced. In this way, cells producing heterologous proteins will not secrete acetate and their biomass yield will be consequentially identical to that of the wild-type or the reference strain. The range of growth rates allowing protein over-expression with no burden is highlighted in blue in Figure 4.11.A. For the concrete case of the eGFP over-production in strain 3152, a critical growth rate for acetate of 0.022 1/h might cause this burden-free zone be too small to be technically and economically feasible. A potential solution to this problem would be to modulate the load imposed by the eGFP expression by using low-copy plasmids [58] and by tuning the strength of promoter and ribosome biding site. As a result, $\mu_{Acetate}^{3152}$ should increase, allowing a burden-free eGFP expression at much higher growth rates than the current system.

4.5. Discussion

The concept of acetate lines and its relationship with metabolic burden is not entirely new. Basan et al. [11] experimentally showed that increasing LacZ overexpression levels caused parallel shifts of the acetate line, thus leading to a reduction of corresponding values of $\mu_{Acetate}$ in E. coli strains. The authors explained this behavior using a proteomic resource allocation model. The model assumes a limited proteomic capacity, which the authors divided into three fractions. The first fraction is dedicated to biomass synthesis and linearly depends on the growth rate, while the other two fractions are used for energy biosynthesis via respiration and fermentation, respectively. The authors rationalized, under the assumption of growth rate maximization, that at high carbon uptake rates, it is more advantageous for the cell to generate energy by the more proteome-efficient fermentation pathway. In this way, a higher fraction of the proteome can be used to support growth. By contrast, at low carbon uptake rates, the cell should use the more carbon-efficient respiration pathway, so that more carbon flux can be used for biomass synthesis. Since heterologous protein over-expression reduces the effective proteome fractions available for biomass synthesis and energy production, loaded cells should exhibit higher acetate secretion rates at fixed growth rates, which was indeed experimentally observed by the authors (refer to Figure 3.A in reference [11]). Here, we used a constraint-based approach to qualitatively account for the same phenomenon of overflow metabolism. Our modelling strategy is similar to the approach used by Varma et. al [151] to understand glucose catabolism in E. coli under various oxygenation rates. By constraining the upper boundary for oxygen uptake rate to a given value, independently of the numerical value of the substrate uptake rate, our constraint-based approach reproduces experimental observations of acetate secretion at high substrate uptake rates. The observed increase in acetate secretion, exhibited by protein-overproducing strains, is reproduced in our model by reducing the numerical value of the oxygen uptake rate constraint, as shown in Figure 4.12. In this figure, orange lines represent the growth behavior of a wild-type strain, while all other lines qualitatively represent strains exhibiting an increasing metabolic burden.

Note that constraining the upper boundary for oxygen uptake directly limits the maximal flux through the respiratory chain, as represented by a saturation-like behavior of the cytochrome bd oxidase activity (Figure 4.12.C). Interestingly, a similar saturation behavior has been experimentally observed for the enzyme ATP synthase, when its expression cost is plotted as a function of the growth rate (refer to Figure 6.A in reference [110]). The same study reported acetate secretion when the ATP synthase reached its maximal expression cost. Both observations provide experimental evidence supporting the key assumption of our constraint-based approach, i.e., that a constraint in the maximal flux through the respiratory chain, implemented in our model by constraining the maximal oxygen uptake rate and experimentally observed by Peebo et al. [110] as a limited ATP synthase expression, gives rise to acetate lines. The work by Peebo also provides indirect experimental evidence to our load-induced oxygen limitation hypothesis. The authors reported that cells grown in amino acids (AA) supplemented medium can support higher ATP synthase expression costs, compared to cells grown in medium without amino acids supplementation. Consequently, $\mu_{Acetate}$ in the AA supplemented medium increases from 0.35 (no AA supplementation) to $0.55 \, 1/h$ (refer to Figure 1.A in reference [110]) Applying the proteomic resource allocation theory, used by Basan et al. [11] to explain overflow metabolism in E. coli, one can rationalize that a higher ATP synthese expression is possible

4.5. Discussion



Figure 4.12.: Emergence of Yield and Acetate Lines By Constraining Flux Through Respiratory Chain. The effect of constraining the upper boundary for oxygen uptake rate on biomass yield (A.); acetate lines -thin and thick lines correspond to maximal and minimal acetate secretion, respectively- $(\mathbf{B}.)$ and the flux through respiratory chain (\mathbf{C} .) is shown. Simulations were performed using the *E. coli* core model and a varying upper boundary for the oxygen uptake rate, as follows: green lines: 4 mmol/gDW h; black lines: 7 mmol/gDW h; blue lines: 14 mmol/gDW h; orange lines: 20 mmol/gDW h. CYTBD refers to the enzyme cytochrome bd oxidase, which produces a proton motive force in the *E. coli* core model by reducing oxygen to water as follows: $2 h[c] + \frac{1}{2} o_2[c] + q_8 h_2[c] \longrightarrow 2 h[e] + h_2 o[c] + q_8[c]$. $q_8 h_2$ and q_8 represent reduced and oxidized ubiquinone pools, respectively. Note that constraining the upper boundary of the oxygen uptake reaction directly limits the maximal flux through the enzyme CYTBD. Interestingly, the growth rate at which the maximal CYTBD activity is reached correspond to the transition from phase I to phase II. This point is exemplarily marked for the blue lines (1). Since the maximal respiration capacity is exhausted, the cell starts using fermentation pathways to generate energy. As a consequence, acetate is secreted and the biomass yield is reduced.

because amino acid supplementation increases proteomic resources by reducing the fraction of the proteome that is dedicated to amino acid biosynthesis. Conversely, heterologous protein overexpression would decrease proteomic resources available for biomass synthesis and energy generation, thus leading to a relative decrease in the maximal ATP synthase expression capacity and a consequent reduction in the flux through the respiratory chain.

Note that our simple constraint-based approach provides a flux-based explanation of the overflow metabolism in *E. coli* and allows for the generation of multiple testable hypothesis:

- 1. Acetate lines are not always composed of a single straight line. Basan et al. [11] reported that plotting growth rates against acetate secretion rates leads to a straight line, which the authors termed acetate line. Here, we showed that this is only the case, if acetate is the only fermentation product, i.e., cellular metabolism is confined to phase II (refer to Figure 4.9 and 4.10). Experimental evidence reported by Peebo et al. [110] (refer to Figure 1.A therein) supports this hypothesis.
- 2. Protein over-expression originates a load-induced oxygen limitation, as discussed in Section 4.3.
- 3. There exist a relationship between biomass yield, acetate and formate lines, as discussed in Section 4.3 and evidenced in Figure 4.10.A to .C.
- 4. Burden-free protein over-expression should possible for growth rates lower than $\mu_{Acetate}$. Consequently, a process-level strategy, as discussed in Section 4.11, can be developed to minimize or eliminate the metabolic burden, expressed as a decrease in biomass yield along with an increase in acetate secretion rate.

Further experimental studies can be designed to test the above mentioned hypothesis. Since oxygen uptake rate plays a central role in both defining the cellular metabolic state (phase I, II or III) and estimating conversion factors used to standardize substrate uptake rates of different carbon sources when energy content is used a quality criterion, its experimental determination should be prioritized. Similarly, experimental determination of protein content in loaded strains should be also considered in order to accurately describe the effect of protein over-expression on oxygen uptake capacity and proteome allocation. Finally, it is recommended that modeling efforts are only conducted on high-quality, reproducible data. Only under this circumstances the design-build-test-learn cycle can be optimally executed.
5. Strain Design Algorithms for Target Identification

The EM approach developed by the James Liao group at the UC, Los Angeles was used as framework to develop a strain design algorithm that we refer to as optEM. This algorithm uses EM to build an ensemble of kinetic models that fulfill a given reference flux distribution. optEM facilitates the maximization of complex user-tailored objective functions, for instance the weighted sum of volumetric productivity (mmol/l h), product yield (mmol/mmol) and production rate (mmol/gDW h). The kinetic nature of the optEM algorithm allows for consideration of typically inaccessible design parameters such as enzyme over-expression level, overall system stability and metabolite concentration pattern after enzyme perturbation. Using the optEM approach, we identified many genetic targets that were already reported in the literature to have beneficial effects on taxadiene yield, thus confirming the prediction power of our approach. We also identified targets not reported in the literature yet [37].

5.1. Strains & Experimental Data

Five production strains were constructed and experimentally characterized by our cooperation partner Monica Fuchs at IBK. Table 5.1 describes main genetic features of each of the strains, which are schematically represented in Figure 5.1 for a better overview. All strains are provided with a genetic makeup necessary to synthesize taxadiene. In strains $\Delta xylE$ 1p and $\Delta ptsG$ 1p, genes contained in plasmid pET28a DS (*ispF*, *ispD*, *idi* and dxs) were genomically integrated in the xylE and ptsG position, respectively. In contrast, all enzymes required for the taxadiene biosynthesis are encoded in two plasmids in strains $\Delta xylE$ 2p and $\Delta ptsG$ 2p. Refer to Table 5.1 for plasmid description. Gene integration aimed at the reduction of the metabolic burden caused by heterologous enzyme expression. Strain cultivation was performed in shaking flask (220 rpm) at 37°C using Riesenberg medium with a mixture of ${}^{12}C$ (4.5 g/l) and ${}^{13}C$ (0.5 g/l) glucose as carbon source. Experimental strain characterization was performed in duplicate and consisted of measurement of concentration time courses for biomass, glucose and acetate. These data were processed as described in Chapter 2.1.2 in order to calculate growth, substrate uptake and acetate secretion rates, respectively. Exchange rates and their standard deviations are reported in Table 5.2. Growth rates exhibit lower variability compared to acetate secretion rates (see Figure 5.2). This is because growth rates were calculated based on OD time courses, whose measurements require a less extent of experimental handling compared to the determination of glucose or acetate concentration time courses via HPLC measurements. Taxadiene could not be detected in the culture medium for any strain, due to low production rates exhibited by all strains combined with low sample volumes. Additional to concentration time courses, ¹³C-labeling data were also available for all strains. These measurements

Table 5.1.: **Taxadiene Producing Strains.** Five different strains were constructed and experimentally characterized in biological duplicates. All strains derive from *E. coli* HMS174(DE3). Refer to table notes for a detailed plasmid description. Strains were grown in minimal medium containing 0.5 g/l [U-¹³C] glucose and 4.5 g/l ¹²C glucose. Refer to Figures A.5 and A.7 in the Appendix for an overview of the non-mevalonate & the taxadiene production pathway, respectively.

| Strain ID | Genotype | Description |
|------------------|--|---|
| HMS_2p | $\mathrm{HMS174(DE3)}$ + $\mathrm{pET28a}_{\mathrm{DS}}$ + | HMS174(DE3) strain transformed with |
| | pACY_MEP | two plasmids. |
| $\Delta xylE_2p$ | $\mathrm{HMS174(DE3)}\ \Delta xylE\ +\ \mathrm{pET28a}\mathrm{DS}$ | Gene $xylE$ is knocked out from strain |
| | $+ {\rm pACY} _{\rm MEP}$ | HMS_2p |
| $\Delta xylE_1p$ | $ m HMS174(DE3) \; \Delta xylE + pET28a_DS$ | Heterologous genes encoded in plas- |
| | | mid pACY_MEP are genomically in- |
| | | tegrated in the $xylE$ position the con- |
| | | trol of a Trc promoter. |
| $\Delta ptsG_2p$ | $\mathrm{HMS174(DE3)}\ \Delta ptsG\ +\ \mathrm{pET28a}DS$ | Gene $ptsG$ is knocked out from strain |
| | $+ {\rm pACY} _{\rm MEP}$ | HMS_2p. |
| $\Delta ptsG_1p$ | $\mathrm{HMS174(DE3)}\;\Delta ptsG+\mathrm{pET28a_DS}$ | Heterologous genes encoded in plas- |
| | | mid pACY_MEP are genomically in- |
| | | tegrated in the $ptsG$ position under the |
| | | control of a Trc promoter. |

pET28a_DS is a high copy number plasmid that contains genes encoding following enzymes: kanamycin resistance, taxadiene synthase (txs) and geranylgeranyl diphosphate synthase (crtE). Expression of all genes is under the control of a T7 promoter.

pACY_MEP is a low copy plasmid that contains genes encoding a chlorampenicol resistance and selected enzymes of the non-mevalonate pathway: 2-C-methyl-D-erythritol 2,4cyclodiphosphate synthase (ispF), 4-diphosphocytidyl-2C-methyl-D-erythritol synthase (ispD), isopentenyl-diphosphate isomerase (idi) and 1-deoxy-D-xylulose-5-phosphate synthase (dxs). Gene expression is under the control of a T7 promoter.

were conducted by our cooperation partner Claudia Huber at **Bio**. Refer to Appendix A.2.3 for raw data.

5.2. Reduction of Metabolic Burden Through Genomic Integration

As mentioned before, the main objective of genomic integration conducted in strains $\Delta ptsG_1p$ and $\Delta xylE_1p$ was a reduction of the detrimental effect that plasmid-based heterologous gene expression exerts on the host metabolism, experimentally evidenced as a reduction in growth rate and yield. The success of this strategy can be assessed using the previously introduced concept of acetate lines (refer to Chapter 4). An acetate line emerges when plotting growth rates against corresponding acetate secretion rates for a given strain. By comparing the relative position of acetate lines between strains, one can assess the effect that a certain perturbation (in genotype or culture conditions) has on cellular fitness. A relative upwards displacement of the acetate line indicates that the given perturbation increases cellular fitness, thus leading to a higher $\mu_{Acetate}$. Since each of the strains listed in Table 5.1 was experimentally characterized for one single growth rate, additional information is needed to plot corresponding acetate lines. An interesting feature



Figure 5.1.: Taxadiene Producing Strains. Each of the five taxadiene producing strains described in Table 5.1 is schematically represented in this figure as follows: A. HMS_2p; B. $\Delta xylE_2p$; C. $\Delta xylE_1p$; D. $\Delta ptsG_2p$; E. $\Delta ptsG_1p$. Note that strains represented in Figures C. and E. contain one single plasmid. In both cases, genes encoded in the plasmid pACY_MEP were genetically integrated under the control of a Trc promoter in the *xylE* and *dptsG* positions, respectively. The effect that the genomic integration of one plasmid has on the metabolic burden can be nicely observed in Figure 5.2.

Table 5.2.: Taxadiene Producing Strains: Exchange Rates. Growth, substrate uptake and acetate secretion rates were calculated from concentration time courses as described in Section 2.1.2. Reported rates correspond to the average of two biological replicates. Errors correspond to one standard deviation.

| Strain | Growth Rate | Glucose | Uptake | Acetate | Secretion |
|------------------|---------------------------------|-------------------|------------------|-----------------|---------------------|
| | | \mathbf{Rate} | | Rate | |
| HMS_2p | $0.128 \pm 2.20 \times 10^{-3}$ | 4.532 ± 4.242 | 2 | $3.013 \pm 6.$ | 51×10^{-1} |
| $\Delta xylE_2p$ | $0.131 \pm 4.20 \times 10^{-3}$ | 3.923 ± 5.27 | $\times 10^{-1}$ | 1.197 ± 1.5 | 99×10^{-1} |
| $\Delta xylE_1p$ | $0.185 \pm 5.90 	imes 10^{-3}$ | 8.527 ± 3.12 | $	imes 10^{-1}$ | $1.024 \pm 4.$ | 60×10^{-2} |
| $\Delta ptsG_2p$ | $0.076 \pm 2.76 \times 10^{-2}$ | 5.686 ± 1.412 | 2 | 1.659 ± 4.5 | 45×10^{-1} |
| $\Delta ptsG_1p$ | $0.189\pm1.00\times10^{-4}$ | 7.166 ± 5.49 | $	imes 10^{-1}$ | $0.387 \pm 1.$ | $03 	imes 10^{-1}$ |

Growth rates are reported in 1/h; glucose and acetate rates are given in mmol/gDW h.

5. Strain Design Algorithms for Target Identification



Figure 5.2.: Acetate Lines for Taxadiene Producing Strains. Straight dotted lines correspond to acetate lines for each strain. Each line was defined by experimental information contained in Table 5.2 and by a constant slope, obtained as described in Appendix A.1.1. The effect of genetic perturbations (genomic integration, gene knock-outs) on strain fitness can be characterized comparing the relative possition of corresponding acetate lines. For instance, orange arrows represent the positive effect that genomic integration of plasmid-encoded genes has on cellular metabolism for both Δ ptsG and Δ xylE strain families. In this specific case, the extent of burden reduction seems to be a function of the genetic background.

of acetate lines is that under certain conditions, their slope remains constant. We make use of this property to generate acetate lines for all strains, as shown in Figure 5.2. Note that although all five strains contain the necessary genetic makeup to produce taxadiene, the form in which this genetic information is introduced into the cell, i.e., plasmid-encoded or genomically integrated, has an effect on the relative position of each acetate line, and thus, on the relative metabolic burden. For instance, genomic integration of genes encoded in plasmid pACY_MEP seems to relieve the metabolic burden by an extent that depends on the host genetic background, as highlighted in Figure 5.2 by the two orange arrows. The effect of gene knock-outs on metabolic burden can also be studied by comparing the relative position of acetate lines for strains HMS_2p, $\Delta xylE_2p$ and $\Delta ptsG_2p$, as shown in Figure 5.2. While knocking out gene xylE in strain HMS_2p leads to a reduction of metabolic burden, the effect of ptsG knockout is not completely clear due to large standard deviations.

5.3. Constraint-based Assessment of Taxadiene Production Potential

The main objective of constructing strains listed in Table 5.1 was to generate a pool of production strain candidates. Experimental data generated during strain characterization, including ¹³C-labeling data and concentration time courses for biomass, glucose and acetate should now be used to identify strains exhibiting a superior production performance for further engineering rounds. Since taxadiene concentration could not be experimentally measured due to its presumably low concentration in the medium and to low sample volume, our initial modeling efforts were focused on the estimation of production capabilities of each strain. We start our analysis by calculating flux ranges for each reaction in the *E. coli* central metabolism best matching experimentally measured amino acids labeling patterns. For that, we used the software 13CFLUX2 [155] along with a modified version of the *E. coli* metabolic model iRL2013 [75]. Refer to Section 2.1.2 for details on the metabolic model and mathematical implementation. The procedure can be summarized as follows:

for each strain in Table 5.1:

- 1. Generate input file for the software 13CFLUX2 containing experimentally determined exchange rates, as summarized in Table 5.2 and labeling data (refer to Table A.8 in the Appendix). An exemplary input file can be found in Appendix A.2.4.
- 2. Calculate intracellular flux distribution that minimizes squared sum of residuals for labeling data.
- 3. Apply statistical workflow described in Section 2.1.2 in order to calculate flux ranges for free reactions.
- 4. Calculate flux ranges for each reaction in the metabolic network using flux variability analysis (FVA) considering experimentally determined exchange rates and flux ranges for free reactions calculated in the previous step.
- 5. Calculate maximal theoretical taxadiene yield as the ratio between taxadiene production rate and glucose uptake rate.

Calculated maximal theoretical taxadiene yields using the previously described steps are plotted in Figure 5.3 for all strains. At this point, it is important to state that product yields shown in Figure 5.3 are not experimental values, but rather a theoretical estimation representing the *potential* of each strain to produce taxadiene with a certain product yield. One can clearly observe that a reduction in the metabolic burden in strains $\Delta xylE_1P$ and $\Delta ptsG_1P$, achieved by genomic integration of genes encoded in plasmid pACY_MEP, leads to a marked increase in the taxadiene production potential.

5.4. Application of Strain-design Algorithms for Target Identification

One valuable application of metabolic modeling is the possibility to *in silico* analyze the effect of a large number of perturbations on cellular metabolism in a fast, efficient and

5. Strain Design Algorithms for Target Identification



Figure 5.3.: Constraint-based Assessment of Production Capabilities. FVA was applied on a extended version of the iRL2013 [75] to estimate the taxadiene production potential of each strain. Shown are maximal theoretical yields, obtained by dividing maximal theoretical flux through the taxadiene pathway by the glucose uptake rate. Refer to Table A.9 in Appendix A.2.5 for an overview of minimal and mean production rates and yields.

cost-effective fashion. Such perturbations can be exerted at the process level (refer to Part III of this work), by modifying medium composition, production temperature, time point of culture induction, dilution rate, etc., or at the genetic level, by modulating the expression of various genes. Product yield, titer and productivity are process parameters commonly chosen for optimization during *in silico* studies. By using *in silico* generated model-based predictions to guide the development of *experimental* strategies for strain and process optimization, time and costs invested in experimental efforts can be greatly minimized.

There are various mathematical approaches used to describe bacterial metabolism, some of which were already presented in Section 2. Here, we apply both a traditionally used constraint-based strain-design algorithm called optKnock [20] and a novel kinetic-based algorithm, we termed OptEM, to identify genetic modifications aiming at the overproduction of taxadiene in $E. \ coli$.

5.4.1. Constraint-based Methods: The OptKnock Algorithm

OptKnock [20] was the first constraint-based strain-design algorithm that used growthcoupling as design principle to systematically identify reaction deletions leading to the overproduction of a target molecule. The basic idea behind growth-coupling is to delete a defined set of reactions, so that the synthesis of a given target molecule become obligatory for the cell to be able to grow, as exemplarily shown in Figure 5.4.B. By deleting three reactions (genes), the cell is forced to change its metabolism to produce taxadiene in order to be able to grow. This is denoted by the arrow in Figure 5.4.B.

As recently reported by Kamp and Klamt [152], growth-coupling strategies can be identified for almost all metabolites in genome-scale metabolic models of five major production



Figure 5.4.: Application of OptKnock to the Production of Taxadiene in *E. coli*: Basic Idea. A. Maximal theoretical taxadiene yield is calculated and plotted as a function of growth rate. A modified version of the *E. coli* core metabolic model was used for all calculations (refer to Appendix B.1.1). Glucose and oxygen uptake rate were kept at a constant value of 10 mmol/gDW h for all simulations. OptKnock was applied to identify reaction deletion targets shown in **B.** After deleting selected reactions from the network, the cell is forced to produce taxadiene along with biomass in order to maximize its growth rate. Points 1 and 2 correspond to predicted cellular behaviors maximizing growth in the wild-type (WT) and mutant, respectively. Genes *ppc*, *pgi* and *pykAF* encode for the enzymes phosphoenolpyruvate carboxylase, glucose-6-phosphate isomerase and pyruvate kinase, respectively.

organisms: E. coli, S. cerevisiae, Corynebacterium glutamicum, Aspergillus niger and Synechocystis sp. PCC 6803, which demonstrates the wide applicability of growth-coupling as design principle. In its original publication, optKnock was applied to identify different E. coli genotypes exhibiting an increased succinate production in silico.

Here, we apply OptKnock to identify triple reaction deletion designs leading to growthcoupled taxadiene overproduction. In a first step, an *E. coli* core metabolism model was slightly modified to allow for taxadiene synthesis, as explained in Appendix B.1.1. Then, deletion strategies were identified for various growth rates, ranging from 0 to 0.2 1/h, in accordance with experimental data provided by Monika Fuchs (refer to Table 5.2). Similarly, the upper bound for glucose uptake rate was updated to 10 mmmol/gDW h. Since the oxygen uptake rate was not provided, two different rates were assumed in order to consider both oxygen-rich and -poor conditions. All calculations were performed using the Optknock script provided with COBRA-Toolbox [124]. Figure 5.5 shows the dependence of OptKnock predictions on cellular growth rate and oxygen conditions.

While the set of reactions identified by OptKnock seems to remain constant over the range of growth rates tested when oxygen-rich conditions are assumed (Figure 5.5.A), the picture looks different when oxygen-poor conditions are assumed, as shown in Figure 5.5.B. In this case, cellular growth rate seems to affect OptKnock predictions. Figure 5.6 summarizes deletion targets for each condition. A stronger effect of growth rate at poor oxygen conditions on the identity of the deletion targets is evidenced by the larger number of different reactions presented in Figure 5.6.B. Although these results are not unexpected, they suggest that neither growth rate nor oxygen supply alone suffice as scale-up criterion to guarantee good large-scale performance of a production strain developed in the laboratory



Figure 5.5.: Application of OptKnock to the Production of Taxadiene in *E. coli*: Dependence on Growth Rate and Oxygen Availability. Deletion candidates identified by OptKnock are shown in blue. A. Oxygen-rich conditions. Oxygen upper boundary was set to 10 mmol/gDW h for all calculations. For a growth rate of 0.1 1/h, the deletion targets identified by OptKnock correspond to pyruvate kinase (PYK), phosphoenolpyruvate carboxylase (PPC) and glucose-6-phosphate isomerase (PGI) B. Oxygen-poor conditions. Oxygen upper boundary was set to 1 mmol/gDW h. For a growth rate of 0.1 1/h, the deletion targets identified by OptKnock correspond to transketolase (TKT2), phosphoenolpyruvate carboxylase (PPC) and pyruvate formate lyase (PFL)

at a shaking flask scale. This point will be further analyzed in the discussion section.

Although predictions made by OptKnock have successfully guided a couple of experimental metabolic engineering efforts [42, 164], none of the best production strains was constructed by the sole deletion of genes corresponding to reaction targets identified by OptKnock. Complementary strategies, like adaptive evolution [42] or codon optimization along with optimization of gene expression balance [164], were necessary to achieve the highest production performance. In a recent review [149], our group identified a similar trend for the overproduction of succinate. We found that while a total of 26 theoretical studies, published between 2002 and 2016, reported different *in silico* strain design strategies for the overproduction of succinate, only 10 studies experimentally implemented any kind of the previously generated theoretical knowledge. Similar to the case of OptKnock, none of these publications reported an exact application of the corresponding computational predictions used to guide the strain design process.

Construction, characterization and adaptive evolution of mutant strains is a costly and time consuming process. Aiming at the minimization of experimental efforts, *in silico* predictions of alternative modeling approaches should be first generated, analyzed and compared, before *in silico* identified production genotypes are *experimentally* implemented towards the construction of actual production strain(s). For that reason, we now turn our attention to the application of a kinetic-based approach to identify targets for taxadiene overproduction *in silico*.



Figure 5.6.: Application of OptKnock to the Production of Taxadiene in *E. coli*: Targets. Deletion targets identified by OptKnock over the whole growth rate range are summarized for each oxygen condition. The larger the number of reactions in each histogram, the higher the effect of growth rate on deletion target identity A. Oxygen-rich conditions. B. Oxygen-poor conditions. Abbreviations: PPC, phosphoenolpyruvate carboxylase; PGI, glucose-6-phosphate isomerase; Pyk, pyruvate kinase; MALS, malate synthase; PFL, pyruvate formate lyase; TKT2, transketolase; ACALD, acetaldehyde dehydrogenase; LDH, L-lactate dehydrogenase; FUM, fumarase; FRD7, fumarate reductase; CS, citrate synthase.

5.4.2. Kinetic-based Methods: The OptEM Algorithm

In many cases, the *modulation* of native and heterologous gene expression in the form of gene up- or down-regulation, rather than gene *knockouts*, is necessary to achieve optimal strain performance [1,164]. Additionally, genetic perturbations can affect the dynamic stability of cellular metabolism, which in turn set limits on maximal productivity [144] and maximal product yield [71]. Since a kinetic description of cellular metabolism is a prerequisite to properly study these issues, constraint-based methods, like the previously discussed OptKnock, overlook the potential detrimental effect that identified genetic interventions could have on actual strain performance. As a consequence, further genetic interventions are often necessary to achieve high experimental strain performance [42, 149, 164].

Rate laws represent a central component of kinetic models of metabolism. They describe reaction fluxes as a function of metabolite and enzyme concentrations and allow the consideration of metabolite-level enzyme regulation. Since rate laws and their associated kinetic parameters are normally unknown for many enzymes, the application and development of kinetic-based modeling approaches for strain design has been rather moderate [28, 149].

Here, we lay the groundwork for OptEM, a novel kinetic-based strain design algorithm. OptEM uses the Ensemble Modeling formalism EM [146] to build an ensemble of kinetic models that fulfill a given reference flux distribution. OptEM facilitates the maximization of complex user-tailored objective functions, for instance the weighted sum of productivity, product yield and production rate. The kinetic nature of the optEM algorithm allows for consideration of typically inaccessible design parameters such as enzyme over-expression



Figure 5.7.: Overview of the Main Steps Comprising the OptEM Strain Design Algorithm Ensemble Construction, Parameter Integration & Flux Calculation and Objective Function Evaluation are the three main steps comprising the OptEM algorithm. The effect of genetic perturbations, defined by \mathbf{U}^{pert} , on strain performance can be assessed in silico by evaluating an user-defined objective function Z. This input-output relationship is shown by the orange arrows. Optimal strain design strategies can be identified applying a brute force or a solver approach. Both options are discussed in the main text.

level, overall system stability and metabolite concentration pattern after enzyme perturbation. The idea behind OptEM is described in Figure 5.7. For a given enzyme perturbation vector \mathbf{U}^{pert} , the methodology calculates the corresponding value of an user-defined objective function. Since enzyme and metabolite concentrations are normalized to 1 for the given reference flux distribution, values higher than 1 refer to enzyme overexpression. Analogously, values lower than 1 represent enzyme downregulations. Depending on the size of the metabolic reconstruction used and the number of perturbations allowed, OptEM can extensively explore the design space by employing a brute force approach, as shown in Figure 5.8. If a brute force approach is impractical due to limited computational resources, a solver approach can be used, as explained in the next section.

The OptEM methodology can be summarized in three main steps, as indicated in Figure 5.7:

- 1. Ensemble Construction: this step requires four inputs, namely a reference flux distribution (\mathbf{V}^{ref}) for the strain being optimized; an associated metabolic reconstruction consisting of a stoichiometric and a regulatory matrix (Net); rate laws or "rules" to generate rate laws for each reaction in the metabolic reconstruction (Rules) and the number of models to be generated (n). The output of this step is an ensemble of n models, all fulfilling the given steady state flux distribution. Since metabolite and enzyme concentrations are normally unknown, they are normalized to 1 during the process of ensemble construction.
- 2. Parameter Integration & Flux Calculation: steady state metabolite concentrations are integrated over an enzyme trajectory, defined by \mathbf{U}^{pert} \mathbf{U}^{init} [74]. Resulting steady state metabolite concentrations can be transformed into fluxes using rate laws generated in the step 1. Note that \mathbf{U}^{init} corresponds to a vector of all-ones

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of adequate size. Output of this step are the vectors \mathbf{V}^{pert} , \mathbf{X}^{pert} and \mathbf{U}^{pert} describing flux distribution, metabolite concentration and enzyme concentration, all of them after conducting enzyme perturbation dictated by \mathbf{U}^{pert} , respectively. Variable SS^{pert} describes the percentage of models remaining stable after perturbation.

3. Objective Function Evaluation: output of step 2 can be used to evaluate an user-defined objective function described by $Z = f(\mathbf{V}^{pert}, \mathbf{X}^{pert}, \mathbf{U}^{pert}, \mathbf{SS}^{pert})$. By doing so, the specific effect of the genetic perturbation described by \mathbf{U}^{pert} on strain performance can be numerically assessed and compared with alternative genetic perturbations, thus leading to the identification of strain designs maximizing Z. Note that the evaluation of the objective function should be performed for each model in the ensemble. The effect of a given perturbation on the objective function Z can be then characterized by calculating the median and 25th and 75th percentiles.

Objective Functions

The vast majority of Metabolic Engineering efforts to date have aimed at the optimization of product yield. However, it has been recognized that not only high product yields but also high volumetric productivity and product titer, strain robustness and the ability to use low-cost substrates are key factors defining process viability and should therefore be primary objectives for bio-process development [74, 86]. In line with this, OptEM was developed to allow the optimization of user-tailored objective functions, considering the most relevant process parameters. Table 5.3 lists various examples. While each of these objective functions targets product yield maximization, they also maximize or minimize secondary objectives like concentration of toxic pathway intermediates, strain robustness and protein burden.

Brute Force Approach

In order to illustrate the probabilistic nature of OptEM predictions, the effect of single enzyme up- and down-regulation on product yield for the strain Δ XylE_1p is exemplarily shown in Figure 5.8. This particular strain was selected as case study out of all production strain candidates (see Table 5.1) because of its superior taxadiene production potential, as identified by a constraint-based analysis -see Figure 5.3 and refer to section 5.3 for details on the estimation of production potential using ¹³C-labeling data-. The reference flux distribution used to construct the ensemble of kinetic models was calculated assuming a taxadiene yield of 2.860×10^{-5} mol taxadiene/mol glucose, which corresponds to a mean taxadiene production level, as shown in Table A.9 in Appendix A.2.5. This assumption is justified by the fact that, as mentioned earlier, no experimental taxadiene concentration was available for this set of strains.

As specified in Figure 5.8 by the arrows, the outcome of single up- or down-regulation of a given enzyme with respect to the numerical value of the objective function can be categorized into three different groups. The first group exhibits an increase of the objective function for *all* models in the ensemble, as shown by the green arrows. In this case, the 25th percentile characterizing the effect of the given enzyme perturbation lies above the basal level of the objective function. Conversely, the second group is characterized by

Table 5.3.: **Objective Functions for OptEM.** The proposed algorithm allows for the optimization of user-tailored objective functions. Some examples are provided below.

| ation of user tanored objective functions. Some examples are provided below. | | | |
|--|---|--|--|
| Rationale | Objective Function | | |
| Product Yield. It is the simplest and most com- monly used objective function in strain optimization | $Z = \frac{\boldsymbol{V}_{txdn}^{pert} C_{txdn}}{\sum\limits_{i} \boldsymbol{V}_{i}^{pert} C_{i}}$ | | |

Product Yield. It is the simplest and most commonly used objective function in strain optimization efforts. Product yield is defined as the amount of product synthesized per amount of substrate consumed. Depending on the units used to calculate this ratio, product yield can be expressed on a molar, mass or carbon basis, as discussed in Chapter 7.

+ Minimization of Toxic Intermediates. Strain designs can be found so that product yield is maximized, while intracellular concentration of toxic intermediates is minimized. For instance, toxicity of high concentrations of phosphorylated pathway intermediates, e.g., isopentenyl pyrophosphate and dimethylallyl pyrophosphate, during taxadiene overproduction in $E. \ coli$ has been experimentally observed [93].

+ Maximization Strain Robustness. Heterologous or native enzyme overexpression can generate failure of the metabolic system due to the disappearance of a stable steady state [74]. In turn, this leads to cell death and a reduced productivity [144]. System robustness can be quantitatively estimated as the probability of system failure in an ensemble of models.

+ Minimization of Protein Burden. Enzyme overexpression draws energy and biomass building blocks from the cellular metabolism. Depending on various factors, e.g., overexpression strength, enzyme amino acid sequence, carbon source, etc., enzyme overexpression can lead to a reduced cellular growth rate and consequently, a reduced productivity. Strain designs can be identified so that product yield is maximized, while the amount of enzyme invested is reduced.

$$Z = \frac{\boldsymbol{V}_{txdn}^{pert} C_{txd}}{\sum_{i} \boldsymbol{V}_{i}^{pert} C_{i}} \left(\frac{1}{\sum_{j} \boldsymbol{X}_{j}^{pert} Tox_{j}}\right)$$

$$Z = \frac{V_{txdn}^{pert} C_{txd}}{\sum_{i} V_{i}^{pert} C_{i}} SS^{pert}$$

$$Z = \frac{\boldsymbol{V}_{txdn}^{pert} C_{txd}}{\sum_{i} \boldsymbol{V}_{i}^{pert} C_{i}} \left(\frac{1}{\sum_{k} \boldsymbol{U}_{k}^{pert} M W_{k}}\right)$$

Vectors V^{pert} , X^{pert} and U^{pert} and variable SS^{pert} are obtained during the second step of the OptEM algorithm, as explained in the main text. V_{txdn}^{pert} and C_{txdn} represent taxadiene flux and number of carbon atoms in a taxadiene molecule, respectively. Variables i, j and k define the set of uptake reactions for carbon sources, toxic intracellular metabolites and perturbed enzymes, respectively. Finally, C_i , Tox_j and MW_k correspond to the number of carbon atoms in the carbon source absorbed in reaction i, relative toxicity index for metabolite j and molecular weight of enzyme k, respectively.



Figure 5.8.: Effect of Single Enzyme Up- and Down-regulation Predicted by OptEM for the Maximization of Taxadiene Yield in Strain $\Delta XylE_1p$ via a Brute Force Approach. Effect of single enzyme up- (A.) and down-regulation (B.) on taxadiene yield is shown. Ensemble of predictions for each perturbation is characterized by calculating the median and the 25th and 75th percentiles. Product yield after each enzyme perturbation is normalized to that of the wild-type strain, which in this specific case is assumed to exhibit a yield of 2.860×10^{-5} mol taxadiene/mol glucose. Green arrows exemplarily highlight perturbations *increasing* the value of the objective function, while orange and black arrows mark perturbations *decreasing* and *inconclusively* affecting the value of the objective function, respectively. Note that in this particular case, individual enzyme identity is not relevant. Rather, we aimed at showing the nature of the outcome that single enzyme perturbation might originate on the objective function, as predicted by OptEM. The model used corresponds to a modified version of the core *E. coli* core [107], containing the taxadiene production pathway and 17 efflux reactions representing biomass synthesis. Ensemble size corresponds to 100 models.

5. Strain Design Algorithms for Target Identification

| Taxadiche Tiela in Strain $\Delta xyi D$ ip. 100 models, three uncreate hax distribu- | | | | |
|--|--------|--------------------------------------|---|--|
| tions. Note that each genetic perturbation corresponds to a single strain design strategy. | | | | |
| Perturbation | Target | Reaction Name | Reaction Details | |
| Up | dxs | 1-deoxyxylulose-5-phosphate synthase | $Pyr + G3P \longrightarrow DXYL5P + CO_2$ | |
| | ispA | Dimethylallyltranstransferase | $DMPP + IPP \longrightarrow GRDP + 2Pi$ | |
| Down | PTAr | Phosphotransacetylase | $AccoA + Pi \longrightarrow ACTP + CoA$ | |
| | Pyk | Pyruvate kinase | $ADP + PEP + H^+ \longrightarrow ATP + Pyr$ | |

Table 5.4.: Enzyme Perturbations Identified by OptEM Leading to an Increased Taxadiene Yield in Strain $\Delta XylE_1p$. 100 models, three different flux distribu-

a decrease in the value of the objective function in *all* models, as shown by the orange arrows. This outcome is characterized by a 75th percentile lying under the basal level of the objective function. Finally, the third group has an undefined outcome. In this situation and depending on model parametrization, a specific enzyme perturbation can increase the objective function in some models, but also decrease it in others. This situation is characterized by a 25th percentile lying under the basal level of the objective function, while the 75th percentile lies above it. This analysis should help define rules for target identification. In this specific work, a given enzyme perturbation is categorized as positive only if the 25th percentile lies above the basal level of the objective function (first group).

As stated before, experimental concentration time courses for taxadiene were not available for any strain described in this chapter. However, the identification of genetic targets is still possible, if a specific taxadiene production rate is assumed that lies inside the intervals calculated in Section 5.3. Clearly, experimental implementation of the identified genetic designs will only lead to an increased taxadiene yield *in vivo*, if the assumption regarding the taxadiene production level was more or less accurate. Since taxadiene production ranges are rather wide -see Figure 5.3-, assuming a production rate accurately matching the actual, unknown rate becomes a difficult task. A methodology to overcome this problem and identify effective targets is presented as follows. For a strain in Table 5.1:

- 1. Identify a range of feasible production rates, as described in Section 5.3.
- 2. Sample the space of feasible production rates.
- 3. For each sample, use linear programming to generate a reference flux distribution that fulfills the assumed production rate (or yield), experimentally measured exchange rates and available ¹³C labeling data and, maximizes/minimizes a defined biologically feasible objective function. ATP maximization or minimization of oxygen uptake rate are some examples.
- 4. Apply the OptEM methodology to identify genetic perturbations maximizing a defined design objective function. Table 5.3 provides some examples.
- 5. Identify strain design strategies being independent on the assumed production rate.

Table 5.4 summarizes the results obtained for strain $\Delta XylE_1p$ after applying the methodology described above and assuming three different taxadiene production levels: 1.385×10^{-7} , 2.431×10^{-4} and 4.26×10^{-1} mmol taxadiene/gDW h, which correspond to the minimal,

Metabolites: **ATP**: adenosine triphosphate; **ADP**: adenosine diphosphate; **Pyr**: pyruvate; **G3P**: glyceraldehyde 3-phosphate; **DXYL5P**: 1-deoxy-D-xylulose 5-phosphate; **DMPP**: dimethylallyl diphosphate; **IPP**: isopentenyl diphosphate; **GRDP**: geranyl diphosphate; **Pi**: phosphate; **AccoA**: acetyl-Coa; **ACTP**: acetyl phosphate; **CoA**: coenzyme A; **PEP**: phosphoenolpyruvate.

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medium and maximal production rates, as identified by the constraint-based method described in Section 5.3, respectively. OptEM suggests that the individual up-regulation of the enzymes catalyzing the first step of two key pathways, namely non-mevalonate pathway (dxs) and taxadiene synthesis (ispA), would lead to an increased taxadiene yield. Interestingly, both genes are located in the same operon [81]. Experimental studies supporting the positive effect of overexpressing dxs (encoding 1-deoxyxylulose-5-phosphate synthase) and ispA (encoding a dimethylallyltranstransferase) on isoprenoid production can been found in the literature [54, 58, 154, 166], thus confirming the prediction power of the OptEM approach. Regarding down-regulation targets, the modulation of Pyk presumably serves the purpose of balancing pool levels of glyceraldehyde 3-phosphate (G3P) and pyruvate, the two precursors of the non-mevalonate pathway. Farmer et al. [39] reported that the simultaneous knockout of genes pykF and pykA, coding for pyruvate kinase I and II, respectively, increased the lycopene production 2.8-fold when compared to the control strain. The study explored many strategies to balance the level of both metabolites and concluded that: alterations in the central metabolism that redirect flux from pyruvate back to G3P enhance lycopene production, while alterations that channel carbon flux away from the G3P pool have the opposite effect, showing that G3P may be limiting in the biosynthesis of lycopene. Since the synthesis of taxadiene and lycopene differs only in the last reaction step, it can be expected that this observation holds true for taxadiene production and more broadly, for the terpenoid production via the non-mevalonate pathway. The second down-regulation target identified by OptEM corresponds to PTAr. This strategy can be rationalized by the fact that down-regulating PTAr necessarily leads to a reduction in the acetate production. Consequently, more carbon atoms are available for taxadiene overproduction.

The same methodology was applied for all other strains listed in Table 5.1. dxs and *ispA* were recurring up-regulation targets, additionally identified for strains HMS 2p and $\Delta xylE 2p$. Further up-regulation targets corresponded to *idi* for strain $\Delta xylE 2p$ and pgi for strain $\Delta ptsG$ 2p. Regarding down-regulation targets, pgk was identified for strain $\Delta ptsG$ 2p. Experimental evidence of the positive effect of *idi* amplification on taxadiene [16] and lycopene [24] production can be found in the literature. Additionally, pgi over-expression has also been reported to increase lycopene titers 2.3-fold compared to respective control strains [24]. We did not find experimental evidence supporting the positive effect of the pgk down-regulation on taxadiene synthesis. However, this strategy can be understood using the rationale provided in the previously mentioned study by Farmer et al. [39]. The gene product of pgk, phosphoglycerate kinase, catalyzes following reaction: 3-phospho-D-glycerate + ATP \iff 3-phospho-D-glyceroyl-phosphate + ADP. Reducing the flux through this reaction would necessarily lead to a reduction in the upstream reaction catalyzed by the G3P dehydrogenase: D-glyceraldehyde 3-phosphate + NAD^+ + phosphate \iff 3-phospho-D-glyceroyl-phosphate + NADH + H⁺. Thus, the expected overall effect of pgk down-regulation is an increase of the G3P pool which, as experimentally demonstrated by Farmer et al. [39], enhances terpenoid production.

Solver Approach

All strain designs previously discussed consist of one single genetic perturbation. However, experimental evidence strongly suggests that, very often, more than one genetic perturbation must be conducted to efficiently redirect the cellular metabolism towards Table 5.5.: Strain Design Strategy Identified by OptEM for the Maximization of Taxadiene Yield in Strain Δ XylE_1p Using a Solver Approach. A down-regulation of enzymes ALCD2x and TALA along with up-regulation of IDI were identified by the OptEM approach to increase the taxadiene yield 1.4-fold in strain Δ XylE_1p. In the case of ethanol secretion, the efficacy of experimentally down-regulating enzyme ALCD2x is questioned by its wide flux range. Note that flux ranges for all reactions were identified using ¹³C-labeling data and experimentally determined values for exchange reactions listed in Table 5.2.

| Position | Popation Staighiomatry | Reference | Flux | Reaction |
|----------|------------------------------------|-----------------------|------------------------------|-------------------|
| Reaction | Reaction Storemometry | Flux | Range | Perturbation Fold |
| ALCD2x | $ETOH + NAD \iff ACALD + H + NADH$ | -11.088 | [-15.5;0] | 0.1 |
| TALA | $G3P + S7P \iff E4P + F6P$ | -1.815×10^{-2} | $[-1.815 \times 10^{-2}; 0]$ | 0.19 |
| IDI | $DMPP \iff IPP$ | -2.75×10^{-3} | [-1.353; 4.059] | 2.21 |

Metabolites: **ETOH**: ethanol; **ACALD**: acetaldehyde; **S7P**: sedoheptulose 7-phosphate; **E4P**: D-Erythrose 4-phosphate; **F6P**: D-Fructose 6-phosphate; **G3P**: glyceraldehyde 3-phosphate; **DMPP**: dimethylallyl diphosphate; **IPP**: isopentenyl diphosphate;

 $\label{eq:constraint} \mbox{Reactions (Enzymes): } {\bf ALCD2x: alcohol dehydrogenase ; TALA: transaldolase ; IDI: isopentenyl-diphosphate delta-isomerase. }$

Flux units are given in mmol/gDW h.

overproduction of the target molecule. For instance, the sole idi over-expression increased the specific taxadiene titer 3.6-fold, from 0.5 mg/gDW in the control strain to 1.8 mg/DW in the strain over-expressing idi. By contrast, when combined with ppk or sthA, idiover-expression increased the specific taxadiene titer 11-fold, from 0.5 mg/DW in the control strain, to approximately 7 mg/DW [16]. A similar observation was made for studies reporting the lycopene [24] and abietadiene [98] overproduction in *E. coli*. In both cases, maximal product yield is reached after simultaneously perturbing two and three genes, respectively.

Motivated by this observation, a Genetic Algorithm (GA) was employed along with the OptEM approach to efficiently identify an enzyme perturbation vector maximizing an user defined objective function, in this specific case, product yield. Unlike the *extensive* search performed by the brute force approach to identify optimal single perturbations, the GA selectively searches the parameter space. The algorithm was implemented using a GA script, which contained nested FMINCON optimization routines. Figure 5.9 shows the optimal genetic perturbation strategy, identified by the OptEM algorithm for the strain $\Delta XylE_1p$, when a taxadiene production rate of $2.431 \times 10^{-4} \text{ mmol/gDW}$ h is assumed and an ensemble of 100 kinetic models is analyzed. In order to increase the success chance of the experimental implementation of the enzymatic perturbation identified by OptEM in silico, the objective function was adjusted to consider the 25th percentile of all responses in the ensemble for the tested perturbation (refer to Figure 5.8, green arrows). Note that alternative approaches, e.g., considering the median or mean response, are also possible.

Table 5.5 and Figure 5.9 summarizes the OptEM predictions for strain $\Delta XylE_1p$. As suggested by the algorithm, down-regulating enzymes ALCD2x and TALA 0.1- and 0.19-fold respectively, together with 2.21-fold up-regulation of enzyme IDI, increased taxadiene yield by at least 40% in 75% of the models encompassing the ensemble of 100 models.

Additional to the perturbation extend of each of the three enzymes, Table 5.5 also includes the reference flux for each reaction used for ensemble construction and its corresponding flux range. Provided flux ranges correspond to the 95% confidence interval calculated using available ¹³C-labeling data and values for exchange reactions listed in Table 5.2.



Figure 5.9.: Strain Design Strategy Identified by OptEM for the Maximization of Taxadiene Yield in Strain ∆XylE_1p Using a Solver Approach. Model used corresponds to the *E. coli* core metabolism (reactions contained in the blue rectangle), which was extended to allow for taxadiene synthesis (reactions contained in the orange rectangle). The model contains a total of 87 reactions and 69 metabolites. Reference flux distribution was generated considering available ¹³C-labeling data, experimentally determined exchange rates and an assumed taxadiene production rate of 2.431 × 10⁻⁴ mmol/gDW h. Matlab scripts used correspond to the FMINCON and GA optimization routines. For the GA, a population size of 10 was used, with a maximal number of 5 generations. Additionally, three reactions were allowed to be simultaneously up- and down-regulated 10- and 0.1-fold, respectively. Solver converged after 185 hours and identified strain design shown, which improved the reference taxadiene production 1.4-fold.

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Refer to Section 2.1.2 for more details on the calculation of confidence intervals. Reaction ALCD2x, representing ethanol production, has a large confidence interval for its rate. In terms of experimental efficacy, a wide confidence interval for a given reaction suggest that the outcome of perturbing its associated enzyme might not deliver results predicted *in silico*. More specifically, *in vivo* knocking out the gene adhE, whose gene product catalyzes the ALCD2x reaction, might not be even necessary, since the reaction ALCD2x, in accordance with available experimental measurements, might also carry a flux of zero under the experimental conditions tested. This rationale can be mathematically implemented by modifying the objective function as follows:

$$Z = \frac{\mathbf{V}_{txdn}^{pert} C_{txdn}}{\sum_{i} \mathbf{V}_{i}^{pert} C_{i}} \left(\frac{1}{\prod_{k} \frac{\mathbf{V}_{k,max}^{ref} - \mathbf{V}_{k,min}^{ref}}{\mathbf{V}_{k}^{ref}}} \right)$$

where \mathbf{V}_{txdn}^{pert} refers to the taxadiene production flux after enzyme perturbation and \mathbf{V}_{i}^{pert} to the uptake rates of carbon sources. C_{i} and C_{txdn} are weights used to transform rates from molar flux (mmol/gDW h) to carbon or mass flux. Alternatively, if only one single carbon source is used for production, weights can be ignored. Consequently, product yields are calculated in a molar basis. Finally, \mathbf{V}^{ref} refers to the vector containing the reference flux distribution. The count variable k defines the set of perturbed enzymes (reactions). Indices min and max respectively refer to lower and upper bound of the confidence interval. By using the objective function shown above, OptEM will mainly identify enzyme perturbation strategies whose affected reactions exhibit tight confidence intervals. In this way, the effect of uncertainties related to alternative flux distributions on target selection can be partly diminished. Note that if $\mathbf{V}_{k,max}^{ref} = \mathbf{V}_{k,min}^{ref}$ for a given reaction k, the objective function should to be adjusted to avoid numerical problems. In this case, it suffices to replace the expression $\frac{\mathbf{V}_{k,max}^{ref} - \mathbf{V}_{k,min}^{ref}}{\mathbf{V}_{k}^{ref}}$ by an arbitrary high number.

5.5. Discussion

Our cooperation partner Monika Fuchs at **IBK** constructed and characterized five different taxadiene producing strains. Necessary genes for optimal taxadiene synthesis were provided by plasmids pET28a_DS and pACY_MEP. In strains $\Delta ptsG_1p$ and $\Delta XylE_1p$, genes contained in plasmid pACY_MEP were integrated into the *E. coli* genome, in the *ptsG* and *xylE* position, respectively. Experimental characterization encompassed measurement of concentration time courses for biomass, glucose and acetate. Additionally, ¹³C-labeling patterns of protein-bound amino acids were also provided. Due to low production rates and concentrations in the culture medium, determination of time courses for taxadiene concentration was not possible for any strain for the low sample volume used.

Our first task was the characterization of the reduction of the metabolic burden in strains $\Delta ptsG_1p$ and $\Delta XylE_1p$. Using the concept of acetate lines [11], we showed that genomic integration of plasmid-coded genes reduced the metabolic burden. As suggested by the position of the acetate lines for strains $\Delta ptsG_1p$ and $\Delta XylE_1p$ relative to their corresponding parent strains $\Delta ptsG_2p$ and $\Delta XylE_2p$, genomic integration seemed to reduce the metabolic burden within strains carrying ptsG deletion in a bigger extent than

within strains carrying $\Delta xylE$ deletion (Figure 5.2). Conversely, it holds that strains carrying a *ptsG* deletion exhibit a higher metabolic burden when loaded with plasmid-based enzyme expression. Interestingly, this trend was also observed within strains used for sugar co-utilization studies (refer to Figure 6.11.B in Chapter 6).

In order to assess the effect of metabolic burden reduction on taxadiene production, we applied a constraint-based approach, namely FVA, on a modified version of the model iRL2013 [75]. Note that this model-based analysis was necessary due to the missing taxadiene concentration time courses. For strains $\Delta ptsG_1p$ and $\Delta XylE_1p$, FVA predicted a higher maximal theoretical taxadiene yield, compared to their respective parent strains. This observation suggests that a metabolic burden reduction can *potentially* increase taxadiene production. However, taxadiene production flux for all strains could also be almost zero, as suggested by the lower boundary of the taxadiene export reaction. Refer to Table A.9 in Appendix A.2.5.

One of our major tasks was the model-driven strain optimization. We first applied OptKnock [20] to predict triple reaction knock-outs potentially improving taxadiene production under two different oxygen levels. The motivation behind this was twofold:

- 1. Basan et al. [11] showed that loading the cells with plasmid-based enzyme expression causes acetate secretion to occur at lower growth rates which, as we shown in Chapter 4, can be *in silico* modeled by reducing the maximal oxygen uptake rate of loaded strains.
- 2. It has been recognized that oxygen supply is one of the most frequent problems associated with usage of shaking flasks [19]. By contrast, on-line monitoring and control of oxygen supply is possible in stirred bio-reactors.

Since both factors, genetic load and process scale-up (from shaking flask to stirred bioreactor) are relevant in the construction and screening of optimal production strains, the effect of a variable oxygen supply on optimal reaction knock-outs needed to be assessed. Interestingly, we observed that oxygen availability indeed had an effect on the set of deletion candidates predicted by optKnock. This implies that a given strain design, optimized using shaking flasks, might not exhibit the same optimal production phenotype in a large scale, stirred bio-reactor. Moreover, this also suggests that additional optimization rounds might be necessary if the level of metabolic load is changed, as plasmid-based enzyme expression presumably affects the respiration capabilities of the cell.

In a recent publication [149], we showed that in spite of their multiple flaws, constraintbased strain design algorithms, e.g. OptKnock, clearly outnumber kinetic-based straindesign algorithms. Motivated by this fact, we developed OptEM, a kinetic-based straindesign algorithm that makes use of the ensemble modeling approach to construct an ensemble of kinetic models, all fulfilling a given reference flux distribution. We applied OptEM to identify single and triple enzyme perturbations leading to an increased taxadiene yield. Single enzyme perturbations were identified by a brute-force approach which extensively explored the parameter space. Remarkably, identified single enzyme perturbations strategies agreed well with reported *in vivo* strategies, suggesting a good prediction power of our strain-design algorithm. The triple enzyme perturbation strategy identified by OptEM for the strain $\Delta XyIE_1p$ (refer to Table 5.5) can be rationalized in the context of the specific flux distribution used for this strain to populate the ensemble of kinetic models.

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More specifically, down-regulation of reaction ALCD2x, responsible for ethanol formation, aims at minimizing carbon loss. Note that the reference flux through this reaction corresponds to roughly 40% of the total carbon uptake. Down-regulation of TALA possibly targets at an increase in the G3P pool. Finally, IDI up-regulation is consistent with many experimental reports describing the positive effect of its over-expression on taxadiene [16] and lycopene [24] production in *E. coli*. Its positive effect on terpenoids production possibly points at sub-optimal DMPP to IPP ratios under physiological conditions and to an interdependence in the optimal expression levels of genes ispH, idi and ispA

The modeling approach used here to circumvent unknown kinetic parameters, a limitation commonly associated with kinetic-based descriptions of the cellular metabolism, opens a wide range of valuable applications. As shown in this chapter, one of these applications is the identification of relevant enzyme perturbations increasing yield of a target molecule. Another application, the assessment of production potential based on the flux distribution of a reference strain, will be applied in Chapter 6 and validated in Chapter 9 using experimental data. While specific kinetic parameter values are not required for any of these applications, computational power is mandatory in order to efficiently analyze large ensembles of kinetic models. Since computer clusters are not yet accessible for the majority of the research community, new mathematical methods are required to efficiently sample relevant parameter sets, thus shrinking the size of the model ensemble. Some options include:

- Application of parallel ¹³C-labeling experiments to accurately estimate the reference flux distribution [75] and thus reduce the scope of kinetic model.
- Consideration of thermodynamic constraints to reduce the space of feasible parameter sets, as suggested by Liebermeister et al. [78,79]
- Reducing the scope of sampled parameters by incorporating kinetic information of well characterized enzymes.

Due to difficulties related to the impossibility of determining experimental taxadiene concentrations for low volume samples, and to a re-orientation of the **SysBioTerp** project, none of the model-driven predictions made in this chapter were experimentally implemented. However, experimental data motivated the development of OptEM, a novel kineticbased strain-design algorithm, which as demonstrated, allows the identification of biologically feasible perturbation targets.

6. Simultaneous Utilization of D-Xylose & Glucose in *E. coli*

Enabling simultaneous utilization of glucose and D-xylose by E. coli for the production of valuable chemicals is a key milestone towards a bio-based economy. Moving toward this goal, six different strains exhibiting two different genetic backgrounds were constructed and experimentally characterized by our cooperation partner Katarina Kemper at IBK. All strains were assessed regarding sugar co-uptake level, metabolic burden and taxadiene production potential by applying constraint- and kinetic-based approaches. In order to describe the extent of simultaneous sugar utilization, we introduced a parameter we termed "% Carbon Xylose". This parameter ranges from 0, when all carbon atoms absorbed by the cell correspond to glucose, to 1, when all carbon atoms absorbed by the cell correspond to xylose. Using this parameter in combination with constraint-based modeling, we successfully predicted the effect of increasing co-substrate uptake on the biomass yield and growth rate. We also analyzed the effect that the simultaneous sugar utilization had on the cellular capacity via acetate lines. Based on experimental data, we hypothesized that metabolic burden is a phenomenon not only limited to protein over-expression, but can also arise due to a increasing usage of protein-expensive pathways, like the pentose phosphate pathway. We observed an increase of total protein content as sugar co-uptake increased and a downwards displacement of acetate lines as sugar co-uptake increased. Finally, we generated a reference flux distribution for each strain using ¹³C labeling data, which we used to construct an ensemble of models describing the cellular phenotype of each strain and to estimate the taxadiene production potential using a kinetic-based method.

6.1. Strains & Experimental Data

All strains presented in this section were constructed and characterized by our cooperation partner Katarina Kemper at **IBK**. Table 6.1 presents an overview of all strains, while Table 6.2 contains experimentally determined exchange rates, estimated as explained in Section 2.1.2. In total, six different strains were constructed and grouped into two strain families for analysis. Strains HMS, HMS_p1x and HMS_p3x belong to the family we term HMS, while all other strains belong to the family $\Delta ptsG$, in which as its name suggests, the gene ptsG has been knocked out.

In order to increase the degree of simultaneous utilization of glucose and D-xylose, a plasmiencoded XylE symporter is constitutively expressed in four of the strains listed in Table 6.1. Two different mutants of the XylE protein were implemented: the first enzyme variant contained one single mutation in its amino acid sequence (p13-XylE_{1x}), while the second variant contained three mutations in its amino acids sequence (p13-XylE_{3x}). Table 6.1.: Strains for Sugar Co-utilization Studies. Six strains were constructed and experimentally characterized. The first two strains, HMS and $\Delta ptsG$ correspond to basis strains for each of the two main strain families. p13-XylE_{1x} refers to a plasmid-coded XylE transporter with 1 mutation in its amino acid sequence, while p13-XylE_{3x} refers to a plasmid-coded XylE transporter containing 3 mutations in its amino acid sequence.

| Strain ID | Genotype | Description |
|----------------------------|--|--|
| HMS Empty | $\mathrm{HMS174(DE3)} + \mathrm{p13}$ | Wild-type (WT) strain. |
| $\Delta \text{ptsG Empty}$ | HMS174(DE3), $\Delta ptsG$ + p13 | WT background with deleted $ptsG$ gene. |
| HMS p1x | $\mathrm{HMS174(DE3)} + \mathrm{p13-XylE}_{1x}$ | WT strain + plasmid constitutively expressing |
| | | XylE transporter mutated in 1 position. |
| HMS p3x | $\mathrm{HMS174(DE3)} + \mathrm{p13-XylE}_{3x}$ | WT strain + plasmid constitutively expressing |
| | | XylE transporter mutated in 3 positions. |
| $\Delta \text{ptsG p1x}$ | HMS174(DE3), $\Delta ptsG + p13$ -XylE _{1x} | $\Delta ptsG$ strain + plasmid constitutively expressing |
| | | XylE transporter mutated in 1 position. |
| $\Delta \text{ptsG p3x}$ | HMS174(DE3), $\Delta ptsG + p13$ -XylE _{3x} | $\Delta ptsG$ strain + plasmid constitutively expressing |
| | | XylE transporter mutated in 3 positions. |

Table 6.2.: Experimental Characterization of Strains Used in Sugar Coutilization Studies. Reported rates correspond to the mean value of two biological replicates. Errors represent one standard deviation. Numerical values for the exchange rates were calculated as explained in Section 2.1.2 using experimental concentration time courses provided in Table A.10 of the Appendix.

| Strain | Growth Rate | Glucose Uptake Rate | Xylose Uptake Rate | Acetate Secretion Rate |
|---------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| HMS Empty | $0.258 \pm 2.88 \times 10^{-3}$ | $5.105 \pm 2.92 \times 10^{-1}$ | $2.057 \pm 3.45 \times 10^{-1}$ | $5.190 \pm 7.26 \times 10^{-2}$ |
| $\Delta ptsG Empty$ | $0.481 \pm 1.42 \times 10^{-2}$ | $3.140 \pm 1.46 \times 10^{-1}$ | $6.535 \pm 6.60 \times 10^{-2}$ | $0.756 \pm 3.22 \times 10^{-2}$ |
| HMS p1x | $0.487 \pm 1.28 	imes 10^{-2}$ | $5.659 \pm 2.51 \times 10^{-1}$ | $2.211 \pm 4.67 \times 10^{-1}$ | $6.559 \pm 2.57 \times 10^{-1}$ |
| HMS p3x | $0.316\pm9.53\times10^{-2}$ | 10.642 ± 7.28 | $11.691 \pm 1.38 \times 10^{1}$ | 3.735 ± 3.13 |
| $\Delta ptsG p1x$ | $0.422 \pm 4.29 \times 10^{-3}$ | $3.090 \pm 6.45 \times 10^{-1}$ | $4.955 \pm 6.74 \times 10^{-1}$ | $7.251 \pm 5.78 \times 10^{-1}$ |
| $\Delta ptsG p3x$ | $0.344 \pm 1.32 \times 10^{-2}$ | $1.599 \pm 2.34 \times 10^{-1}$ | $7.649 \pm 6.77 \times 10^{-1}$ | $8.779 \pm 5.51 \times 10^{-1}$ |

Growth rates are reported 1/h; glucose, xylose and acetate rates are given in mmol/gDW h.

Strains were experimentally characterized in duplicate. Experimental measurements consisted of concentration time courses for OD, glucose, D-xylose and acetate (refer to Appendix A.3.1 for raw data). All strains were cultivated in Riesenberg medium containing 2.5 g/l D-xylose, 2 g/l glucose and 0.5 g/l uniformly labeled ¹³C-glucose. Samples for labeling analysis were taken after 7 hours culture. Raw labeling data can be found in Appendix A.3.2. Exchange rates shown in Table 6.2 were used to calculate three strain performance parameters, namely % Carbon Xylose, total carbon uptake and biomass yield. The first performance parameter quantifies the extent of sugar co-utilization exhibited by each strain and is defined as follows:

$$\% Carbon Xylose = \frac{5 r_{xylose}}{5 r_{xylose} + 6 r_{glucose}}$$

where r_{xylose} and $r_{glucose}$ refer to uptake rates for xylose and glucose, respectively. These rates are multiplied by 5 and 6 in order to obtain carbon fluxes (C-mmol/gDW h) for each sugar. Clearly, % Carbon Xylose can take values between 0 and 1, and describes all possible scenarios, from a sole glucose utilization to sole xylose utilization, respectively. Strains listed in Table 6.2 exhibit a wide range of simultaneous sugar utilization, ranging from 0.25 for the parent strain HMS to 0.8 for the engineered strain $\Delta ptsG p3x$.

Figure 6.1 graphically shows the effect of increasing the extent of simultaneous xylose

Table 6.3.: Strain Performance Parameters. Extent of sugar co-utilization is quantitatively described by the variable % Carbon Xylose. Total carbon uptake was calculated as the weighted sum of xylose and glucose uptake. Weights correspond to the sugar carbon content, i.e. 5 and 6 respectively. Biomass yield was calculated as the ratio between growth rate and the weighted sum of substrate uptake rate for xylose and glucose. In this case, weights correspond to molecular weights of each substrate. Performance parameters were calculated independently for each of the two biological replicates. Reported values correspond to the mean value. Errors represent one standard deviation.

| Strain | % Carbon Xylose | Total Carbon Uptake | Biomass Yield |
|---|---------------------------------|----------------------------------|---------------------------------|
| HMS Empty | $0.250 \pm 2.09 \times 10^{-2}$ | 40.912 ± 3.48 | $0.211 \pm 1.56 \times 10^{-2}$ |
| $\Delta \mathbf{ptsG} \ \mathbf{Empty}$ | $0.634 \pm 8.44 	imes 10^{-3}$ | 51.512 ± 1.21 | $0.311 \pm 1.91 \times 10^{-3}$ |
| HMS p1x | $0.245 \pm 4.74 \times 10^{-2}$ | $45.007 \pm 8.26 \times 10^{-1}$ | $0.361 \pm 1.61 \times 10^{-2}$ |
| HMS p3x | $0.380 \pm 2.13 \times 10^{-1}$ | $122.308 \pm 1.13 \times 10^2$ | $0.170 \pm 1.82 \times 10^{-1}$ |
| $\Delta ptsG p1x$ | $0.574 \pm 1.80 \times 10^{-2}$ | 43.316 ± 7.23 | $0.329 \pm 5.16 \times 10^{-2}$ |
| $\Delta \mathbf{ptsG} \ \mathbf{p3x}$ | $0.800 \pm 9.32 \times 10^{-3}$ | 47.838 ± 4.79 | $0.240 \pm 1.49 \times 10^{-2}$ |

Total carbon uptake rates are given in c-mmol/gDW h; biomass yields are given in g biomass/g substrate.

and glucose utilization on biomass yield, growth rate and total carbon uptake. While the total carbon uptake rate seems to be independent on the extent of sugar co-utilization, both biomass yield and growth rate seem to decrease as the fraction of absorbed xylose is increased. Note that the experimental data corresponding to the strain HMS p3x seems to correspond to an outlier. This is confirmed by large standard deviations in all its performance parameters.

The effect of the ptsG gene deletion and mutations in the transporter protein XylE on the extent of xylose and glucose co-utilization can be evidenced and quantified using the introduced variable % Carbon Xylose. Overall, the strain family $\Delta ptsG$ exhibited higher levels of sugar co-utilization, with growth rates and biomass yields being comparable to those of the HMS strain family. Expressing the single mutated transporter $XylE_{1x}$ does not seem to increase sugar co-utilization levels, when compared to the respective control strain. By contrast, expression of the triple mutated transporter $XylE_{3x}$ consistently increased the extend of sugar co-utilization within the strain family $\Delta ptsG$. Due to large standard deviations in the experimental measurements for strain HMS p3x, the effect of expressing the triple mutated transporter $XylE_{3x}$ cannot be precisely quantified. However, the mean value of % Carbon Xylose for this strain suggests a positive effect on sugar co-utilization. (see Figure 6.1)

6.2. Constraint-based Characterization of Simultaneous Sugar Utilization

Our first modeling efforts are focused on a constraint-based description of the simultaneous sugar utilization in *E. coli*. More specifically, experimentally obtained values for total carbon uptake along with *in silico* estimated oxygen uptake rates are used to describe the effect of increasing sugar co-utilization on growth rate and biomass yield. Then, the concept of acetate lines presented in Chapter 4 is utilized to estimate the level of metabolic burden in each strain and to unveil its connection with increasing levels of sugar co-utilization.



Figure 6.1.: Strain Performance Parameters as a Function of Simultaneous Sugar Co-utilization Extent. Effect of simultaneous glucose and xylose utilization on biomass yield. Reported values correspond to the mean value of two biological replicates. Error bars represent one standard deviation. (A.), cellular growth rate (B.) and total carbon uptake rate (C.). For strain families HMS and ΔptsG, an increasing extent of sugar co-utilization seems to reduce both the biomass yield and growth rate. By contrast, total carbon uptake seems to be independent on the extent of sugar co-utilization. Experimental data for HMS p3x seem to represent an outlier.

6.2.1. Biomass Yield & Growth Rate

We learned from experimental data that an increase in the degree of xylose and glucose co-utilization, quantified via % Carbon Xylose, seems to reduce the cellular growth rate and the biomass yield in both strain families (see Figure 6.1.A and .B). However, the negative effect of increasing % Carbon Xylose vales on growth rate and biomass yield was experimentally observed in a limited range of sugar co-utilization, i.e, from 0.24 to 0.38 for strain family HMS and from 0.57 to 0.8 for the strain family Δ ptsG. In order to estimate the effect of sugar co-utilization on growth rate and biomass yield in the whole range of % Carbon Xylose, i.e. from 0 to 1, we employed experimentally determined exchange rates listed in Table 6.2, along with the *E. coli* genome-scale metabolic reconstruction iJO1366 [106].

We start by estimating the oxygen uptake rate for each of the six strains. For that, we minimize the reaction representing oxygen import from the medium to the cell, while simultaneously constraining reactions in the iJO1366 model representing rates for growth, glucose and xylose uptake, and acetate secretion to match experimentally determined values, as listed in Table 6.2. The estimated oxygen uptake rate for each strain is shown in Figure A.8 (in Appendix A.3.3). Overall, we observe a decrease in the oxygen uptake rate, as % Carbon Xylose increases. For strain HMS p3x, its unusually high substrate uptake (refer to Figure 6.1.C) leads to an *in silico* oxygen uptake rate of zero. Since the coefficients of determination \mathbb{R}^2 for the linear regression of oxygen uptake rate against % Carbon Xylose have relatively low values, 0.62 for strain family HMS and 0.56 for strain family Δ ptsG (for only three data points), we decide to consider two different case studies:

- Case study I: the oxygen uptake rate (r_{O_2}) is assumed to depend on % Carbon Xylose (x), as described by the functions: $r_{O_2} = -35.57x + 13.43$ for strain family HMS and $r_{O_2} = -12.02x + 13.69$ for strain family ΔptsG .
- Case study II: r_{O_2} is assumed to be independent from % Carbon Xylose and from the strain family. Additionally, we assign it a constant value of 5.2 mmol O_2/gDW h,



Figure 6.2.: In silico Calculated Effect of Sugar Co-Utilization on Growth Rate and Biomass Yield: Case Study I. Effect of simultaneous glucose and xylose utilization on growth rate (A.) and biomass yield (B.) as predicted using a constraint-based approach. For all calculations, the oxygen uptake rate (r_{O_2}) is assumed to depend on % Carbon Xylose (x), as described by the functions: $r_{O_2} = -35.57x + 13.43$ for strain family HMS and $r_{O_2} = -12.02x + 13.69$ for strain family Δ ptsG. Additionally, a constant total carbon uptake rate of 45 mmol Carbon/gDW h was assumed. Given these two constraints and assuming different sugar co-utilization levels, the maximal growth rate supported by the *E. coli* metabolic reconstruction iJO1366 was calculated using the COBRA toolbox along with the solver Gurobi.

which corresponds to the mean value of all estimated oxygen uptake rates, except the one for strain HMS p3x, which is assumed to be a outlier.

The second step consists on the determination of the total carbon uptake rate. From Figure 6.1.C, we observe that the total carbon uptake rate seems to be independent from both strain family and % Carbon Xylose. Ignoring the data point for strain HMS p3x, we obtain a mean total uptake rate of 45 mmol Carbon/gDW h. Assuming a constant total carbon uptake rate matching this value, one can estimate the effect of varying % Carbon Xylose values on growth rate and biomass yield by means of linear programming. Calculations are done for the two study cases previously introduced and shown in Figure 6.2 for case study I and Figure 6.3 for case study II.

In both cases, a negative effect of increasing % Carbon Xylose values on growth rate and biomass yield is predicted, in line with experimental observations (Figure 6.1.A and .B). As for particular values for growth rate and biomass yield at a given degree of sugar coutilization, they are greatly influenced by the assumption made on the oxygen uptake rate (r_{O_2}) . When r_{O_2} is assumed to be constant, regardless of the strain family and the degree of sugar co-utilization (Case Study II, Figure 6.3), our constraint-based approach predicts the strain family HMS to have higher growth rates and biomass yields than the strain family Δ ptsG. This trend is reversed, when a dependency of r_{O_2} on % Carbon Xylose is assumed. Since the main objective of this *in silico* analysis was to determine the kind of effect of sugar co-utilization on growth rate and biomass yield in the whole range of % Carbon Xylose, rather than calculating specific values for these variables, we conclude that, irregardless of the assumptions made on the oxygen uptake rate, increasing values of



Figure 6.3.: In silico Calculated Effect of Sugar Co-Utilization on Growth Rate and Biomass Yield: Case Study II. Effect of simultaneous glucose and xylose utilization on growth rate (A.) and biomass yield (B.) as predicted using a constraint-based approach. For all calculations, a constant oxygen uptake rate of 5.2 mmol O₂/gDW h and a constant total carbon uptake rate of 45 mmol Carbon/gDW h were assumed. Given these two constraints and assuming different sugar co-utilization levels, the maximal growth rate supported by the *E. coli* metabolic reconstruction iJO1366 was calculated using the COBRA toolbox along with the solver Gurobi.

% Carbon Xylose decrease both growth rate and biomass yield. Additionally, we conclude that experimentally measured oxygen uptake rates are indispensable to precisely calculate growth rates and biomass yields as a function of % Carbon Xylose.

6.2.2. Acetate Lines & Metabolic Burden

Plasmid-based expression of two XylE mutants, $XylE_{3x}$ and $XylE_{1x}$, was employed to alter the degree of xylose and glucose co-utilization within two *E. coli* strain families. As discussed in Chapter 4, protein expression can cause the reduction of cellular fitness, a phenomenon commonly know as metabolic burden. Here, we aim at applying the concept of acetate lines to assess potential fitness costs involved with an increased level of % Carbon Xylose. Based on a high amino acid sequence similarity of both XylE mutants, whose amino acid sequence only differ in 3 positions out of a total of 491 amino acid residues, one can anticipate similar protein expression levels. In terms of relative position and number of acetate lines, this means that the experimental data points for each strain family should be confined to just two acetate lines; one for the parent strain carrying an empty plasmid and one for the two strains supporting the plasmid-based XylE mutant expression. Figure 6.4 schematically shows the expected relative position of the acetate lines within a given strain family.

Experimental acetate lines are obtained by plotting growth rates against acetate secretion rates and employing the previously determined slope (refer to Figure A.1, Appendix A.1.1), as shown in Figure 6.5.B. By plotting growth rate as a function of % Carbon Xylose in the adjacent Figure 6.5.A, one can analyze the effect of simultaneous sugar co-utilization on the localization of the acetate lines.



Acetate Secretion

Figure 6.4.: Expected Shift in Acetate Lines as a Result of Plasmid-based XylE-Expression. A relative downwards shift of the acetate line is expected in strains supporting plasmid-based expression of XylE mutants, compared to the respective parent strains carrying only an empty plasmid. Since the amino acid sequence of $XylE_{1x}$ and $XylE_{3x}$ only differs in three amino acid positions, one would expect very similar protein expression levels. Consequently, the data points for strains bearing plasmids $p13-XylE_{1x}$ and $p13-XylE_{3x}$ should lie on the same acetate line.

Contrary to our expectations, we observe three acetate lines for each strain family instead of just two, as previously hypothesized based on protein sequence similitude. For instance, within strain family Δ ptsG, strains can be sorted by increasing burden levels, suggested by the relative position of the corresponding acetate lines, as follows: Δ ptsG Empty $< \Delta$ ptsG p1x $< \Delta$ ptsG p3x. This observation suggests that an increased degree of sugar co-utilization in strain Δ ptsG p3x might originate a metabolic burden that cannot be explained by the sole effect of XylE expression, which corresponds to the shift of the acetate line from Δ ptsG Empty to Δ ptsG p1x. This trend is not observed within the strain family HMS, in which sorting by burden level leads to: HMS p1x < HMS p3x <HMS Empty. By exhibiting the highest burden within its strain family, strain HMS Empty does not fit the observed - and biologically reasonable - trend for the strain family Δ ptsG. Consequently, we recommend our cooperation partner Katarina Kemper to experimentally characterize the strain HMS Empty one more time.

Based on its high sugar co-utilization degree and relative position of its acetate line, strain Δ ptsG Empty represents an ideal production strain candidate. In order to confirm its outstanding performance, this strain is also suggested for experimental re-measurement. As can be observed in Figure 6.6, performance of strain Δ ptsG was experimentally reconfirmed. By contrast, growth rate, acetate secretion rate and % Carbon Xylose of strain HMS Empty were significantly affected by experimental strain re-measurement. New experimental data cause the burden level in strain family HMS to match the one observed in strain family Δ ptsG. Consequently, one can generalize the effect of XylE expression and increased % Carbon Xylose on burden level as follows: *Strain* Empty < *Strain* p1x < *Strain* p3x, where *Strain* refers to either HMS or Δ ptsG. Key aspects learned from Figure 6.6 can be summarized into two points:

1. Sugar co-utilization increases extent of metabolic burden. This is evidenced by a



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Figure 6.5.: Effect of Glucose and Xylose Co-utilization on Growth Rate and Its Associated Metabolic Burden. The detrimental effect of increasing glucose and xylose co-utilization levels on growth rate can be visualized by means of % Carbon Xylose (A.). By plotting growth rate against acetate secretion rates (B.) the metabolic burden associated with an increased sugar co-utilization can be assessed.



Figure 6.6.: Effect of Glucose and Xylose Co-utilization on Growth Rate and Its Associated Metabolic Burden. Re-measurement of Selected Strains Experimental characterization of parent strains HMS Empty and $\Delta ptsG$ Empty is repeated and represented by the black symbols labeled as HMS Empty2 and $\Delta ptsG$ Empty2, respectively. Note that the denomination "Empty2" emphasizes that these data points represent experimental repetitions.

downwards displacement of the acetate line for strain HMS p3x and Δ ptsG p3x, relative to the acetate line of the corresponding strain expressing the XylE transporter with one single mutation. A tentative explanation for this observation is that xylose metabolism should be associated with an increased expression of protein-expensive pathways.

2. Strain family $\Delta ptsG$ does not seem to allow for robust plasmid-based protein expression. This is evidenced by the different extent in the response to protein expression observed for the two different strain families. Consider for example the expression of XylE_{1x}. While the acetate lines for HMS Empty2 and HMS p1x are almost identical, acetate lines for $\Delta ptsG$ Empty2 and $\Delta ptsG$ p1x are clearly differentiated, suggesting that the extent of metabolic burden caused by XylE_{1x} expression is much higher in the strain family $\Delta ptsG$ than in the family HMS. Similar trends are observed for the expression of XylE_{3x}. Additionally, Figure 5.2 provides further experimental evidence to this observation.

6.3. Assessing Taxadiene Production Potential

Does an increased degree of sugar co-utilization have a beneficial effect on taxadiene production? Which strain has the highest taxadiene production potential? Here, we apply both a constraint- and a kinetic-based approach to help answer these questions.

The calculation of maximal theoretical product yields by means of linear programming represents the simplest approach to assess the production capabilities of a given metabolic network under consideration of a given set of constraints. Here, we use the *E. coli* genome-scale metabolic reconstruction iJO1366 along with experimentally determined total carbon and estimated oxygen uptake rate to highlight the effect of increasing degrees of % Carbon Xylose on maximal theoretical taxadiene yields. As shown in Figure 6.7, calculations are done assuming two different growth scenarios. In the first case, a growth rate of zero is assumed (Figure 6.7.A), while in the second case, the same reaction is constrained to have an arbitrary value of 0.2 1/h for all % Carbon Xylose values (6.7.B). Regarding the oxygen uptake rate, it is assumed to be independent from % Carbon Xylose values and the genetic background (refer to case study II, Section 6.2.1). Additionally, a constant value of 7 mmol O_2/gDW h was assumed in order to ensure the existence of a flux distribution fulfilling all constraints over the whole range of % Carbon Xylose.

Since *E. coli* does not naturally produce taxadiene, the stoichiometric matrix of model iJO1366 is correspondingly expanded to allow for taxadiene biosynthesis from IPP and DMAPP as pathway precursors (refer to Appendix B.1.1). By maximizing the flux through the taxadiene export reaction, under consideration of constraints on growth rate and of glucose, xylose and oxygen uptake rates, one can assess the maximal production capability of the network. Usually, the production capability is expressed in terms of product yield. In this case, since two carbon sources are considered, product yield is expressed on a carbon basis:

$$Taxadiene \ Carbon \ Yield = \frac{20 \ r_{txdn}}{5 \ r_{xylose} + 6 \ r_{glucose}},$$

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Figure 6.7.: Assessing Taxadiene Production Potential by a Constraint-based Approach. The taxadiene production capability of the genome-scale metabolic reconstruction iJO1366 was assessed by means of linear programming assuming a constant growth rate (μ) of zero (**A**.) and of 0.2 1/h (**B**.). For all calculations, the upper boundary for oxygen uptake was set to 7 mmol/gDW h. In line with experimental evidence, a constant, combined carbon flux of 45 mmol C/gDW h was assumed. We observe a reduction in the maximal theoretical taxadiene yield as % Carbon Xylose increases from 0 to 1, as follows: When μ =0 (**A**.); taxadiene yield exhibits a maximal reduction of 1.2% for strain family HMS and of 0.208% for strain family Δ ptsG. Similarly, when μ =0.2 1/h (**B**.), taxadiene yield exhibits a maximal reduction of 1.68% for strain family HMS and of 0.28% for strain family Δ ptsG.



Figure 6.8.: Assessing Taxadiene Production Potential by a Kinetic-based Approach. Taxadiene production potential was estimated as suggested in [71]. Lumped reaction representing taxadiene synthesis is given in the main text. A total of 10.000 models were constructed based on ¹³C-labeling data and experimentally determined exchange reactions. A modified version of the *E. coli* core model was used as input for the ensemble modeling approach. Given KAY values correspond to the median. Note that error bars represent 25th and 75th percentiles of KAY values within the ensemble.

where r_{txdn} corresponds to the maximal taxadiene production rate and r_{xylose} and $r_{glucose}$ to xylose and glucose uptake rate, respectively. Multiplication by 20, 5 and 6 is used to transform respective rates from units mmol/gDW h into c-mmol/gDW h. Alternatively, rates can be transformed into g/gDW h by multiplication with respective molecular weights. Thus, obtained product yields would be on a mass basis.

Figure 6.7 reveals that for both strain families and the two growth regimes considered, increasing levels of xylose and glucose co-utilization reduce the potential of the *E. coli* metabolic network to produce taxadiene. However, the maximal reduction observed corresponds to just 1.69 %. Additionally, and for % Carbon Xylose values smaller than 1, our constraint-based approach predicts a higher taxadiene production potential for the strain family HMS. Finally, increasing growth rates at constant substrate uptake rate reduces the maximal taxadiene yield that can be reached by the network. This last observation can be rationalized from a mass balance perspective. As the growth rate increases at a constant substrate uptake level, the amount of carbon atoms drawn from the cellular metabolism to support biomass synthesis is incremented. Consequently, less carbon atoms are left that can be potentially used for taxadiene.

Actual product yields of strains in early optimization stages are usually low. Therefore, maximal theoretical product yields seldom allow an accurate assessment of production performance.

It has been recently shown that the dynamic stability of a given metabolic network can impose a further constraint on the maximal product yield that can be achieved by the network. Lafontaine Rivera et al. [71] termed this yield "Kinetically Accessible Yield (KAY)". In order to estimate KAY for a given molecule, the authors calculated flux values through a lumped reaction expressing the synthesis of the target molecule in one single reaction. Sub-

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Figure 6.9.: Dependence of Taxadiene Production Potential on % Carbon Xylose. Production potential calculated by a kinetic-based approach is plotted against % Carbon Xylose. Orange and blue arrows highlight the strain exhibiting the best production potential for strain family HMS and Δ ptsG, respectively. Note that while vertical error bars represent the 25th and 75th percentiles of KAY values within an ensemble of 10.000 models, i.e. they are *in silico* generated values, horizontal error bars represent the standard deviation of the experimental data.

sequently, product yields are calculated by dividing the flux through the lumped reaction by the corresponding substrate uptake rates. KAY equals to the maximal product yield that can be achieved before the network loses stability. The system is considered stable as long as the real part of eigenvalues of the Jacobian matrix is negative. Since a kinetic model describing cellular metabolism is needed for KAY calculations and, kinetic parameters associated with the particular kinetic model are typically unknown, Lafontaine Rivera et al. calculated KAY for an *ensemble* of kinetic models, rather than for one single model. The ensemble of kinetic models was constructed by sampling kinetic parameters so that the obtained models fulfill a given reference flux distribution. This methodology was applied to accurately predict experimental isobutanol yields in three different *E. coli* strains. Refer to Figure 5.B in [71] and to Section 2.3.1 for more details on the mathematical and computational implementation of the KAY approach.

Here, we used available ¹³C labeling data and exchange rates listed in Table 6.2 to generate a reference flux distribution for each strain using the software 13CFLUX2 [155] along with the *E. coli* metabolic model iRL2013 [75]. We extended the iRL2013 model to consider xylose uptake. Then, we estimated the production potential of each strain by calculating its kinetically accessible taxadiene yield by maximizing the flux through the following lumped reaction:

 $8 \text{ ATP} + 4 \text{ G3P} + 8 \text{ H}^+ + 8 \text{ NADH} + 4 \text{ NADPH} + 4 \text{ PYR} \longrightarrow 4 \text{ ADP} + 4 \text{ CO}_2 + 8 \text{ H}_2\text{O} + 8 \text{ NAD} + 4 \text{ NADP} + 16 \text{ P}_1 + 4 \text{ AMP} + TXDN.$

Results are summarized in Figure 6.8. Interestingly, sightly higher product yields are predicted for the strain family HMS, in accordance with our constraint-based estimation of production potential (see Figure 6.7). With a kinetically accessible yield of 0.109 c-



Figure 6.10.: Dependence of Taxadiene Production Potential on Growth Characteristics. Production Potential is plotted against growth rate (A.) and biomass yield (B.). In both cases, the existence of a particular value for growth rate and biomass yield maximizing the production potential is suggested by the data. Note that while vertical error bars represent the 25th and 75th percentiles of KAY values within an ensemble of 10.000 models, i.e. they are *in silico* generated values, horizontal error bars represent the standard deviation of the experimental data.

mol/c-mol, strain HMS p1x is predicted to have the highest taxadiene production potential from all considered strains. Analogously and with a kinetically accessible yield of 0.037 c-mol/c-mol, strain Δ ptsG p1x is predicted to exhibit the highest production potential within strain family Δ ptsG. In order to assess the effect xylose and glucose co-utilization has on production potential, calculated KAYs are plotted against respective % Carbon Xylose values, as shown in Figure 6.9. Orange and blue arrow highlight strains HMS p1x and Δ ptsG p1x respectively. For strain family HMS, KAY increases from 0.07 c-mol/cmol (for strain HMS Empty2) to 0.109 c-mol/c-mol (for strain HMS p1x) as % Carbon Xylose increases from 0.09 to 0.24 to then decreases to 0.012 (for strain HMS p3x) as % Carbon Xylose keeps increasing to reach 0.38. As for strain family Δ ptsG, KAY exhibits its maximum value of 0.037 c-mol/c-mol (for strain Δ ptsG p1x) at a % Carbon Xylose value of 0.57 and decreases as % Carbon Xylose increases. We conclude from Figure 6.9 that for each strain family, an optimal value of % Carbon Xylose exists. Deviations from this optimal point negatively affect the taxadiene production potential.

From Figure 6.2 we learned that increasing values of % Carbon Xylose led to a reduction in growth rate and biomass yield. Since both of these variables are better suited to globally describe the metabolic status of the cell, we analyze their effect on KAY, as shown in Figure 6.10. Growth rate and biomass yield seem to affect KAY in a similar way. In both cases, the data seem to suggest the existence of particular values for growth rate and biomass yield that maximize KAY. Remarkably, optimal growth rate (or biomass yield) for strain family HMS seems to coincide with optimal growth rate (or biomass yield) for strain family Δ ptsG.

6.4. Model-based Identification of Optimal Production Strain Candidates

So far, we have independently

- analyzed the effect of XylE mutants expression in two different strain families on the degree of sugar co-utilization using the variable % Carbon Xylose;
- characterized the effect of increasing levels of % Carbon Xylose on metabolic burden using the concept of acetate lines and,
- assessed the taxadiene production potential for each strain using a novel kinetic-based approach.

Now, we step forward to identify optimal production strain candidates considering these three factors at the same time. As suggested by Figure 6.11, strain HMS p1x does not only have the highest taxadiene production potential out of all strains, but it also exhibits a moderate degree of sugar co-utilization and metabolic burden. In order to allow for taxadiene production, strain HMS p1x must be further engineered by the introduction of genes by means of plasmids or genomic integration. As a consequence of this additional load, we expect a reduction in the growth rate of strain HMS plx. As suggested by Figure 6.11.C, a reduction in its growth rate would even increase its KAY value for taxadiene, since we expect the maximal KAY value to lie in the orange zone. If a strain with a higher degree of sugar co-utilization is desired, strain $\Delta ptsG p1x$ can be used as parent strain for further engineering rounds. Similarly to strain HMS plx, we expect a reduction in the growth rate of this strain due to an increased load. Assuming that the maximal KAY value for this strain family lies in the blue zone, a reduction in its growth rate would lead to an increase in the taxadiene production potential too. Note that the positive effect of additional load and subsequent growth rate reduction does not always lead to an increased KAY value. For instance, KAY values for strains $\Delta ptsG p3x$ and HMS p3x would probably decrease due to the reduction in their growth rates, as suggested by Figure 6.11.C.

6.5. Discussion

Xylose and glucose are the two most abundant sugars present in lignocellulosic biomass, a feedstock commonly regarded as renewable [40,52,100]. Unlike glucose-rich substrates such as corn, wheat or sugar cane, plant biomass can be provided in large quantities without ethical concerns related to food prices and land use. Efficient conversion of lignocellulosic hydrolysates requires simultaneous xylose and glucose utilization. However, in most bacteria, carbon sources are used in a hierarchical manner. For instance, *E. coli* preferably metabolizes glucose over xylose. This carbon source preference arises from different regulatory mechanisms, commonly referred to as Carbon Catabolite Repression (CCR). CCR can occur at many levels, including transcription activation and repression, control of translation and, inhibition of enzyme activity [49]. Many strategies have been developed to deactivate CCR to allow for simultaneous sugar utilization in *E. coli*, including deactivation of the phosphotransferase system by knocking out the genes ptsH, ptsI and crr [44], mutation of the gene ptsG [100], mutation of the global regulatory protein crp [163] and



Figure 6.11.: Model-based Identification of Optima Production Strain Candidates. Three different criteria, namely sugar co-utilization degree (A.), associated metabolic burden (B.) and production potential (C.) are applied to identify optimal production strain candidates. Error bars in Figures A. and B. represent one standard deviation of the data. In Figure C., vertical error bars represent one standard deviation of the experimental data, while horizontal values represent 25th and 75th percentiles of KAY values within an ensemble of 10.000 models.

deletions of some metabolic genes [45,165]. In *S. cerevisiae*, another biotechnologically relevant microorganism, the mutation of a XylE transporter lead to simultaneous xylose and glucose utilization. All known xylose transporters are competitively inhibited by glucose. Since the mutant XylE transporter exhibited no inbihition by glucose [40], xylose could be transported into the cell by the mutant XylE in presence of glucose.

Our cooperation partner Katarina Kemper at **IBK** combined two strategies, namely knocking out the gene ptsG and novel mutations in the xylose specific transporter XylE, to achieve different levels of sugar co-utilization in six *E. coli* strains. We quantified the extent of glucose and xylose co-utilization in those strains by means of a variable we termed % Carbon Xylose. As suggested by the experimental data (Figure 6.1) and confirmed by a constraint-based approach (Figure 6.2 and 6.3), increased % Carbon Xylose levels lead to a reduction in both the observed growth rate and biomass yield. Irregardless of the level of sugar co-utilization, the combined carbon uptake remained constant under the experimental conditions tested, at a level of 45 c-mmol/gDW h. This constant total carbon uptake rate, along with the lower quality of xylose (refer to Figure 6.12) offer an explanation for the decreased growth rates and biomass yields experimentally observed as % Carbon Xylose values increases. Moreover, experimental data suggest a decrease in the oxygen uptake rate as sugar co-utilization increases (refer to Figure A.8 in Appendix A.3.3), which as shown in Figure 6.12, should decrease even more the quality of xylose as substrate, expressed by its specific energy content.

For our strains, increased levels of xylose and glucose co-utilization come at the cost of an increased metabolic burden. This is evidenced in Figure 6.11.B by the downwards shift of the acetate line of a given strain, relative to its parent strain, as % Carbon Xylose increased. Interestingly, strain family Δ ptsG, showing overall a higher extent of % Carbon Xylose, seemed to exhibit a higher protein content than strain family HMS, presumably necessary to support high levels of sugar co-utilization (refer to Figure A.9 in Appendix A.3.4 for preliminary total protein content measurements supporting this hypothesis). As a consequence, strains derived from the parent strain Δ ptsG Empty showed a stronger



Figure 6.12.: Substrate Quality: Glucose vs Xylose for Different Oxygen to Substrate Ratios. Quality of glucose and xylose as substrates was assessed using energy content as quality criteria for different oxygen to substrate ratios (A.). The energy content ratio between glucose and xylose (B.) shows that glucose exhibits a higher substrate quality. However, this advantage over xylose greatly depends on the oxygen to substrate ratio. All calculations were performed using the genome-scale metabolic reconstruction iJO1366, as explained in Section 4.2.1.

downwards shift in its acetate lines, when compared to the shifts observed within the strain family HMS (see Figure 6.11.B). Since the introduction of further genetic elements into the strains and their expression is necessary to yield a strain capable of producing taxadiene, strain response to an additional load should be considered for the selection of optimal production strain candidates.

In order to accurately select optimal production strain candidates for further engineering rounds and thus to contribute the reduction of *in vivo* experimentation, we applied both a constraint- and a kinetic-based approach to quantitatively assess the taxadiene production potential of all strains. The constraint-based approach indicated a linear reduction in the theoretical maximal taxadiene yield as % Carbon Xylose increased for both strain families. Additionally, strain family HMS exhibited a superior performance when % Carbon Xylose < 1. Considering these predictions, the strain HMS Empty should be further engineered into a production strain, as it exhibits the lowest % Carbon Xylose out of all strains. On the other hand, the kinetic-based approach suggested a more complex relationship between the kinetically accessible taxadiene yield and % Carbon Xylose. This method predicted an overall higher taxadiene production potential for the strain family HMS, just as the constraint-based approach did. However, unlike the constraint-based approach, the kinetic based approach suggested the existence of a maximal taxadiene yield for each strain family, located at % Carbon Xylose values different from zero. Remarkably, the kineticbased approach suggested that optimal taxadiene production was only indirectly defined by % Carbon Xylose. The true variable determining the kinetically accessible yield for taxadiene was the growth rate or the biomass yield. Experimental evidence supporting this observation was provided by our cooperation partner Lars Janoschek at **STT**; refer to Figure 9.3.A in Chapter 9. Based on three aspects, namely extent of sugar co-utilization, its associated metabolic burden and taxadiene production potential, we suggest strain HMS plx for further engineering rounds towards the construction of an optimal production
strain. Since a further load, exerted by additional genetic elements introduced to allow taxadiene synthesis, is expected to reduce growth rate and biomass yield, we expect the experimental taxadiene yield to surpass the predicted KAY value for this strain, as shown in Figure 6.11.C. To the best of our knowledge, this work represents the first reported effort to guide the selection of strain candidates potentially exhibiting high production performance while considering concepts of metabolic burden and kinetically accessible yields.

At the moment of the submission of this work, experimental implementation of this modeldriven suggestion was still pending.

Part III. Results: Process Optimization



The third part of this work is composed of three chapters. In **Chapter 7** we address some of the questions arising when designing a production process: what is the best substrate (carbon source) for the production of a given target molecule? Which performance criteria should be defined to identify optimal carbon source? If two different metabolic pathways can be used for production, which one should be preferred? Does the pathway performance depend on the selected carbon source? Then, in **Chapter 8**, experimental data (growth, substrate uptake and production rates) of a semi-batch process for four different temperatures and time points of induction were analyzed. The aim was to develop a model to estimate optimal values for these two process parameters. Finally, in Chapter 9, two theoretical approaches for product yield prediction are compared: a constraint-based and a kinetic-based approach. Traditionally, production potential of metabolic networks has been assessed by constraint-based methods. By applying linear programming, it is possible to calculate maximal theoretical yield on a defined carbon source and on a given metabolic network. However, theoretical maximal yield is not an adequate proxy for *experimental* product yield, especially when it comes to describing the production performance of strains in early development stages. By contrast, a novel kinetic-based approach showed promising results, even though numerical values of all kinetic parameters were unknown.

7. Model-based Medium Optimization

Typically, the following questions are to be addressed in early design stages of a given biotechnological production process: what is the best substrate for the production of the target molecule? Which performance criteria should be applied to identify the optimal carbon source? If two different metabolic pathways can be used for production, which one should be preferred? Does pathway performance depend on the selected carbon source? Here, we apply constraint-based modeling to answer these questions. First, we defined two different performance criteria to assess the performance of various substrates, namely the maximal profit and the maximal theoretical yield. We calculate theoretical yields using three different bases: a carbon, a molar and a mass basis. Then, we used these criteria to rank 180 different growth-supporting carbon sources. The underlying calculation is the potential of the substrate to be transformed into taxadiene by the E. coli metabolic network. Three-substrate mixtures were also considered in the calculations. Additionally, aerobic and anaerobic optimal network performance was compared. Since taxadiene production via the non-mevalonate pathway requires energy in the form of ATP and CTP, our model-driven analysis suggests an aerobic production process. Surprisingly, no single carbon source tested allowed a complete conversion into taxadiene, i.e., all substrates exhibited a maximal theoretical yield lower than 1 c-mol taxadiene/c-mol substrate. The largest maximal theoretical yield was obtained for ethanol as single carbon source, with a value of 0.92 c-mol taxadiene/c-mol ethanol. By contrast, glucose exhibited a maximal carbon yield of 0.65 c-mol taxadiene/c-mol glucose. An analysis of optimal flux distributions identified CO_2 as the main source for carbon loss. Finally, we found out that the endogenous non-mevalonate pathway allows for a higher theoretical yield than the heterologous mevalonate pathway for glucose as the carbon source. However, this is not true for all 180 carbon sources analyzed. When both pathways were active in an optimal ratio, we observed a small degree of synergy (<6%) for some substrates, including glucose.

7.1. Performance Criteria for Substrate Selection

Before one can actually select the best substrate from a list of candidates, performance criteria need to be defined. For biotechnological production processes, *product yield* has been traditionally used to assess and to compare the production performance of different substrates and strains. Product yield is defined as the ratio of product gained to substrate consumed. Depending on the units used to calculate the ratio, one can express product yield on three different bases: on a molar basis (mol product/mol substrate), on a carbon basis (c-mol product/c-mol substrate) or on a mass basis (g product/g substrate). When assessing the economic performance of a given set of substrates, profit can be used as a performance criterion. We define profit as the ratio of US dollars gained to US dollars invested.

7. Model-based Medium Optimization

The choice of a particular performance criterion to identify the best carbon source depends on the aim of the optimization process. Thus, if the process designer is interested in maximizing revenue, the performance criterion to be applied seems obvious. On the other hand, if network efficiency is to be optimized, product yield on a carbon or mass basis should be preferred over product yield on a molar basis. This is because maximal values of molar yield are not constrained to a defined interval, but rather depend on the substrate used. This leads to difficulties while assessing a given product yield on a molar basis. For instance, is a product yield of 0.1 mol taxadiene/mol glucose good enough? By contrast, values for product yield expressed on a carbon or mass basis will always range from 0 to 1. Substrates exhibiting a product yield of 1 c-mol product/c-mol substrate allow for a *complete* conversion of substrate into product. In other words, the network performance is already optimal and can not be further improved.

7.1.1. Single Substrates

We start our constraint-based analysis by assessing 180 different growth-supporting substrates, based on the performance criteria previously described. The *E. coli* metabolic reconstruction iJO1366 [106] was used for all calculations. *Growth-supporting* refers to the ability of the iJO1366 network to *in silico* grow on a given substrate. In order to calculate maximal theoretical yields representing true upper boundaries, both the Non-growth Associated Maintenance (NGAM) term and the cellular growth rate were set to 0. Additionally, oxygen uptake rate was set to an artificially high value of 100 mmol/gDW h to ensure sufficient oxygen availability. Since the *E. coli* metabolism does not allow for an endogenous taxadiene production, the iJO166 model was extended by adding necessary reactions allowing taxadiene production as shown in Appendix B.1.1. Following steps were applied to calculate maximal profit and taxadiene yields using the endogenous non-mevalonate pathway for precursor production.

- 1. Choose one of the 180 substrates listed in Table B.1 (see Appendix B.1.2).
- 2. Set a rate of 1 mmol substrate/gDW h by adjusting the lower and upper bound of the respective uptake reaction.
- 3. Maximize flux through the taxadiene export reaction using linear programming.
- 4. The numerical value of the maximal flux calculated in previous step coincides with the taxadiene yield on a molar basis, i.e. $mol \ txd/mol \ substrate$. This is because substrate uptake rate was set to 1 mmol/gDW h. txd refers to taxadiene.
- 5. Calculate product yield on a *carbon* basis by multiplying yield obtained in step 4 by the factor: $\left[\frac{\frac{20\ c-mol\ txd}{1\ mol\ txd}}{\frac{x\ c-mol\ substrate}{1\ mol\ substrate}}\right]$; $x\ c-mol\ refers$ to the number of carbon atoms in the substrate chosen in step 1.
- 6. Calculate product yield on a mass basis by multiplying yield obtained in step 4 by the factor: $\begin{bmatrix} \frac{272.48 \ g \ txd}{1 \ mol \ txd} \end{bmatrix}$; $x \ g \ substrate$ refers to the molecular weight of the substrate chosen in step 1.

7. Calculate profit by multiplying yield obtained in step 4 by the factor: $\left[\frac{12600U L t L d}{1 mol t w d}\right]$; x US\$ substrate refers to current market price of the substrate chosen in step 1 per mol.

Carbon content, molecular weight and market price for all carbon sources can be found in Table B.2 in the Appendix. Figure 7.1 lists the substrate having the highest performance for each criterion and glucose and glycerol along with their respective position in the ranking. Refer to Table B.1 in the Appendix for a complete overview. From Figure 7.1 we can easily conclude that there is no global optimal substrate exhibiting the highest value for all performance criteria. Rather, optimal substrate differs according to the metrics used. In the case of glucose and glycerol, it is interesting to observe that while glucose seems to be superior when considering product yield on a molar basis, the trend is reversed when product yield is considered on either a carbon or mass basis.



Figure 7.1.: Substrate Ranking via Four Different Performance Criteria Performance criteria considered are profit in units of US\$ txd/US\$ substrate (**D**.) and taxadiene yield on a molar (**A**.), carbon (**B**.) and mass basis (**C**.). For each criterion, the substrate exhibiting the highest performance is shown. Performance and relative position in the ranking for glucose and glycerol is also provided. Profit and yield values are shown in the square brackets. The model used was a modified version of iJO1366. Substrate uptake rate was set to 1 mmol substrate/gDW h, oxygen uptake rate to 100 mmol/gDW h. Growth rate and NGAM were set to zero.

Another interesting observation is the fact that no single substrate can support a complete conversion into taxadiene. Ethanol allows with 0.88 c-mol txd/c-mol ethanol the highest conversion efficiency. This value means that in the best case, 12% of all carbon atoms absorbed by the network are lost in the form of by-products. At this point, it is important to state that these values only represent the *potential* of the metabolic network to produce taxadiene, without guarantee of biological feasibility. Due to regulatory or toxic effects triggered by the substrate or pathway intermediates, which are not considered in maximal theoretical yield calculations, we expect actual product yields to be significantly lower. Nevertheless, theoretical yield calculations are useful to unravel the potential of a given metabolic network.

Table 7.1.: Metabolic Models Used for Synergy Studies. All three models are based on the *E. coli* metabolic reconstruction iJO1366. All models were extended to allow for taxadiene production. IPP and DMAPP are referred to as pathway precursors for taxadiene synthesis.

| | Characteristics |
|---------|---|
| Model 1 | Mevalonate pathway is used for precursor biosynthesis |
| Model 2 | Non-mevalonate pathway is used for precursor biosythesis |
| Model 3 | Both mevalonate and non-mevalonate pathways are used for precursor biosynthesis |

7.2. Synergy as Design Principle for Pathway Selection

Motivated by the impossibility to achieve a complete conversion of any carbon source into taxadiene, we ask following question: can the simultaneous activity of both the mevalonate (MVA) and non-mevalonate (MEP) pathway improve substrate conversion? We introduce our approach to answer this question using glucose as the case study. Let us start by considering three different metabolic models, as shown in Table 7.1. Then, let us calculate the maximal theoretical yield for each of the three models. By comparing theoretical product yields supported by each model, it is possible to identify synergistic effects arising due to the simultaneous utilization of both pathways. Synergy exists, if the theoretical product yield for Model 3 is higher than the theoretical product yield for Model 1 and Model 2.

We quantify synergy as follows:

$$Synergy = \frac{max(Y_1, Y_2, Y_3) - max(Y_1, Y_2)}{max(Y_1, Y_2)}$$

where Y_i refers to product yield of one of the three models introduced in Table 7.1. Note that the basis used to express product yield (mol, mass or carbon) do not have an effect on the numerical value of synergy. It is possible to identify optimal pathway usage originating the observed synergy via constraint-based modeling, as shown in Figure 7.2. For that, a new constraint, determining the fraction of carbon flux going through each of the two pathways (mevalonate or non-mevalonate pathway), is set on the metabolic model. More specifically, we modulate the activity of the MEP pathway by constraining the flux through its first reaction, termed DXS in Figure 5.9 and DXPS in model iJO1366. By calculating maximal taxadiene yields for various MEP activity levels, ranging from 0 to 1, it is possible to identify an optimal flux fraction (MEP^{opt}), as shown in Figure 7.2. Note that MEP^{opt} will not only depend on the identity of the substrate used, but also on the production conditions. For glucose, it increases from 75% to 91% if the conditions are changed from fully aerobic to fully anaerobic. This observation suggests that the performance of the MEP pathway is less dependent on the value of oxygen uptake than the MVA pathway. In fact, while the maximal taxadiene yield achieved via the MEP pathway is reduced by roughly 15% as a consequence of oxygen deprivation, the maximal taxadiene yield achieved via the MVA pathway drops by 55% (refer to downwards displacement of points (1) and (3) in Figure 7.2.A and .B). In order to analyze the effect of growth rate on maximal taxadiene yields, synergy and MEP^{opt}, we consider a growth rate of 0.2 1/h along with a glucose and oxygen uptake rate of 10 mmol/gDW h. As shown in Figure 7.2.C, cellular growth reduces the maximal taxadiene reached by the E. coli network. This results obvious from a mass

balance perspective. Since growth and taxadiene production compete for a limited supply of carbon atoms, an increase in the growth rate will necessarily lead to a reduction in the maximal taxadiene yield. Interestingly, MEP^{opt} decreases from 75% to 70% if growth is considered (compare Figure 7.2.C and .A). This trend continues if growth is increased to 0.4 1/h. In this case, MEP^{opt} amounts to 56%, suggesting that taxadiene production via MVA pathway is less affected by growth than the MEP pathway (results not shown). However, at a growth rate of 0.4 1/h, the synergy between the MEP and MVA pathway only reaches 0.4 %.

Now, we extend synergy calculations to all carbon sources considering fully aerobic conditions and setting NGAM and growth rate to 0. Figure 7.3 summarizes the synergy observed for 180 substrates (refer to Table B.1 in the Appendix for a complete overview of the results). We observe that the simultaneous activity of the MEP and MVA pathway does not lead to an increased taxadiene yield for all substrates, i.e. synergy amounts to 0%. In total, 57 carbon sources belongs to this group, almost the half of which (28 substrates) exhibit higher taxadiene yield using the MEP pathway. With only 14 substrates having a synergy higher than 2.5% but lower than 5.7%, we conclude that simultaneous activity of both the MEP and MVA pathway does not lead to a substantial product yield improvement. A closer look at obtained carbon yields (refer to column "MEP+MVA. Carbon Yield" in Table B.1 in the Apendix) reveals that ethanol, with a carbon yield of 0.92 c-mol txd/c-mol ethanol, still exhibits the highest carbon efficiency. Although the synergy between MEP and MVA pathways increased the carbon yield for ethanol from 0.88 to 0.92 c-mol/c-mol, network performance is not optimal yet, since still 8% of all carbon atoms are lost in the form of by-products.

7.2.1. Three-Substrate Mixtures

Determined to find a network configuration that allows a complete substrate conversion into product, we asked the question, if substrate mixtures can potentially increase network performance. In order to keep the problem computationally tractable, we limited our study to two- and three-substrate mixtures. In total, we tested 972,150 different medium compositions:

$$\binom{180}{1} + \binom{180}{2} + \binom{180}{3} = \frac{180!}{1!\ 179!} + \frac{180!}{2!\ 178!} + \frac{180!}{3!\ 177!} = 972,150$$

As in section 7.1.1, we used a constraint-based approach along with the *E. coli* metabolic reconstruction iJO1366 to obtain results shown in Figure 7.4. Since substrate mixtures are considered, product yields calculated on a molar basis do not allow a direct assessment of the network carbon efficiency. Consequently, product yields are reported on a carbon basis. Calculations for profit and product yields on a mass basis can be performed analogously. To guarantee that the maximal possible product yield is identified during calculations, both pathways for precursor production (mevalonate and non-mevalonate) were introduced in the model iJO1366. The applied procedure was the following:

7. Model-based Medium Optimization



Figure 7.2.: Synergy as Design Principle for Pathway Selection. Glucose As a Case Study. All calculations were performed using the model iJO1366. This model was complemented with both the non-mevalonate (MEP) and the mevalonate (MVA) pathway. As shown in the top of the figure, the MVA pathway draws three acetyl-CoA molecules to produce one IPP molecule. By contrast, the MEP pathway draws a molecule of pyruvate and a molecule of glyceraldehyde 3-phosphate to produce a mixture of IPP and DMAPP. Refer to Figures A.5, A.6 and A.7 in the Appendix for a detailed overview of these two pathways and the reactions required for taxadiene production. The activity through the MEP pathway was *in silico* modulated from 0 to 1, which corresponds to its maximal flux. Modulation was done by constraining flux trough the reaction DXPS, the first reaction of the MEP pathway. Additional constraints were applied as follows: (A.) Fully aerobic taxadiene production. Oxygen uptake rate was set to 100 mmol/gDW h, glucose uptake rate to 1 mmol/gDW h and NGAM to 0. (B.) Anaerobic taxadiene production. Rates were set as (A.) but oxygen uptake rate was set to 0. (C.) Aerobic taxadiene production with a growth rate of 0.2 1/h and NGAM of 3.15 mmol ATP/gDW. Synergy was calculated as explained in the main text. Points (1), (2) and (3) correspond to Model 1, 2 and 3 respectively (see Table 7.1). MEP^{opt} defines the activity of the MEP pathway for which taxadiene flux is maximal.

7.2. Synergy as Design Principle for Pathway Selection



- Figure 7.3.: Synergy as Design Principle for Pathway Selection. 180 Substrates Synergy was calculated as explained in the main text for 180 different carbon sources. Taxadiene yields were calculated considering no growth rate and a NGAM value of 0. All calculations were made using the model iJO1366. Refer to Table B.1 in the Appendix for a complete overview of the results.
 - 1. Choose one of the 972,150 possible substrate mixtures (or single substrates).
 - 2. Allow the model to consume these substrates by setting the upper bounds for respective uptake reactions to 1 mmol substrate/gDW h.
 - 3. Maximize flux through the taxadiene export reaction using linear programming.
 - 4. Numerical value of product yield on a carbon basis can be calculated as follow: $\frac{20 \ r_{txd}}{\sum_{i=1}^{n} r_i \ c_i}$, where r_{txd} refers to taxadiene production rate, r_i substrate uptake rate for substrate *i* and c_i carbon content of substrate *i*. Consequently, $\sum_{i=1}^{n} r_i \ c_i$ refers to the total carbon uptake.
 - 5. Repeat step 1 to 4 for all remaining substrate mixtures.

Figure 7.4 reveals interesting features of the taxadiene production potential of the *E. coli* metabolic network. In average, maximal product yield expressed on a carbon basis lies at 0.57 c-mol txd/c-mol substrate for the substrate mixtures analyzed (refer to Figure 7.4.A). This means that on average, 43% of the absorbed carbon atoms of a given mixture are lost in the form of by-products. Additionally, ethanol still exhibits the highest *in silico* performance, with a product yield on carbon basis of 0.924 c-mol/c-mol (refer to Figure 7.4.B). In a last attempt to push the *E. coli* metabolic network to reach its production limit *in silico*, we turned our attention to analyze by-product secretion during taxadiene production. The motivation was not only to identify a medium composition leading to complete carbon conversion, but also the identification of bottle necks in the taxadiene production. Based on an analysis of optimal flux distributions, we noticed a significant carbon leak towards CO₂. In order to assess the extent of simultaneous taxadiene and CO₂ production, we calculated corresponding CO₂ carbon yields for the 972,150 substrate mixtures. Results are summarized in Figure 7.4.C. Interestingly, carbon leak in the form of CO₂ can amount to values up to 62% of the total carbon uptake. CO₂ production

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Figure 7.4.: Maximal Product Yield for Three-Substrate Mixtures Maximal taxadiene yields were calculated for 972,150 substrate mixtures considering both MEP and MVA for taxadiene production. All yields were calculated on a carbon basis. Shown are histogram of taxadiene yields (A.), zoomed histogram of taxadiene yields (B.) and CO₂ yields (C.). Vertical dotted line correspond to glucose. Calculations were done with the model iJO1366 considering fully aerobic taxadiene production. NGAM and growth rate were set to 0. CO₂ yields were calculated using the CO₂ export flux obtained for each of the 972,150 substrate mixtures.

has many sources, including production of pathway precursors, e.g. acetyl-coA production from glucose by the enzyme pyruvate dehydrogenase, NADH/NADPH regeneration and the first and last reaction of the MEP and MVA pathway, respectively. Even though production of acetyl-CoA and co-factor regeneration (NADH/NADPH) can occur without concomitant CO₂ production by clever substrate selection, CO₂ production associated to the MEP and MVA pathways cannot be avoided without engineering enzymes responsible for CO2 release, namely 1-deoxy-D-xylulose-5-phosphate synthase (encoded by gene dxs) and phosphomevalonate decarboxylase (encoded by gene mvaD), respectively (Refer to Figures A.5 and A.6 in the Appendix for a detailed overview of the MEP and MVA pathways). As far as we know, this has not been achieved yet. Thus we conclude that a *carbon neutral* taxadiene production is not possible for any substrate or substrate mixture.

If CO₂ production cannot be avoided, carbon fixation could offer a solution to the *the CO₂ challenge*. Bar-even et al. [10] designed and analyzed different synthetic carbon fixation pathways. The shortest possible fixation pathway identified by the authors corresponded to a pathway fixing two CO₂ molecules to produce glyoxylate, a two carbon compound. Two glyoxylate molecules can be then assimilated by a bacterial-like glycerate pathway to produce glyceraldehyde 3-phoshate (G3P) and one CO₂ molecule. The carbon fixation and glyoxylate assimilation pathway can be lumped into a single reaction as follows: $3 \text{ CO}_2 + 3 \text{ ATP} + 4 \text{ NADPH} \longrightarrow \text{ G3P}$. In order to investigate if the introduction of a synthetic CO₂ fixation pathway would lead to increased taxadiene yields, we introduced this pathway into the iJO1366 model. Then, we calculated the maximal taxadiene yield supported by the network using glucose as carbon source and both MEP and MVA pathways. We observed no improvement in the taxadiene yield for glucose.

7.3. Discussion

Even though the conclusion of the CO_2 challenge is rather unsatisfactory, we generated an extensive *in silico* knowledge regarding optimal carbon sources for taxadiene production. As such, this knowledge can be used to optimize experimental medium composition by employing substrates exhibiting high *in silico* performance values as carbon source. For instance, substrates potentially increasing the taxadiene production performance of a given main carbon source, for example glucose, can be rapidly identified and experimentally tested. Additionally, profit as performance criterion can be used in early stage techno-economic feasibility studies. By defining a minimum profit level that should be achieved by the process, it is possible to determine if a given host microorganism and a determined substrate have the *potential* to yield an economically feasible production process.

Many studies have assessed and compared the production potential of various substrates using the MEP, MVA or both pathways *in silico* [1,50,95,162]. However, the work reported here surpasses the scope of any of these studies, as we assessed and compared a total of 972,150 unique substrate mixtures. We demonstrated that it is impossible to convert any single substrate or substrate mixture into taxadiene in a carbon neutral fashion. Ethanol, with a taxadiene yield of of 0.924 c-mol/c-mol, was identified by our large-scale *in silico* analysis as the substrate allowing the highest carbon efficiency. Interestingly, as identified by Gruchattka et al. [50], ethanol along with the MVA pathway has allowed the highest experimental terpenoid yield (on a carbon basis) reported to date (refer to Table 2 in [50], for original publication refer to [156]). Even though the host microorganism was *S. cerevisiae* and the terpenoid produced corresponded to artemisinic acid, this study strongly points at the potential of ethanol as an efficient carbon source for taxadiene and in general, for terpenoids production.

As for the synergistic effects arising from the simultaneous utilization of the MEP and MVA pathway, a recent publication [160] experimentally reported an improvement in isoprene yield, when both pathways were active in *E. coli*. Yield improvement amounted to 20-fold and threefold respectively, compared to the sole usage of the MEP or the MVA pathway. In the case of the fully aerobic taxadiene production in *E. coli*, our constraint-based approach predicted an increment of 0.72% and 7.38%, compared to the sole performance of the MEP and MVA pathways, respectively (refer to Figure 7.2.A). Even though the extent of the synergy experimentally observed by Yang et al. [160] can not be directly compared to our in silico simulations, his study suggests that synergy calculations based on sole stoichiometric constraint-based assessment of pathway synergy was provided by Shen et al. [136]. The authors showed that *in silico* predicted synergistic effects arising from the simultaneous activity of two different pathways for the 1-propanol production, namely the threonine and the citramalate pathway, could be also observed *in vivo*.

Unlike our constraint-based calculations and additional reports [1,50,95] predicting a higher in silico potential of the MEP pahtway over the MVA pathway for taxadiene production, Yang et al. [160] experimentally demonstrated the superiority of the MVA pathway over the MEP pathway for isoprene production. Since both taxadiene and isoprene production depends on the DMAPP production flux, supported by either the MEP or MVA pathway, the report by Yang et al. [160] clearly evidences one of the intrinsic limitations of constraint-based modeling. Since pathway regulation at the transcription-, translation- or

7. Model-based Medium Optimization

enzyme activity-level are poorly considered or not considered at all in genome-scale metabolic reconstructions, biologically relevant aspects constraining flux through metabolic pathways can be overseen. Since the MVA pathway is a non-native pathway in *E. coli*, the flux through this pathway is not constrained by any regulatory elements. Consequently, terpenoid yields using the heterologous MVA pathway have been repeatedly reported to surpass the performance of the native MEP pathway [93, 98, 160]. In spite of its flaws, constraint-based modeling represents a valuable modeling tool. This is because large scale constraint-based analyses are computationally tractable (due to the efficiency of available linear-programming solvers) and because high quality genome-scale metabolic reconstructions for many relevant industrial microorganisms are easily accessible to the research community [66,123]. More importantly, the metabolism of all microorganisms is subjected to mass balance constraints. Hence, theoretical yields calculated using constraint-based approaches are true constraints, representing the maximal potential of a given host metabolism.

8. Model-based Semi-Batch Optimization

The performance of a plasmid-based production strain was experimentally assessed in a semi-batch process at different temperatures and time points of induction. Available data consisted of concentration time courses for biomass, substrate and product. The modeling task was to identify optimal production temperature and time point of induction in silico. To that end, we applied dFBA as modeling framework to describe the available experimental data. We used Arrhenius-like functions to mathematically describe the temperature dependence of calculated rates (growth, substrate uptake and production). Maximal productivity was used as the performance metric to be optimized by the model. By perturbing both production temperature and time point of induction and analyzing the system response, we identified a process setting that increased the maximal productivity by 56% in silico [84]. Unfortunately, Experimental implementation of this model-based prediction by our cooperation partner was not possible due to lacking reproducibility of experimental results. This was potentially caused by strain/plasmid instability. However, we believe that the proposed approach represents a valid proof of concept for process optimization using readily available experimental data in early stages of strain and process development.

8.1. Strain & Experimental Data

The strain used in this work was constructed by our cooperation partner Max Hirte at **IBK** and experimentally characterized by Lars Janoscheck at **STT**. Experimental strain characterization was performed in a 1.5 liter bio-reactor and was limited to the measurement of concentration time courses for glucose, biomass and taxadiene. Production was induced by adding Isopropyl β -D-1-thiogalactopyranoside (IPTG) to the bio-reactor after a previously defined biomass concentration was reached. We termed this moment the induction time point, $t_{induction}$. As shown in Table 8.1, this process parameter remained relatively constant for all processes, ranging from 6.25 to 8.25 hours. Since the main objective of this first characterization round was to identify an optimal production temperature, four different temperatures ranging from 16 to 37°C were tested. Note that while the production temperature $(T_{production})$ was varied, the temperature before induction was kept constant at a value of 37°C to ensure fast biomass formation. Figure 8.1 shows a schematic representation of the process set-up and experimental time courses obtained for a production temperature of 16 °C. Data for all other temperatures can be found in Tables B.3 to B.8, in Appendix B.2.1. The effect of IPTG addition on taxadiene production can be clearly observed in Figure 8.1.D. Shortly after induction, taxadiene is formed and its concentration keeps increasing as the process continues.

In order to use provided experimental data to identify optimal process parameters (production temperature and time point of induction), it is first necessary to develop a process

8. Model-based Semi-Batch Optimization

Table 8.1.: Experimental Process Parameters for Six Semi-Batch Fermentations.In order to identify optimal process conditions, six semi-batch fermentations were performed,testing four different production temperatures and time points of induction. Refer to TablesB.3 to B.8, in Appendix B.2.1 for experimental concentration time courses.

| | / | | | | |
|------------|-----------------------|------------------|----------------|--------------|--|
| Durana ID | Temperature | Production | Induction | Process | |
| Process ID | before induction [°C] | Temperature [°C] | Time Point [h] | Duration [h] | |
| 1 | 37 | 16 | 8.5 | 76.5 | |
| 2 | 37 | 16 | 7 | 73.75 | |
| 3 | 37 | 22 | 7.25 | 75 | |
| 4 | 37 | 37 | 7.25 | 75.25 | |
| 5 | 37 | 22 | 6.25 | 74.75 | |
| 6 | 37 | 27 | 6.25 | 74.75 | |



Figure 8.1.: Process Set-up and Experimental Data A production strain containing three plasmids was characterized in a bioreactor using four different production temperatures. During the process, glucose was added to the bioreactor in irregular time intervals to prevent the culture from starving (A.). Strain characterization consisted of measurements of concentration time courses for dry weight biomass (B.), glucose (C.) and taxadiene concentration (D.). Dashed vertical line in Figure B. to D. represents the time point of plasmid induction t_{induction}.



Figure 8.2.: Modeling Experimental Data: Characteristic Process Times. Three different biomass production phases arise when characteristic times G_1 and G_2 are introduced. Analogously, two taxadiene formation phases are defined by G_1 and G_{2p} . Uncoupling taxadiene formation phases from biomass production provided a better fit of experimental data (results not shown). This is done by introducing G_{2p} (with $G_{2p} \neq G_2$) to mark the end of the first taxadiene formation phase. $r_{glucose}$, $r_{production}$ and μ refer to glucose uptake, taxadiene secretion and growth rates, respectively. μ_{WT} refers to the growth rate of the wild-type.

8.2. Mathematical Identification of Characteristic Process Phases and Rates Calculation

model capable of describing taxadiene production and its effect on biomass formation and glucose consumption. To describe growth dynamics, we first divide the process time into three different phases, defined by two characteristic times G_1 and G_2 . The rationale behind this strategy is the following: before the system is induced, cells grow with a rate defined by temperature and substrate concentration. This two parameters were kept constant for all six fermentations. Once the system is induced by IPTG, cellular growth is sharply decreased, as the cell reallocates its limited transcription and translation machinery to support the expression of genes encoded in the three plasmids. Thus, G_1 defines the moment, in which a reduction in the growth rate can be experimentally observed. We refer to the difference between $t_{induction}$ and G_1 as the time response. Since Taxadiene can be produced after all necessary enzymes are synthetized by the cell, G_1 also marks the moment in which taxadiene production begins. Due to the accumulation of toxic by-products and diminishing growth-supporting substrates, the cellular growth rate should decreases one more time as the process continues. We use the characteristic time G_2 to describe this moment. Analogously, G_{2p} is introduced to describe the moment in which the taxadiene production rate decreases or completely ceases. Figure 8.2 presents an overview of the location of all characteristic process times.

8.2. Mathematical Identification of Characteristic Process Phases and Rates Calculation

An optimization-based approach is introduced to guide the identification of characteristic process times for biomass production as follows:

Find G_1 and G_2 maximizing Z:

$$Z = \sum_{i}^{3} c_{i} R_{i}^{2}(G_{1}, G_{2}) = c_{1} R_{1}^{2} + c_{2} R_{2}^{2} + c_{3} R_{3}^{2},$$

with R_i^2 being the determination coefficient corresponding to the least squares regression of the natural logarithm of dry weight measurements against time, for phase *i* (see Figure 8.3.A), and:

 $c_i = 1$ if $\#Points \geq 3$, else $c_i = 0$.

#Points refers to the number of data points used for the linear regression.

Optimal G_1 and G_2 are identified using a brute force approach, in which Z values are calculated for all possible G_1 and G_2 combinations within a predefined interval. Since G_1 is defined to be located shortly after $t_{induction}$, we scan for optimal Z values between $G_1 = t_{induction}$ and $G = t_{induction} + 4$ h. As for G_2 , preliminary calculations showed optimal values to be located between 15 h and 60% of the total process time. Figure 8.3 shows the results obtained after applying this methodology for the identification of characteristic process times for batch 1. Optimal values for G_1 and G_2 can be obtained from Figure 8.3.B or C. Additionally, Figure 8.3.C, suggests the existence of many combinations of G_1 and G_2 values reaching at least 95% of the maximal Z value obtained for the whole simulation.

The identification of characteristic times implicitly allows the calculation of rates for growth, glucose uptake and taxadiene production. Growth rate in each of the three bio-

8. Model-based Semi-Batch Optimization



Figure 8.3.: Modeling Experimental Data: Mathematical Identification of Process Phases Results are shown for batch 1. A. Natural logarithm of biomass dry weight measurements (DW) is plotted against time. Our optimization-based approach identifies characteristic times G_1 and G_2 such that the sum of the three resulting R^2 is maximal. B. Values of the objective function Z for different G_1 and G_2 combinations. C. Characteristic process times achieving at least 95% of the maximal Z. As can be observed from this figure, Optimal characteristic process time correspond to $G_1 = 8.5$ h and $G_2 = 24.5$ h.

Table 8.2.: Growth, Production and Substrate Uptake Rates for Different Process Phases and Production Temperatures. Growth rates were calculated as described in Section 2.1.2 for three different phases identified by the optimization-based approach described in the main text. The same phases were used for the determination of substrate uptake rates. By contrast, only two phases were used for the calculation of production rates. Additionally, the identification of the characteristic time G_{2p} was done manually. However, an optimization-based approach could be analogously implemented.

| Batch ID | Char | Charasteristic Times [h] | | | Growth Rate [1/h] | | /h] | Gluo [1 | cose Uptak nmol/gDW | e Rate / h] | Txd Produ [mmol/ | ction Rate gDW h] |
|----------|-----------------------|--------------------------|-------|------|------------------------|------------------------|------------------------|------------|------------------------|----------------|------------------------|-----------------------|
| | tind | G1 | G_2 | G2p | Phase I | Phase II | Phase III | Phase I | Phase II | Phase III | Phase I | Phase II |
| 1 | 8.5 | 8.5 | 24.5 | 52.5 | 3.402×10^{-1} | 4.010×10^{-2} | 4.320×10^{-3} | 5.024 | 0.652 | 0.305 | 4.770×10^{-5} | 0.000 |
| 2 | 7 | 7.5 | 23.8 | 26.5 | $2.983	imes10^{-1}$ | 3.230×10^{-2} | $3.030 	imes 10^{-4}$ | 3.272 | 0.678 | 0.251 | 7.858×10^{-5} | 1.114×10^{-5} |
| 3 | 7.25 | 7.65 | 25.2 | 28.7 | 3.091×10^{-1} | 6.149×10^{-2} | $3.297 	imes 10^{-3}$ | 6.636 | 1.486 | 0.347 | 4.412×10^{-4} | 0.000 |
| 4 | 7.25 | 8 | 27.25 | 19.1 | $4.265	imes10^{-1}$ | 3.070×10^{-2} | 2.060×10^{-3} | 4.675 | 2.569 | 1.022 | 8.401×10^{-5} | 0.000 |
| 5 | 6.25 | 6.5 | 30.2 | 38 | 5.642×10^{-1} | 2.220×10^{-2} | 4.020×10^{-3} | 5.878 | 0.474 | 0.216 | 1.280×10^{-4} | $1.657 	imes 10^{-5}$ |
| 6 | 6.25 | 6.9 | 24.2 | 29.7 | 4.807×10^{-1} | 4.140×10^{-2} | 3.840×10^{-3} | 8.491 | 1.295 | 0.355 | 3.867×10^{-4} | 0.000 |



Figure 8.4.: Modeling Experimental Data: Results Experimental process set-up used for semi-batch fermentations (A.). Measured time courses for biomass (B.), glucose (C.) and taxadiene (D.) are compared with their respective *in silico* simulated time course for the Batch 1. Dashed vertical line in Figure B. to D. represents the time point of plasmid induction t_{induction}.

8.3. Dependence of Model Parameters on Production Temperature

mass production phases equals the slope of the corresponding line shown in Figure 8.3.A. Glucose uptake and taxadiene secretion rates are calculated by multiplying the growth rate of each of the phases by the slope of the straight line that results from plotting the glucose (or taxadiene) concentration as a function of biomass dry weight. Refer to Section 2.1.2 for more details on the calculation of rates from concentration time courses. Table 8.2 summarizes characteristic process times and respective rates for all six data sets. Note that taxadiene production rate in the second product formation phase (see Figure 8.2) was set to zero for Batches 1, 3 4 and 6. While this is a valid assumption in Batches 1 and 6 (refer to Figures 8.4 and B.5, respectively) because the taxadiene concentration remains relatively constant during this phase, we clearly observe a reduction in the taxadiene concentration for Batches 3 and 4 (refer to Figures B.2 and B.3 in Appendix B.2.3). This means that the taxadiene production rate in the second product formation phase should be negative rather than zero. Since the number of experimental points for taxadiene concentration in this phase is very limited, we assume a zero production rate to be more accurate than a rate calculated using just two data points. Independently of the validity of this assumption, it does not have an effect on predicted optimal $T_{production}$ or $t_{induction}$ values, as we will discuss later.

Exchange rates and characteristic process times are parameters that allow for a complete description of respective experimental concentration time courses. To demonstrate this, we applied dFBA to generate *in silico* time courses for each semi-batch fermentation process using parameters listed in Table 8.2 along with information regarding glucose pulses and initial biomass and glucose concentrations for each batch (refer to Tables B.3 to B.8, in Appendix B.2.1 for numerical values). As explained in Section 2.1.1, dFBA allows for the combination of reactor dynamics with cellular metabolism, thus allowing the simulation of concentration time courses of extra-cellular metabolites in the reactor. Figure 8.4 exemplarily shows the performance of dFBA simulations for batch 1 (refer to Figures B.1 to B.5 in Appendix B.2.3 for a complete results overview). As observed, *in silico* generated concentration time courses closely match experimental data (see Table B.11 in Appendix B.2.3 for R^2 values). All dFBA simulations reported in this work were performed using MATLAB functions provided by DFBALab [47].

8.3. Dependence of Model Parameters on Production Temperature

The main objective of the modeling effort presented in this chapter is the identification of optimal values for two process parameters, namely production temperature and time point of induction. So far, we have developed a modeling approach that allows the simulation of concentration time courses, closely matching experimental data. Since not all parameters listed in Table 8.2 are *directly* accessible, meaning that their numerical values cannot be freely adjusted experimentally, we venture to explore the effect of both production temperature ($T_{production}$) and time point of induction ($t_{induction}$) on them. Note that numerical values of growth and glucose uptake rate during the first production phase, μ_{WT} and $r_{glucose,WT}$ in Figure 8.2, are considered to be constant, since strain, initial medium composition and temperature in the first biomass production phase were not changed and are not subject to optimization in this work.

8. Model-based Semi-Batch Optimization



Figure 8.5.: Dependence of Characteristic Process Times on Temperature and Time Point of Induction. The dependence of characteristic process times on temperature is studied indirectly, by analyzing the relationship between duration of phases and temperature. This approach would allow the estimation of characteristic process times obtained at a non-measured $T_{production}$ and $t_{induction}$.

We first study the dependence of characteristic process times on $t_{induction}$ and $T_{production}$. For that, we apply the schema shown in Figure 8.5. Instead of directly analyzing the effect of $T_{production}$ on G_1 , G_2 and G_2p , we analyze its effect on $t_{response}$ and the duration of the second biomass production phase $(t_{biomass2})$ and first taxadiene formation phase $(t_{production1})$. Figure 8.6 shows these relationships. While $t_{response}$ linearly increases with $T_{production}$, meaning that the cell needs more time to synthesize enzymes required for taxadiene production at high temperatures, the duration of the main production phase, $t_{production1}$ linearly decreases as $T_{production}$ increases. As for $t_{biomass2}$, we do not observe a clear dependence on $T_{production}$. For that reason, we assume a constant value of 18.3 h, which corresponds to the average duration of the second biomass formation phase, as calculated from characteristic times listed in Table 8.2.



Figure 8.6.: Modeling Experimental Data: Temperature Dependence of Duration of Process Phases Linear relationships are used to describe the effect of $T_{production}$ on $t_{response}$ (A.), on the duration of the second biomass production phase (B.) and first product formation phase (C.).

The effect of $t_{induction}$ on G_1 , G_2 and G_2p can be described as follows:

$$G_1 = t_{response} + t_{induction}$$

$$G_2 = t_{biomass2} + G_1$$

$$G_{2p} = t_{production1} + G_1$$

Using these equations and the relationships shown in Figure 8.6, it is possible to calculate



Figure 8.7.: Modeling Experimental Data: Temperature Dependence of Exchange Rates Rates shown for a T_{production} of 16 and 22°C correspond to average values. A quadratic polynomial is used to mathematically describe the effect of temperature on growth (A. and B.) and glucose uptake rates (C. and D.) in the second and third biomass production phase. As for the taxadiene production rate in the first product formation phase, an Arrhenius-like formula is applied to mathematically describe the observed temperature dependency (E.). Plot F. shows taxadiene production rate obtained for each T_{production}. Refer to Table B.10 in Appendix B.2.2 for more details on the formulas used for regression.

numerical values for G_1 , G_2 and G_{2p} for a given set of $T_{production}$ and $t_{induction}$.

To describe the temperature dependence of growth and glucose uptake rate in the second and third biomass production phases, we used a second-degree polynomial. This approach was motivated by the work by Ratkowsky et al. [113], which suggested a linear relationship between the square root of growth rate and temperature, as follows: $\sqrt{\mu} = b(T - T_o)$. As shown in Figure 8.7 (plots A to D), a quadratic polynomial allows a good description of the experimentally observed temperature dependence of both growth and glucose uptake rates. Previous to the work by Ratkowsky et al. [113], Arrhenius-like formulas were suggested to describe the effect of temperature on biological phenomena (growth and bacterial luminescence) [36,57]. We use the formula suggested by Johnson et al. [57], developed to describe the effect of temperature on cellular growth, to account for the effect of temperature on the production rate during the first product formation phase. As evidenced in Figure 8.7.E, this approach provides a good fit to the data.



Figure 8.8.: Volumetric Productivity for Batches 2 and 5 Experimentally observed taxadiene productivity (circles) is plotted as a function of process time for Batches 2 (A.) and 5 (B.). Blue line represents predictions made with our dFBA-based approach.

8.4. *In silico* Optimization of Production Temperature and Time Point of Induction

So far, we have identified numerical values for characteristic process times and exchange rates (see Table 8.2), which used in combination with dFBA, allow the generation of concentration time courses for biomass, glucose and taxadiene, closely matching experimental data. Additionally, we introduced formulas to describe the effect of two process parameters, namely $T_{production}$ and $t_{induction}$, on them (characteristic process times and exchange rates). In this way, it is possible to *in silico* generate concentration time courses for $T_{production}$ and $t_{induction}$ values experimentally not tested so far and evaluate their impact on a given performance metric. In this section, we show how the developed model can be applied to identify values for $T_{production}$ and $t_{induction}$ that potentially increase the maximal volumetric productivity of the process. This metric is defined as follows: $P_{max} = max(\frac{txd_{concentration}}{t})$, where $txd_{concentration}$ refers to a vector containing taxadiene concentrations at certain time points, contained in the time vector t.

In order to reduce the simulation time and to provide a reliable prediction regarding optimal process parameters, we assume that for a given batch process, P_{max} is contained in the first product formation phase. This assumption was done to avoid inaccuracies in the calculation of the taxadiene time course during the second product formation phase, arising due to the incapacity of accurately describe the observed decrease in the taxadiene concentration during this phase for Batches 3 and 4 (refer to Figures B.2 and B.3, respectively). Taking a look at the taxadiene time course for Batches 2 and 5 (Figures B.1 and B.4, respectively), one might argue that this assumption negatively affects the prediction power of the model, since the taxadiene concentration keeps increasing for both batches during the second product formation phase. Interestingly, our simulations (see Figure 8.8) suggest that for both batches, P_{max} is indeed located within the first product formation phase, indicating that our assumption is accurate and do not affect the prediction power of the model. A similar behavior is observed for all other batches.

In order to identify numerical values for $T_{production}$ and $t_{induction}$ increasing P_{max} we proceed



Figure 8.9.: Model-based Optimization of Process Parameters A. 3D-View B. Top view. Optimal conditions correspond to $t_{induction} = 7.3$ h and $T_{production} = 32$ °C. Under these conditions, P_{max} amounts to 1.45×10^{-3} mmol/l h.

as follows:

- 1. Generate a two dimensional grid for $T_{production}$ ranging from 16 to 37 °C and $t_{induction}$ ranging from 0 to 13 hours, with a defined step, for instance 1°C for $T_{production}$ and 0.1 h for $t_{induction}$. Each position in the grid represents a specific combination of both process parameters.
- 2. For each position in the grid:
 - a) Calculate exchange rates and characteristic process times using formulas listed in Table B.9 and B.10. Note that growth and glucose uptake rate during the first biomass production phase are kept constant, and set to average observed values: $\mu_1=0.403 \text{ 1/h}$; $r_{glucose}=5.662 \text{ mmol/gDW}$ h (refer to Table 8.2)
 - b) Define initial concentrations. For instance 0.12 g/l biomass, 111 mmol/l glucose and 0 mmol/l taxadiene.
 - c) Generate respective concentration time courses using dFBA.
 - d) Compute P_{max}
- 3. Generate a three dimensional plot to evaluate the effect of $T_{production}$ and $t_{induction}$ on P_{max}

Figure 8.9 summarizes the results obtained after applying the procedure described above. A total of 2882 unique combinations of $T_{production}$ and $t_{induction}$ were tested in silico. As shown in the figure, a production temperature of 32°C and an induction time point of 7.3 hours represent optimal process parameters. Under these conditions, a P_{max} of 1.45×10^{-3} mmol/l h is reached. Compared to the P_{max} of 9.2615×10^{-4} mmol/l h for Batch 6, the highest P_{max} experimentally observed for all batches, this represents an increment of roughly 56 %.

8.5. Discussion

In this chapter, we developed a dFBA-based model capable of reproducing experimentally measured concentration time courses for biomass, glucose and taxadiene. Exchange rates and characteristic process times (see Figure 8.2) were used as model parameters. By expressing these parameters as a function of experimentally accessible process variables, namely time point of induction $(t_{induction})$ and production temperature $(T_{production})$, we were able to identify numerical values for these variables, which increased the maximal process productivity, P_{max} , by 56% in silico. Unfortunately and due to reproducibility issues, possibly related to strain instability, our cooperation partner at **STT** was not able to confirm our model predictions.

The introduction of characteristic process times and their associated phases represents a key element of our modeling approach. In order to keep model complexity as low as possible, we introduced three biomass production phases and two product formation phases. We believe that this strategy considers the lowest possible number of phases, while allowing a correct description of the data. Clearly, alternative models considering more phases for biomass production and product formation are also possible. However, these approaches would introduce unnecessary complexity, while at the same time complicating the interpretation of model parameters from a biological point of view.

In order to identify characteristic process times, we applied an optimization-based method. By maximizing an objective function Z, representing the goodness of fit of the biomass dry weight time course, values for G_1 and G_2 could be identified. By contrast, characteristic time G_{2p} was obtained by visual inspection. Consequently, our model reproduced the time course for biomass with increased accuracy, while the goodness of fit for glucose and taxadiene was comparatively poor (see Table B.11, in Appenxid B.2.3). A possibility to correct this drawback is to consider all characteristic times to maximize a more balanced objective function Z_{Total} :

$$Z_{Total}(G_1, G_2, G_{2p}) = Z_{Biomass}(G_1, G_2) + Z_{Glucose}(G_1, G_2) + Z_{Taxadiene}(G_{2p})$$

where $Z_{Glucose}$ and $Z_{Taxadiene}$ are defined analogously to $Z_{Biomass}$. This approach will certainly allow for data description in a more balanced fashion. However, it will also require more experimental information. In our opinion, this could compromise the biological significance of model parameters, since its determination would be exposed to an increased degree of experimental error. The reason why we decided to only use the biomass time course for the identification of characteristic process times was simple. As biomass formation can be easily monitored through optical density measurements (OD), more data points with less experimental error are available. To demonstrate the feasibility of using OD time courses as input signals defining G_1 and G_2 , we applied a similar approach to the one described in this chapter to identify optimal process conditions. Our OD-based model suggested a production temperature of 30.5°C and a time point of induction of 7.5 hours as optimal, in line with the previously obtained optimal values using a dry weight-based model (refer to Figure 8.9).

In spite of the mentioned drawbacks, numerical values for exchange rates identified by our approach for each phase had a biological meaning. For instance, the detrimental effect of system induction on cellular fitness can be evidenced by comparing the numerical values for growth and substrate uptake rate between Phase I and II (see Table 8.2). As a consequence of taxadiene production, the cellular growth rate decreased by roughly one order of magnitude. This behavior is in line with the phenomenon of metabolic burden, discussed in Chapter 4. Additionally, the temperature dependence of growth, glucose uptake and taxadiene production rates could be accurately described using established models [36, 57, 113].

Even though we limited our analysis to the identification of optimal values for two different process parameters, the spectrum of potential applications of the developed model is wide, including among others:

- 1. Development of substrate feeding strategies. Using a model-based approach to systematically design feeding strategies, starving phases in the bioreactor along with their associated negative impact on P_{max} , can be minimized/eliminated. Refer to Figure B.3 in Appendix B.2.3 for an illustration of this issue.
- 2. Estimation of optimal batch duration. After the maximal productivity (P_{max}) has been reached, additional process duration generates the process productivity to decrease (see Figure 8.8). Our model allows the identification of optimal values for this process variable, so that no unnecessary production time is wasted.
- 3. Estimation of by-product secretion patterns. For each point of time during the process, dFBA calculates flux distributions fulfilling certain constraints. In our specific case, these constraints correspond to growth, glucose uptake and taxadiene production rates for each phase. By maximizing and minimizing the flux through exchange reactions of interest, for instance acetate secretion, concentration time courses for the desired by-product can be estimated. A similar strategy can be applied to analyze differences in the intracellular flux distributions for the various process phases, thus allowing the identification of potential bottle necks limiting the production flux.

9. Product Yield Prediction

A theoretical approach for accurate product yield prediction would reduce experimental efforts during the development of optimal production strains. It would radically boost the pace of the science of Metabolic Engineering. Traditionally, constraint-based methods have been used to asses the production potential of metabolic networks. By applying linear programming, it is possible to calculate the maximal theoretical product yield for a defined carbon source and a given metabolic network (refer to Chapter 7). However, this metric only serves as a maximal bound for product yield and does not always represent an adequate proxy for experimental product yield. This is especially true when it comes to describing the production performance of strains in early development stages (refer to Table 2 in [50]).

Here, a kinetic-based approach was *applied* to predict experimental yields of six different semi-batch processes. The method is based on the EM approach and was introduced by the group of James Liao [71]. It requires three inputs: a metabolic network, a reference flux distribution and a rate law for each reaction. Unknown kinetic parameters are sampled so that the provided reference flux distribution is fulfilled. We observed that this method predicted experimental yields more accurately than its ad hoc constraint-based counterpart. Since labeling data for the semi-batch experiments were lacking, reference flux distributions were estimated using constraint-based methods along with two different objective functions: minimization of oxygen uptake and minimization of citrate synthase activity. We observed a dependence of calculated yield values on the reference flux distribution. However, regardless of the objective function used, predictions made by the kinetic-based method were by up to two orders of magnitude more accurate than the constraint-based method. We also adjusted traditionally used E. coli metabolic reconstructions [106, 107], making them suitable inputs for the EM approach. Finally, we used the COBRA Toolbox [124] to create required Matlab structures for the EM approach [70, 71, 74, 144, 146]. Thus, we created a missing bridge between widespread constraint-based and emerging kinetic modeling platforms [91].

9.1. Strain & Experimental Data

Experimental data used correspond to experimental taxadiene yields obtained for the six semi-batch fermentations introduced in Chapter 8. Taxadiene yields shown in Table 9.1 were calculated as the ratio of taxadiene production rate to glucose uptake rate for each of the two production phases. Biomass yields were calculated analogously, as the ratio between growth rate in each phase and corresponding glucose uptake rate. Refer to Section 8.1 and Table 8.2 for a description of experimental set-up and rates determination.

Since taxadiene production ceased during the second phase (between G2p and process end) for the majority of the fermentations (batches 1, 3, 4, 6), we will focus our analysis on the

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Table 9.1.: Biomass and Product Yields for Six Semi-Batch Fermentations. Biomass and Product yields are calculated for all phases. Yields are calculated as the ratio between taxadiene secretion rate (or growth rate) and glucose uptake rate. When calculating biomass yield, glucose uptake rate should be converted to units of g/gDW h.

| Batch ID | Bio | mass Yield [g | Txd Yield [mol/mol] | | |
|----------|------------------------|------------------------|------------------------|------------------------|----------------------|
| Daten ID | 1 Phase | 2 Phase | 3 Phase | 1 Phase | 2 Phase |
| 1 | 3.758×10^{-1} | 3.413×10^{-1} | 7.875×10^{-2} | 7.313×10^{-5} | 0.000 |
| 2 | 5.061×10^{-1} | 2.644×10^{-1} | 6.701×10^{-3} | 1.159×10^{-4} | 4.438×10^{-5} |
| 3 | 2.585×10^{-1} | 2.296×10^{-1} | 5.274×10^{-2} | 2.968×10^{-4} | 0.000 |
| 4 | 5.064×10^{-1} | 6.633×10^{-2} | 1.119×10^{-2} | 3.270×10^{-5} | 0.000 |
| 5 | 5.328×10^{-1} | 2.601×10^{-1} | 1.031×10^{-1} | 2.702×10^{-4} | 7.657×10^{-5} |
| 6 | 3.143×10^{-1} | 1.775×10^{-1} | 6.003×10^{-2} | 2.987×10^{-4} | 0.000 |

Table 9.2.: Average Biomass and Product Yields for Four Different Production Temperatures. Yields were calculated for the respective phases after system induction. Yield values for 16°C were calculated from average values of batches 1 and 2, while yield values for 22°C were calculated from batches 3 and 5. Errors correspond to one standard deviation. Since for production temperatures of 27 and 37°C only one single data set was available, no errors can be reported.

| Temperature | Average Biomass Yield | Average Product Yield |
|-------------|---|---|
| [°C] | $[\mathbf{g}/\mathbf{g}]$ | [mol/mol] |
| 16 | $3.029 \times 10^{-1} \pm 5.434 \times 10^{-2}$ | $9.451 \times 10^{-5} \pm 3.024 \times 10^{-5}$ |
| 22 | $2.449 \times 10^{-1} \pm 2.157 \times 10^{-2}$ | $2.835 \times 10^{-4} \pm 1.88 \times 10^{-5}$ |
| 27 | 1.775×10^{-1} | 2.987×10^{-4} |
| 37 | $6.633	imes10^{-2}$ | 3.270×10^{-5} |

first taxadiene production phase (refer to Figures 8.2 and 8.3 for phase definition). Table 9.2 shows the average taxadiene and biomass yield calculated for the respective phases after system induction. Yield values for 16°C were calculated from batches 1 and 2, while yield values for 22°C were calculated from batches 3 and 5.

9.2. Constraint-based Product Yield Prediction

Constraint-based modeling can be applied to calculate maximal theoretical product yields for various carbon sources and genotypes, as already shown in Chapter 7. Due to the simplicity of its calculation, maximal theoretical yield has been traditionally used to assess and compare production potential under a variety of conditions. We start our analysis by calculating maximal theoretical product yield for all six available data sets (corresponding to four production temperatures) using experimentally measured growth and substrate uptake rates (refer to Table 8.2) as constraints. The calculations were performed using an expanded version of the *E. coli* core model (refer to Appendix B.1.1) as follows:

- 1. Select one of the six data sets.
- 2. Constraint the *E. coli* core model by setting numerical values of upper and lower bounds of the growth and substrate uptake reactions to match experimentally measured rates. Refer to Table 8.2 for rate values.



Figure 9.1.: Constraint-based Product Yield Prediction. Model used for constraint-based product yield calculations was a modified version of the *E. coli* core model. The model was constrained by setting growth and glucose uptake rates to corresponding experimental values. Maximal theoretical yield was calculated using linear optimization.

- 3. Maximize flux through the taxadiene export reaction using linear programming.
- 4. Calculate taxadiene yield as the ratio between production flux calculated in the previous step and experimentally measured substrate uptake rate.

Figure 9.1 compares experimental product yields with maximal theoretical product yields. As it can be observed in the figure, *in silico* predictions differ by up to four orders of magnitude from the experimental target yield.

9.3. Kinetic-based Product Yield Prediction

A kinetic-based approach was used to calculate the so-called KAY [71]. KAY is defined as the maximal production flux that can be drawn from the host metabolic system before the metabolic system becomes unstable or the intracellular concentration of any metabolite in the system becomes negative. Dynamic system stability is evaluated by checking the eigenvalues of the system Jacobian matrix. Refer to [71] or Section 2.3.1 for details. Assuming that production performance of the strain under consideration is mostly constrained by kinetic stability issues, KAY should be a suitable proxy to describe observed experimental yields. The mathematical definition of KAY implies that its numerical value depends on the model kinetic structure used to simulate the host metabolism and on its associated parameters. Since both model structure and kinetic parameters are normally unknown, KAY can be calculated for an ensemble of kinetic models, built using the EM approach. Consequently, KAY will not have a unique numerical value but will rather be constrained into a range of probable values.

Here, we will assess the suitability of KAY to predict experimental product yield for six semi-batch data sets. In a first step, an ensemble of models describing a given reference flux distribution is built. Due to the process set-up used to generate experimental data,

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growth and substrate uptake rates after system induction correspond to the most suitable experimental information to generate corresponding reference flux distributions by using linear optimization. For that, two different objective functions were minimized: oxygen uptake rate and citrate synthase activity. Both objective functions aim to describe a cellular phenotype with limited respiratory capacity. The rationale behind the selection of these objective functions is justified by experimental observations performed when analyzing heterologous gene expression in $E. \ coli$, as discussed in Chapter 4. For each reference flux distribution, an ensemble of 1000 kinetic models is built and KAY is calculated for each model in the ensemble. For each ensemble, calculated KAY values are characterized by 25th and 75th percentiles and a median value. The procedure can be summarized as follows:

- 1. Select one of the six data sets.
- 2. Constraint the *E. coli* core model by setting numerical values of upper and lower bounds of the growth and substrate uptake reactions to match experimentally measured rates. Refer to Table 8.2 for rate values.
- 3. Generate two reference flux distributions by minimizing either oxygen uptake rate or citrate synthase activity.
- 4. For each reference flux distribution, apply the EM approach to build an ensemble of 1000 models.
- 5. Calculate KAY values for each ensemble as described in Section 2.3.1.
- 6. Characterize results by providing 25th and 75th percentiles and a median KAY value.

Figure 9.2 shows product yield predictions via KAY for all data sets and two objective functions. For both objective functions, experimental product yields (see Table 9.1) are within calculated ranges for KAY values in four out of six data sets. However, incorrectly predicted product yields are different for each objective function. Considering both cases simultaneously, KAY has the *potential* to correctly predict five out of six experimental product yields. The maximal discrepancy between calculated KAY values and experimental product yields does not exceed one order or magnitude. By contrast, product yield prediction using maximal theoretical yield differed by up to four orders of magnitude from the experimental target yield.

9.4. Application of KAY to Predict Optimal Biomass Yield During Production

So far, the application of KAY has been limited to predict experimental product yields in engineered strains [71]. Here, we explore further applications by using the KAY concept to analyze the effect of biomass yield on production performance. This analysis was partly motivated by the dependence between product and biomass yield shown in Figure 9.3.A. There, a biomass yield seems to exist, for which product yield is maximal. Even though the effect of varying temperatures on the observed product-biomass yield behavior can not be completely ruled out, it is still interesting to compare *in silico* predictions made by both constraint- and kinetic-based approaches.



Figure 9.2.: Kinetically Accessible Yield (KAY) for Experimental Product Yield Prediction. A. KAY for minimization of oxygen uptake rate as objective function. B. KAY for minimization of citrate synthase activity as objective function.

We start our analysis by analyzing predictions made by the traditionally used constraintbased approach. We used a modified version of the E. coli core model for all calculations (refer to Appendix B.1.1), with glucose uptake rate set to 10 mmol/gDW h. Maximal theoretical product yields supported by the network were calculated while simultaneously considering cellular growth as an additional constraint. Growth rates ranged from 0 to 0.6 h^{-1} . Results are represented in Figure 9.3.B by the orange line. As shown in the Figure, the higher the growth rate (biomass yield), the lower the maximal theoretical yield. In other words, if product yield is to be maximized, cells should be prevented from growing. Such predictions will always be obtained when analyzing the effect of cellular growth on the theoretical maximal product yield using constraint-based methods. The rationale behind it is simple. Since constraint-based methods only considers mass balances, any flux increase of a competing reaction (growth in this case) will necessarily lead to a decrease in the production flux (and product yield), if the substrate uptake rate is kept constant. Comparing this prediction with experimental observation shown in Figure 9.3.A, we conclude that it qualitatively describes experimental data only after the maximal product yield is reached (for biomass yields higher than 0.2 g/g). While the constraintbased approach suggests that the maximal product yield should be reached at a biomass yield of zero (Figure 9.3.A), experimental maximal product yield is clearly reached at a non-zero biomass yield (Figure 9.3.B).

Now, we turn our attention to the application of KAY to predict the dependence of product yield on biomass yield. In order to keep predictions of both methods (constraint- and kinetic-based) comparable, we used the same *E. coli* core model to generate an ensemble of models, for which KAY is calculated. Reference flux distributions were generated by minimizing oxygen uptake rate, while keeping substrate uptake rate at a constant value of 10 mmol/gDW h. Growth rates were varied between 0 and 0.6 h⁻¹. Refer to Seccion 2.3.1 for details on mathematical and computational implementation of KAY. Results are represented in Figure 9.3.B by blue diamonds. There are three aspects in which the prediction of the product yield vs. biomass yield relationship using a kinetic-based approach fundamentally differs from the prediction made by the already discussed constraint-based approach. First, the order of magnitude of the calculated KAY values is dramatically lower



Figure 9.3.: Dependence of Maximal Product Yield on Biomass Yield Model used was a modified version of the *E. coli* core model. Glucose uptake rate was set to 10 mmol substrate/gDW h for all calculations. A. Experimentally observed dependence. B. In silico calculated dependence using a constraint based approach (orange line) and the KAY method (data points in blue). Error bars correspond to 25th and 75th percentiles. Diamonds correspond to median KAY of the respective ensemble.

than maximal theoretical product yields and is therefore more in line with experimental product yields (refer to Figure 9.3.A). Second, the kinetic-based approach predicts the maximal product yield to be located at a non-zero biomass yield of 0.11 g/g, surprisingly close to the location of the maximal experimental product yield 0.17 g/g, especially considering that no experimental information was used to generate reference flux distributions. Third, the predicted relationship between product yield and biomass yield using the kinetic-based method shows a non-linear trend, similar to the experimentally observed behavior. In contrast, the constraint-based method predicted a linear relationship between these two quantities. Overall, the consideration of a kinetic layer seems to improve the prediction capabilities of the stoichiometric model, even though exact reference flux distributions and corresponding parameter values were unknown.

9.5. Discussion

In Section 9.3, we successfully applied a kinetic-based approach to predict experimental product yields of a semi-batch process. Exchange rates (growth and substrate uptake rate) during production phase (after system induction) were used along with two different objective functions to generate reference flux distributions needed to construct an ensemble of models and subsequently calculate KAY values. We observed a dependence of calculated KAY values on the used reference flux distribution (see Figure 9.2). This highlights the importance of using appropriate reference flux distributions to obtain accurate product yield predictions. Since unambiguous determination of reference flux distributions is in many cases not possible due to technical or economical limitations (refer to Section 2.1.2), an interesting, yet unexplored possibility is the consideration of an ensemble of ensembles. Representative reference flux distributions (each used to populate one ensemble) can be generated by either assuming different (biologically relevant) objective functions, as done in



Figure 9.4.: Increasing the Utility of the KAY Concept The concept of proteome partitioning can be used to calculate the vector of enzyme concentrations after system (plasmid) induction (E_f) . By integrating Equation 2.25 between E_0 and E_f , the vector of steady state metabolite concentrations can be calculated. This vector can be used in a subsequent step to calculate the corresponding flux distribution, which can be in turn used as input for a KAY analysis. Note that in the wild-type strain (pie chart on left side of this figure), the fraction of heterologous protein U amounts to zero. However, it is represented in the pie chart to symbolize that this fraction gains importance as the induction level is increased.

Section 9.3, or by simply covering to some extent the space of mathematically feasible flux distributions by sampling free (independent) fluxes (see Equation 2.18). In a second step, all ensembles are merged into one single ensemble and one single prediction is generated. Clearly, this approach would necessary require the implementation of computer clusters and an efficient parallelization strategy. The approach presented in Figure 2.6.B could be used as an initial cluster set-up.

Typically, experimental information regarding growth and substrate uptake rates during the production phase are unavailable. However, these data are normally known for uninduced strains or wild-types. In order to increase the utility of KAY calculations, the procedure used in Section 9.3 can be extended to allow for product yield prediction starting directly from the wild-type phenotype. In the original paper, Lafontaine Rivera et al. [71] used this idea. Starting from an estimated flux distribution for the wild-type, they successfully predicted the isobutanol yield for three different strains, one of which exhibited three different gene deletions ($\Delta adhE$, Δpta and Δldh). In order to assess the production potential of that strain, the effect of gene deletions on the flux distribution was first assessed. Then, a KAY analysis was performed using only models that retained stability after mathematically knocking out the three genes. The calculated KAY value was consistent with the experimentally determined yield. A similar approach could be applied to estimate the production potential of highly burdened strains. The idea is simple and is motivated by the concept of proteome partitioning developed by the Hwa group at UC, San Diego [132–134]. Consider the pie chart shown on the left side of Figure 9.4. The proteome partitioning model introduced by Hwa and coworkers assumes that the microbial proteome can be split into three different sectors: Q, P and R. Sector Q is fixed and does not depend

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on the cellular growth rate. R contains all ribosomal proteins and their affiliates, while P represents all proteins responsible for nutrient influx and metabolism. Since the size of the proteome is limited, the expression of an heterologous protein U effectively decreases the fraction allocable to the P and R sectors, as represented in the pie chart on the left side of Figure 9.4. If functions describing the fraction of sectors P (ϕ_P) and R (ϕ_R) in dependence of the heterologous fraction U (ϕ_U) are known, then it should be possible to estimate changes in the flux distribution as ϕ_U increases. For a given ϕ_U fraction, KAY values can be then calculated using the calculated flux distribution as a starting point (V_f in Figure 9.4) [91].

The results and outlook presented in this chapter evidences the huge potential of kineticbased modeling, more specifically, of EM-based methods. In our opinion, Figures 9.3 and 9.2 directly support the predictive power of EM-based methods like KAY itself and optEM (see Section 5.4.2). Additional experimental work, including measurements of protein content in both wild-type and induced strains, will be required to further extend and validate the applicability of KAY as proposed in Figure 9.4. An interesting prediction of KAY is the interdependence between biomass and product yield, shown in this Chapter (see Figure 9.3) but also in Chapter 6 (refer to Figure 6.10.B). The validity of this relationship and the ability of KAY to successfully describe it could be exploited not only for the optimal design of fermentation processes but also for the calculation of optimal induction levels, described by the fraction of heterologous protein ϕ_U .
10. Concluding Remarks and Outlook

The coverage of this thesis is mostly limited to the taxadiene production in *E. coli*. However, a review on the application of computational methods to increase succinate production in engineered strains evidenced interesting trends of the current model-based, *rational* Metabolic Engineering. Even though the details of that review can be found elsewhere [149], we will highlight some of the key lessons learned from that review in order to understand the way how it motivated and guided parts of the *in silico* studies presented here. Then, we will provide some conclusions and future perspectives concerning the main results of this work.

10.1. Lessons From Succinate Production in Engineered Strains

Biotechnological production of succinate has been one of the preferred case studies to test predictions made by strain-design algorithms. Since the introduction of OptKnock in 2003 and until 2016, a total of 26 different strain-design algorithms *in silico* targeting the succinate overproduction (refer to Table 1 in [149] or Table 2.4 of this work) have been published. None of these studies was accompanied by an *in vivo* validation of the algorithm's predictions. Rather, the rich biological knowledge available, gained over decades of research in succinate production in a variety of industrially relevant microorganisms, was used to test the predictive power of the algorithms. An analysis of the nature of mathematical methods used to develop these strain-design algorithms and the way how their predictions are used to guide *in vivo* strain development leads to three key conclusions:

- 1. Constraint-based methods predominate. Roughly 80% of the 26 strain-design algorithms targeting succinate overproduction have a constraint-based nature. This observation is not surprising and is, in our opinion, mainly justified in the relative simplicity of its mathematical formulation, availability of the required information (a genome-scale metabolic reconstruction and an objective function), and its computational tractability.
- 2. *Kinetic-based methods are underrepresented.* Contrasting the predominance of constraintbased methods, only one single method, out of 26 strain design algorithms reviewed, had a kinetic-based nature. In our opinion, this evidences the difficulties associated with kinetic descriptions of cellular metabolism. In addition to a stoichiometric layer, kinetic information in form of rate laws, describing the flux through each reaction as a function of enzyme-specific parameters and metabolite concentrations, are also required. Since this information is typically unavailable, the construction of large-scale kinetic models have been hindered.

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3. In silico predictions are not always precise. We found out that only 10 studies reported the model-guided construction of strains exhibiting an enhanced succinate production (refer to Table 2 in [149]). Within these studies, only two used one of the 26 strain-design algorithms previously developed. All other studies reported the construction of production strains based on knowledge gained from FBA calculations. Additionally, none of the 10 studies reported an exact implementation of *in silico* predictions. Often, complementary strategies like directed evolution were necessary to achieve high succinate yields. Altogether, these observations point to a limited predictive power of constraint-based methods, especially when aspects like fine tuning of enzyme expression or dynamic stability of the system become important factors determining the effectiveness of a given genetic intervention [1,2].

10.2. Lessons From Taxadiene Production in E. coli

As previously mentioned, advantages of constraint-based methods over kinetic-based methods include the simplicity of use, while simultaneously offering a moderate predictive power. Due to their computational tractability, constraint-based simulations can be performed on a large-scale, thus allowing the identification of non-trivial network properties. In the specific case of taxadiene production in *E. coli*, we demonstrated that a carbon-neutral taxadiene production is not possible for any substrate or substrate mixture. This observation can be easily extended to the production any terpene. This is because carbon leak in form of CO_2 is concomitant to the formation of both IPP and DMAPP, the universal terpene precursors, via either the mevalonate or the non-mevalonate pathway. Additionally, our large-scale constraint-based analysis pointed at a synergy between the mevalonate and the non-mevalonate pathway *in silico* (**Chapter 7**). Remarkably, this synergy was experimentally observed, although in a greater extent, for the production of isoprene in *E. coli* [160].

The predictive power of constraint-based modeling is increased, if biologically meaningful constraints are used. In **Chapter 4**, we applied a constraint-based approach to simulate the experimentally observed effect of protein load on by-product secretion. By reducing the upper boundary of oxygen uptake rate as protein/plasmid load increases, we could qualitatively reproduce the downwards shift of the acetate line experimentally observed in loaded strains. Our assumption on decreasing respiratory capacity is in part justified by proteomic measurements reported by Peebo et al. [110].

One of the main disadvantages of constraint-based methods, which paradoxically has its origin in the simplicity of the mathematical formulation of constraint-based approaches, is the omission of enzyme kinetics. As a consequence, important aspects such as dynamic stability of the cellular metabolism, intracellular concentration of potentially toxic metabolites, metabolite-level enzyme regulation and fine tuning of enzyme expression cannot be adequately considered. By contrast, multiple studies have highlighted the importance of at least one of these factors for the construction of terpenoids overproducing strains [1,2,38]. Motivated by this and by the fact that kinetic-based models are underrepresented despite of their application potential in rational Metabolic Engineering, we ventured to explore the utility of the ensemble modeling, an emerging approach for the construction and analysis of kinetic models. The predictive power of the ensemble modeling approach was evaluated in Chapter 5 and 9. Even though kinetic parameters were sampled and reference flux distributions were calculated by means of constraint-based modeling using two experimental exchange rates, namely growth and substrate uptake rate, predicted taxadiene yields using the concept of KAY [71] agreed remarkably well with experimental data (Chapter 9). Additionally, predicted targets by our EM-based strain-design algorithm optEM for increased taxadiene production were in line with known, reported beneficial genetic perturbations (Chapter 5). We also observed an interesting dependence of experimental taxadiene yields on biomass yields, which, to the best of our knowledge, has not been described before. Interestingly, this dependence could be reproduced using the concept of KAY. In Chapter 6, we observed the same dependency for strains exhibiting varying levels of % Carbon Xylose. We combined these predictions and the fact that biomass yield is likely to decrease (as genetic elements necessary for taxadiene production should increase the metabolic burden) to suggest that strain HMS p1x represents the best production strain candidate for further optimization rounds.

Even though the ensemble modeling approach showed an unexpectedly high predictive power and utility, its widespread in the community has been hindered, possibly by its high computational burden. Clearly, this represents a challenge for small research facilities, as computer clusters do not belong to standard equipment. As discussed in Chapter 5, computational power can be reduced by increasing the amount of experimental information used to define and characterize the reference state required to populate the ensemble of kinetic models. A related issue is the existence of alternative flux distributions equally fulfilling constraints imposed by experimentally determined exchange rates or available ¹³C-labeling data. The dependence of KAY predictions on the reference flux distribution is exemplary shown in Figure 9.2, Chapter 9. An option to deal with this additional uncertainty source is to sample the space of possible flux distributions and to perform the desired ensemble modeling-based analysis (KAY [71], EMRA [74, 144] or OptEM) independently. Then, the collective response can be characterized as usual, by providing 25th and 75th percentiles for the whole ensemble of ensembles. Certainly, this imposes an even higher computational burden. Therefore, an optimal trade-off between uncertainty and degree of experimental characterization should be individually found according to equipment availability.

We envision the spectrum of ensemble modeling-related methods and applications to keep widening. For instance, KAY could be used as a soft sensor, calculated in real-time from online OD, substrate and oxygen concentration measurements. This is especially useful when online experimental determination of product concentrations is not possible. By using KAY as an accurate proxy for strain performance, it should be possible to dynamically adjust process conditions such as stirrer velocity, substrate feeding and process time to maximize production and profit. Further potential applications include combination of the ensemble modeling approach with dynamic flux balance analysis for identification of strain designs with increased productivity [170] and guidance while experimentally constructing instability-prone genotypes [2].

High quality, reproducible experimental data play a crucial role in the efficient development and validation of modeling approaches and more broadly, in the advance of science. Nowadays, reproducibility issues do not represent the incapacity of isolated research groups to reproduce own or other group's results, but rather a generalized problem affecting the whole research community, with an extent depending on the specific research field [9,99]. In

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this work, model-based improvement strategies for strains (Chapter 4 & 5) and a production process (Chapter 8) were identified. Unfortunately and due to reproducibility issues, none of these strategies could be validated. This limited the experimental implementation of the theoretical workflow developed (refer to Chapter 3) and hindered the desired optimization of strains and their associated production processes through the implementation of model-based predictions in an iterative fashion. However, various theoretical methods for each of the steps of the workflow were developed and applied. Figure 10.1 provides an overview of these methods and summarizes relevant input-output relationships used along this work.

Chapter 6 was concluded by suggesting strain HMS p1x as an optimal production strain candidate. After genetic elements allowing terpenoid production are introduced into this strain, modifications in its metabolism leading to an increased production performance can be identified by applying the tools discussed in **Chapter 5**. Once the desired production performance has been reached, associated optimal process parameters can be identified as shown in **Chapter 8**. As for culture medium composition, a similar procedure to the one used in **Chapter 7** can be applied to identify promising carbon sources. These steps are illustrated in Figure 10.1 by the dashed lines and represent one possible implementation of the workflow using all tools described in this work.

Two opposite approaches have been suggested to increase reproducibility of results, namely standardization [111] and heterogenization of experimental conditions [116]. In either case, future experimental efforts should aim to keep increasing confidence in experimental data. On the modeling side, strategies should be developed to properly handle uncertainties and experimental error, thus allowing the generation of predictions that are robust to noise.



Figure 10.1.: Application of the Workflow to the Production of Taxadiene in *E. coli*: Conclusion. The proposed workflow, covering both model-guided strain engineering and model-driven process optimization, was applied to the production of taxadiene in *E. coli*. Even though model-based optimization strategies for strain and production process could not be experimentally validated due to reproducibility issues of experimental data, we demonstrated the utility of a variety *in silico* approaches. Refer to each chapter for more details. Main input-output relationships are shown for each chapter. Applied methods are given in boxes. Dashed lines represent further steps towards the construction of an optimal terpenoid producing strain and the optimization of its performance in a bio-reactor.

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Acronyms

¹³C-MFA ¹³C-Metabolic Flux Analysis.

 $[U^{-13}C]$ uniformly labeled ¹³C.

E. coli Escherichia coli.

CCR Carbon Catabolite Repression.

dFBA dynamic Flux Balance Analysis.

DMAPP dimethylallyl diphosphate.

EM Ensemble Modeling.

EMRA Ensemble Modeling for Robustness Analysis.

EMU Elementary Metabolite Units.

FBA Flux Balance Analysis.

FVA Flux Variability Analysis.

G3P glyceraldehyde 3-phosphate.

 ${\bf GA}\,$ Genetic Algorithm.

 $\ensuremath{\mathsf{GDP}}$ Gross Domestic Product.

gDW gram dry weight.

HPLC High Performance Liquid Chromatography.

i.e. id est.

IPOPT Interior Point OPTimizer.

IPP isopentenyl diphosphate.

IPTG Isopropyl β -D-1-thiogalactopyranoside.

KAY Kinetically Accessible Yield.

A cronyms

MEP non-mevalonate.

mmol millimol.

 ${\sf MS}\,$ Mass Spectromety.

 $\ensuremath{\mathsf{MVA}}$ mevalonate.

NGAM Non-growth Associated Maintenance.

 ${\sf NMR}\,$ Nuclear Magnetic Resonance.

 $\boldsymbol{\mathsf{OD}}$ Optical Density.

PTS phosphotransferase system.

 $\ensuremath{\mathsf{RAM}}$ Random Access Memory.

 ${\bf rpm}\,$ revolutions per minute.

SBT Fachgebiet Systembiotechnologie.

 $\ensuremath{\mathsf{SLURM}}$ Simple Linux Utility for Resource Management.

TCA tricarboxylic acid.

UC University of California.

WT wild-type.

A.1. Metabolic Burden

A.1.1. Slope of Acetate Line

The slope of experimental acetate lines was determined for three different strains, namely strain 31, 3150 and 3152. Refer to Table 4.1 for strain description. For strain 31, three different data sets were available for the determination of its slope. Slope of acetate lines was determined using standard linear least square regression for both growth rate as a function of acetate and acetate as a function of growth rate, as shown in Figure A.1. Since experimental acetate secretion rates normally exhibit higher standard deviations than growth rates (refer to Figure 5.2 and 6.11), the slope of the lines acetate vs growth rate is considered to describe more accurately the slope of the acetate lines. Since strains 31, 3150 and 3152 differ only by its metabolic load, the slope of their acetate lines should be constant [11]. The average slope considering all acetate lines correspond to: 28.063 ± 3.587 mol acetate/gDW



Figure A.1.: Determination of the Acetate Line Slope for *E. coli* HMS. Slope of acetate lines for strains 31, 3150 and 3152 were determined using linear regression for growth rate vs. acetate secretion rate (A.) and acetate secretion rate vs. growth rate (B.). Values for coefficient of determination were: $R_{31_1}^2 = 0.79$, $R_{31_2}^2 = 0.80$, $R_{31_3}^2 = 0.97$, $R_{3150}^2 = 0.92$, $R_{3152}^2 = 0.45$. y_{31_i} refers to the regression for one three different data sets. Symbols are as follows: +: acetate, \circ : fructose, *: galactose, \Box : glucose, \diamond : mannose.

A.1.2. Amino Acid Sequences

Protein sequences for eGFP, mCherry, antibiotic resistances and additional replication proteins are given below. The mCherry-plasmid contains: mCherry, kanamycine resistance and replication protein 237. The eGFP-plasmid contains: eGFP, gentamycine resistance, replication protein 648 and protein XylS. These protein sequences can be used to construct strain specific metabolic reconstructions.

Amino acid sequence for eGFP

 $\label{eq:structure} MVSKGEELFTGVVPILVELDGDVNGHKFSVSGEGEGDATYGKLTLKFICTTGKLPVPWPTLVTTLTYGVQCFSRYPDHMKQHDFFKSAMPEGYVQERTIFFKDDGNYKTRAEVKFEGDTLVNRIELKGIDFKEDGNILGHKLEYNYNSHNVYIMADKQKNGIKVNFKIRHNIEDGSVQLADHYQQNTPIGDGPVLLPDNHYLSTQSALSKDPNEKRDHMVLLEFVTAAGITLGMDELYK$

Amino acid sequence for mCherry

MVSKGEEDNMAIIKEFMRFKVHMEGSVNGHEFEIEGEGEGEGRPYEGTQTAKLKVTKGGPLPFAWDILSPQF MYGSKAYVKHPADIPDYLKLSFPEGFKWERVMNFEDGGVVTVTQDSSLQDGEFIYKVKLRGTNFPSDGPV MQKKTMGWEASSERMYPEDGALKGEIKQRLKLKDGGHYDAEVKTTYKAKKPVQLPGAYNVNIKLDITSH NEDYTIVEQYERAEGRHSTGGMDELYK

Protein sequence for kanamycine resistance

 $\label{eq:scsrprlnsnmdadlygykwardnvgqsgatiyrlygkpdapelflkhgkgsvandvtdem vrlnwltefmplptikhfirtpddawllttaipgktafqvleeypdsgenivdalavflrrlhsipvcncpf nsdrvfrlaqaqsrmnnglvdasdfdderngwpveqvwkemhkllpfspdsvvthgdfsldnlifdegk ligcidvgrvgiadryqdlailwnclgefspslqkrlfqkygidnpdmnklqfhlmldeff$

Protein sequence for gentamycine resistance

 $\label{eq:mlrssndvtqqgsrpktklggssmgiirtcrlgpdqvksmraaldlfgrefgdvatysqhqpdsdylgnllrsktfialaafdqeavvgalaayvlpkfeqprseiyiydlavsgehrrqgiatalinllkheanalgayviyvqadygddpavalytklgireevmhfdidpstat$

Protein sequence for replication protein 237

MATQSREIGIQAKNKPGHWVQTERKAHEAWAGLIARKPTAAMLLHHLVAQMGHQNAVVVSQKTLSKLIGRSLRTVQYAVKDLVAERWISVVKLNGPGTVSAYVVNDRVAWGQPRDQLRLSVFSAAVVVDHDDQDESLLGHGDLRRIPTLYPGEQQLPTGPGEEPPSQPGIPGMEPDLPALTETEEWERRGQQRLPMPDEPCFLDDGEPLEPPTRVTLPRR

Protein sequence for replication protein 648

 $\label{eq:spectral} MSNVASPPMVYKSNALVEAAYRLSVQEQRIVLACISQVKRSEPVTDEVMYSVTAEDIATMAGVPIESSYNQL KEAALRLKRREVRLTQEPNGKGKRPSVMITGWVQTIIYREGEGRVELRFTKDMLPYLTELTKQFTKYALA DVAKMDSTHAIRLYELLMQWDSIGQREIEIDQLRKWFQLEGRYPSIKDFKLRVLDPAVTQINEHSPLQVEW AQRKTGRKVTHLLFSFGPKKPAKAVGKAPAKRKAGKISDAEIAKQARPGETWEAARARLTQMP$

Protein sequence for protein XylS

MDFCLLNEKSQIFVHAEPYAVSDYVNQYVGTHSIRLPKGGRPAGRLHHRIFGCLDLCRISYGGSVRVISPGL ETCYHLQIILKGHCLWRGHGQEHYFAPGELLLLNPDDQADLTYSEDCEKFIVKLPSVVLDRACSDNNWHKP REGIRFAARHNLQQLDGFINLLGLVCDEAEHTKSMPRVQEHYAGIIASKLLEMLGSNVSREIFSKGNPSFERV VQFIEENLKRNISLERLAELAMMSPRSLYNLFEKHAGTTPKNYIRNRKLESIRACLNDPSANVRSITEIALDY GFLHLGRFAENYRSAFGELPSDTLRQCKKEVA

| Time | В | iomass, [g/ | /1] | Gala | actose, [mm | ol/l] | Acetate, [mmol/l] | | | |
|------|------------------|-------------|-----------|---------------|---------------|------------------------|-------------------|------------------------|------------------------|--|
| [h] | 31 3150 3152 | | | 31 | 3150 | 3152 | 31 | 3150 | 3152 | |
| 0 | 1.597E-02 | 1.903E-02 | 1.209E-02 | 2.346E + 01 | $2.391E{+}01$ | $2.302\mathrm{E}{+}01$ | NaN | NaN | 7.980E-01 | |
| 1.5 | 2.075E-02 | 1.930E-02 | 1.362E-02 | $2.322E{+}01$ | $2.202E{+}01$ | $2.150E{+}01$ | NaN | 7.191E-01 | 7.597E-01 | |
| 3 | 3.707E-02 | 3.004E-02 | 1.804E-02 | $2.088E{+}01$ | $2.309E{+}01$ | $2.129E{+}01$ | NaN | 8.542E-01 | 7.326E-01 | |
| 4.5 | 6.215E-02 | 3.806E-02 | 2.183E-02 | $2.076E{+}01$ | $2.101E{+}01$ | $2.125\mathrm{E}{+}01$ | NaN | $1.056\mathrm{E}{+00}$ | 8.901E-01 | |
| 6 | 1.043E-01 | 3.933E-02 | 1.894E-02 | $2.016E{+}01$ | $2.259E{+}01$ | $2.100\mathrm{E}{+}01$ | 7.349E-01 | $1.534\mathrm{E}{+00}$ | $1.061\mathrm{E}{+00}$ | |
| 7.5 | 1.710E-01 | 5.493E-02 | 2.462E-02 | 1.817E + 01 | 2.076E + 01 | 2.142E + 01 | 7.137E-01 | 1.823E + 00 | $1.205E{+}00$ | |

Table A.1.: Concentration Time Courses for Galactose as Carbon Source.

Table A.2.: Concentration Time Courses for Glucose as Carbon Source.

| Time | В | iomass, [g/ | [1] | Glu | icose, [mmo | 01/1] | Ac | etate, [mmo | Formate, [mmol/l] | |
|------|--------------|-------------|-----------|--------------|------------------------|------------------------|-----------|------------------------|------------------------|---------------|
| [h] | 31 3150 3152 | | | 31 3150 3152 | | 31 3150 | | 3152 | 31 | |
| 0 | 1.506E-02 | 1.858E-02 | 1.660E-02 | 2.298E+01 | $2.029E{+}01$ | $2.049E{+}01$ | NaN | NaN | 7.703E-01 | NaN |
| 1.5 | 2.697E-02 | 3.103E-02 | 2.291E-02 | 1.931E+01 | 1.877E + 01 | $1.907E{+}01$ | 7.026E-01 | 8.158E-01 | 7.973E-01 | NaN |
| 3 | 6.765E-02 | 2.904E-02 | 1.624E-02 | 1.819E+01 | $1.856E{+}01$ | $1.921E{+}01$ | 1.320E+00 | 9.096E-01 | 9.029E-01 | NaN |
| 4.5 | 1.410E-01 | 4.303E-02 | 2.435E-02 | 1.666E + 01 | $1.861E{+}01$ | 1.866E + 01 | 2.461E+00 | 1.164E + 00 | $1.080E{+}00$ | $5.730E{+}00$ |
| 6 | 3.114E-01 | 4.844E-02 | 3.292E-02 | 1.326E+01 | $1.885E{+}01$ | $1.903E{+}01$ | 4.919E+00 | $1.600E{+}00$ | $1.390E{+}00$ | $2.748E{+}01$ |
| 7.5 | 4.991E-01 | 4.221E-02 | 3.031E-02 | 6.482E+00 | $1.873\mathrm{E}{+}01$ | $1.899\mathrm{E}{+}01$ | 6.485E+00 | $1.855\mathrm{E}{+00}$ | $1.466\mathrm{E}{+00}$ | NAN |

A.1.3. Concentration Time Courses

Experimental time courses for biomass, substrate, acetate and formate for growth on different carbon sources (galactose, glucose, mannose, fructose and acetate) are shown in Tables A.1 to A.5. From these time courses, respective rates were calculated as explained in Section 2.1.2 and are listed in Table A.6. Note that formate was only detected for strain 31, when grown fructose, mannose and glucose.

A.1.4. Flux Distribution Patters for Three Zones

FVA results for Phase I, II and III are shown in Figures A.2 to A.4, respectively. The *E. coli* core model was used for all calculations. For each phase, glucose and oxygen uptake rate were set to defined values then, maximal growth rate was calculated. After fixing the growth rate to that value, minimal and maximal rates supported by each reaction in the model was calculated. Three rules were used to identify biologically feasible fluxes:

- 1. minFlux = maxFlux and minFlux = 0
- 2. minFlux == 0 and maxFlux > 900
- 3. abs(abs(minFlux)-abs(maxFlux))>900

reactions *not* fulfilling *any* of these rules are identified their flux ranges plotted for each phase. Note that in each phase, exchange reactions are highlighted in blue.

Time Biomass, [g/l] Mannose, [mmol/l] Acetate, [mmol/l] Formate, [mmol/l] [h] 31 3150315231 3150 315231 3150 315231 1.993E-02 1.696E-02 1.987E+01 2.054E+011.038E+002.580E-02 2.111E + 01NaN NaN NaN 1.5 $2.850\mathrm{E}\text{-}02$ 2.688E-02 1.741E-02 2.122E + 01 $2.053E{+}01$ $1.847\mathrm{E}{+}01$ 7.858E-01 7.244E-01 1.035E+00NaN 5.737E-02 4.131E-021.984E-021.861E + 01 $2.053E{+}01$ 1.839E + 011.217E + 007.244E-01 1.165E + 00NaN 3 4.266E-02 4.59.660E-02 2.237E-02 1.827E + 011.858E + 011.874E + 011.473E + 009.470E-01 1.312E + 00NaN 1.620E + 016 1.792E-01 5.619E-02 2.246E-02 $1.859E \pm 01$ $2.083E \pm 01$ $1.874E \pm 01$ 2.121E+00 1.755E+001.312E+001.949E + 005.358E-02 2.950E-02 $1.613E \pm 01$ 1.917E + 01 $1.819E \pm 01$ 1.913E + 001.405E+002.437E+01 7.52.859E-01

Table A.3.: Concentration Time Courses for Mannose as Carbon Source.

Table A.4.: Concentration Time Courses for Fructose as Carbon Source.

| Time | В | iomass, [g/ | /1] | Fru | ctose, [mmo | ol/l] | Ac | etate, [mmo | Formate, [mmol/l] | |
|------|------------|-----------------------------|-----------------------------|---------------|------------------------|------------------------|---------------|------------------------|------------------------|---------------|
| [h] | 31 | 31 3150 3152 31 3150 3152 | | 31 | 31 3150 | | 31 | | | |
| 0 | 1.497E-02 | 1.696E-02 | 7.487E-03 | $2.393E{+}01$ | $2.245E{+}01$ | $2.426E{+}01$ | NaN | NaN | 7.192E-01 | NaN |
| 1.5 | 2.517E-02 | 1.867E-02 | 9.471E-03 | 2.466E + 01 | $2.378E{+}01$ | $2.151E{+}01$ | 9.693E-01 | 7.371E-01 | 7.626E-01 | NaN |
| 3 | 3.906E-02 | 2.426E-02 | 1.191E-02 | 2.147E + 01 | $2.180E{+}01$ | $2.198E{+}01$ | 1.102E+00 | 9.476E-01 | 7.957E-01 | NaN |
| 4.5 | 8.966E-02 | 3.346E-02 | 1.768E-02 | $2.014E{+}01$ | 2.166E + 01 | $2.196E{+}01$ | $1.539E{+}00$ | $1.275E{+}00$ | 9.296E-01 | NaN |
| 6 | 1.648E-01 | 3.987E-02 | 1.705E-02 | $1.694E{+}01$ | $2.302E{+}01$ | 2.121E + 01 | 2.526E + 00 | 2.231E + 00 | $1.055E{+}00$ | $1.683E{+}01$ |
| 7.5 | 2.787 E-01 | $4.970\mathrm{E}\text{-}02$ | $2.345\mathrm{E}\text{-}02$ | $1.429E{+}01$ | $2.113\mathrm{E}{+}01$ | $2.206\mathrm{E}{+}01$ | 3.652E + 00 | $1.797\mathrm{E}{+00}$ | $1.224\mathrm{E}{+00}$ | $2.798E{+}01$ |

Table A.5.: Time Courses for Acetate as Carbon Source.

| Time, | В | $\overline{\mathbf{biomass}}, [\mathbf{g}]$ | ′l] | Acetate, [mmol/l] | | | | | | |
|-------|-----------|---|-----------|-------------------|------------------------|------------------------|--|--|--|--|
| [h] | 31 | 3150 | 3152 | 31 | 3150 | 3152 | | | | |
| 0 | 1.335E-02 | 1.696E-02 | 1.146E-02 | $2.235E{+}01$ | $2.357E{+}01$ | $2.122E{+}01$ | | | | |
| 1.5 | 1.633E-02 | 1.488E-02 | 1.795E-02 | $2.192E{+}01$ | $2.139E{+}01$ | $2.008\mathrm{E}{+}01$ | | | | |
| 3 | 2.426E-02 | 1.858E-02 | 1.479E-02 | $1.926E{+}01$ | $2.026\mathrm{E}{+}01$ | $2.000E{+}01$ | | | | |
| 4.5 | 3.310E-02 | 1.732E-02 | 1.786E-02 | $1.859E{+}01$ | $2.034E{+}01$ | $1.973E{+}01$ | | | | |
| 6 | 4.221E-02 | 1.885E-02 | 1.651E-02 | $1.720E{+}01$ | $2.037E{+}01$ | $1.928E{+}01$ | | | | |
| 7.5 | 6.621E-02 | 1.831E-02 | 2.318E-02 | $1.492E{+}01$ | 2.048E + 01 | 1.940E + 01 | | | | |

Table A.6.: Exchange Rates for Three Strains and Five Sugars. Rates for growth, substrate uptake and acetate secretion were calculated from measured time courses as described in Chapter 2.1.2

| | Glucose | | | Mannose | | | Fructose | | | Galactose | | | Acetate | | |
|---------------|---------|--------|-------|---------|-------|-------|----------|-------|--------|-----------|-------|-------|---------|-------|-------|
| | | Strain | | Strain | | | Strain | | | Strain | | | Strain | | |
| | 31 | 3150 | 3152 | 31 | 3150 | 3152 | 31 | 3150 | 3152 | 31 | 3150 | 3152 | 31 | 3150 | 3152 |
| μ | 0.487 | 0.111 | 0.086 | 0.384 | 0.112 | 0.054 | 0.402 | 0.152 | 0.150 | 0.328 | 0.146 | 0.090 | 0.213 | 0.019 | 0.066 |
| r_{uptake} | 14.111 | 4.449 | 4.540 | 5.433 | 3.353 | 3.619 | 15.198 | 6.249 | 12.643 | 10.103 | 9.248 | 8.814 | 29.668 | 7.829 | 8.967 |
| $r_{acetate}$ | 6.074 | 4.707 | 3.336 | 1.670 | 4.905 | 1.755 | 4.324 | 6.432 | 4.734 | - | 4.825 | 2.655 | - | - | - |

 μ is given in 1/h; both substrate uptake (r_{uptake}) and acetate secretion ($r_{acetate}$) rates are given in mmol/gDW h. '-' symbolizes that no acetate secretion was detected.



Figure A.2.: Flux Variability Analysis for Phase I. Upper boundary for glucose and oxygen uptake rates were set to 0.75 and 4 mmol/gDW h, respectively. CO₂ is the only carbon-based by-product secreted by the cell.



Figure A.3.: Flux Variability Analysis for Phase II. Upper boundary for glucose and oxygen uptake rates were set to 2 and 4 mmol/gDW h, respectively. CO₂ and acetate represent carbon-based by-products secreted by the cell.



Figure A.4.: Flux Variability Analysis for Phase III. Upper boundary for glucose and oxygen uptake rates were set to 4 and 4 mmol/gDW h, respectively. CO₂, acetate and formate represent carbon-based by-products secreted by the cell.



Figure A.5.: Non-Mevalonate Pathway (MEP). The non-mevalonate pathway consists of 8 different reactions. This pathway converts pyruvate and glyceraldehyde 3-phosphate into the universal isoprenoid precursors dimethylallyl diphosphate and isopentenyl diphosphate. All metabolite's figures were taken from KEGG [103]

A.2. Strain Design Algorithms for Target Identification

A.2.1. Mevalonate, Non-Mevalonate & Taxadiene Formation Pathways

Terpenes are naturally synthesized compounds formed by the ligation of activated isoprene molecules IPP and its isomer DMAPP. In nature, IPP and DMAPP can be synthetized through two different metabolic routes: the mevalonate (MVA) or the non-mevalonate (MEP) pathway. Figures A.5, A.6 and A.7 schematically show the non-mevalonate, the mevalonate and the taxadiene production pathways, respectively.

A.2.2. Concentration Time Courses for Taxadiene Producing Strains

Table A.7 summarizes time courses for OD, glucose and acetate concentration for five different strains. Concentrations were measured in duplicate.

A.2.3. ${}^{13}C$ Labeling Data

Table A.8 provides labeling patterns for protein-bound amino acids for five different taxadiene producing strains. Measurements were kindly provided by Claudia Huber at **Bio**

A.2. Strain Design Algorithms for Target Identification



Figure A.6.: Mevalonate Pathway (MVA). The mevalonate pathway consist of 7 different reactions. This pathway converts three molecules of acetyl-coA into one molecule of isopentenyl diphosphate (IPP). Dimethylallyl diphosphate is produced via isomerization of IPP. All metabolite's figures were taken from KEGG [103]



Figure A.7.: **Taxadiene Production Pathway.** Three molecules of isopentenyl diphosphate and one molecule of dimetylallyl diphosphate are converted in a serie of four reactions into taxadiene -a diterpene-. All metabolite's figures were taken from KEGG [103]

OD Glucose, [mmol/l] Acetate, [mmol/l] Time, [h] 2 1 $\mathbf{2}$ 1 2 HMS 2p 0 0.5740.58225.186 38.874 0.512 0.648 0.644 2.0980.65015.40736.6650.9401 3 0.8940.903 19.17313.0761.9591.7671.188 5.7470.868 1.11323.57428.18451.39271.37421.48920.2488.232 6.831 $\Delta ptsG 2p$ 0 0.5820.57429.43737.7340.5140.4510.6310.61526.627 37.706 0.6870.7651 0.73519.5561.4310.79528.3900.929 3 50.9330.74727.94527.7102.3081.961 $\overline{7}$ 0.873 16.959 26.5751.940 1.1344.500 $\Delta ptsG 1p$ 0 0.561 0.564 29.276 44.400 0.412 0.404 0.696 0.69227.75324.8741 0.4553 1.1491.16729.74024.8380.403 $5 \\ 7$ 1.3981.51822.468 0.89518.6461.0582.20822.1241.3542.12414.8301.834 $\Delta xylE 2p$ 0 0.5220.55627.46851.1260.5560.5350.6240.633 31.077 26.8520.9670.760 1 0.9270.87623.33515.3311.6620.993 3 $\mathbf{5}$ 1.1461.17325.10023.4283.0552.39271.3081.30218.74215.4123.2792.715 $\Delta xylE 1p$ 0.540 0 0.56128.647 34.630 0.5520.501 1 0.6220.62131.23918.5371.1314.8203 0.9450.97228.53317.004 2.1241.31721.021 4.2663.044 51.4131.37715.139 $\overline{7}$ 1.9711.9176.9478.7402.8893.148

 Table A.7.: Concentration Time Courses for Taxadiene Producing Strains.
 Duplicate concentration time courses for five taxadiene producing strains are given.

| | P | HMS | 2n | AxvlE | 2n | AxvlE | 1n | AntsG | 2n | AntsG | 1n |
|---------------------|-------------------|-------|------------------------|-------|-------------------------|-------|-------------------------|-------|------------------------|-------|------------------------|
| Amino Acid | Fragment | % - | -σ σ | % | $-\frac{2}{\sigma}$ | % | $-\sigma^{1}$ | % | $-\sigma^{2}$ | % | $-\sigma^{1}$ |
| Ala-260 | M+0 | 0.934 | 2.980E-03 | 0.944 | 1.315E-03 | 0.919 | 2.968E-03 | 0.931 | 3.617E-03 | 0.912 | 2.092E-03 |
| Ala-260 | M+1 | 0.009 | 2.564E-03 | 0.008 | 1.291E-03 | 0.016 | 2.732E-03 | 0.019 | 3.303E-03 | 0.019 | 1.962E-03 |
| Ala-260 | M+2 | 0.006 | 3.178E-04 | 0.006 | 6.089E-04 | 0.010 | 6.032E-04 | 0.010 | 6.044E-04 | 0.012 | 5.825E-04 |
| Ala-260 | M+3 | 0.050 | 6.413E-04 | 0.042 | 6.788E-04 | 0.055 | 5.422E-04 | 0.040 | 3.745E-04 | 0.057 | 7.258E-04 |
| Asp-418 Asp-418 | M+0 M+1 | 0.891 | 1.809E-03 | 0.909 | 9.501E-04 8.426E-04 | 0.862 | 4.125E-03 4.174E-03 | 0.888 | 1.894E-03 1.680E-03 | 0.841 | 2.554E-03 2.810E-03 |
| Asp-418 | M+2 | 0.024 | 1.147E-03 | 0.020 | 5.316E-04 | 0.033 | 1.330E-03 | 0.033 | 2.134E-03 | 0.050 | 1.077E-03 |
| Asp-418 | M+3 | 0.035 | 3.678E-04 | 0.025 | 4.796E-04 | 0.037 | 8.487E-04 | 0.022 | 5.565E-04 | 0.025 | 5.196E-04 |
| Asp-418 | M+4 | 0.003 | 2.635E-04 | 0.002 | 3.231E-04 | 0.004 | 1.584E-04 | 0.002 | 3.570E-04 | 0.003 | 8.999E-05 |
| Glu-432 | $^{\mathrm{M}+0}$ | 0.854 | 2.631E-03 | 0.872 | 3.018E-03 | 0.820 | 4.462E-03 | 0.854 | 4.843E-03 | 0.804 | 2.166E-03 |
| Glu-432 | $^{M+1}$ | 0.042 | 2.117E-03 | 0.045 | 3.079E-03 | 0.060 | 3.794E-03 | 0.054 | 3.564E-03 | 0.077 | 1.841E-03 |
| Glu-432 | M+2 | 0.082 | 1.566E-03 | 0.066 | 6.649E-04 | 0.095 | 1.916E-03 | 0.073 | 1.695E-03 | 0.096 | 2.225E-03 |
| Glu-432 Clu 422 | M+3 M+4 | 0.018 | 1.000E-03 | 0.013 | 6.943E-04 | 0.020 | 6.734E-04 | 0.015 | 6.820E-04 | 0.019 | 5.804E-04 |
| Glu-432 Glu-432 | M+4 M+5 | 0.003 | 2 339E-04 | 0.003 | 2.509E-04 6.043E-05 | 0.004 | 4.178E-04 1 119E-04 | 0.003 | 7.015E-05 | 0.004 | 7 789E-05 |
| Glv-246 | M+0 | 0.936 | 6.189E-04 | 0.947 | 7.906E-04 | 0.924 | 6.366E-04 | 0.939 | 2.662E-03 | 0.918 | 1.091E-03 |
| Gly-246 | M+1 | 0.013 | 6.568E-04 | 0.011 | 6.325E-04 | 0.018 | 6.722E-04 | 0.019 | 2.531E-03 | 0.024 | 9.768E-04 |
| Gly-246 | M+2 | 0.051 | 6.939E-04 | 0.042 | 2.483E-04 | 0.058 | 5.347E-04 | 0.043 | 3.970E-04 | 0.058 | 3.015E-04 |
| His-440 | $^{M+0}$ | 0.857 | 3.009E-03 | 0.881 | 1.877E-03 | 0.827 | 2.361E-03 | 0.862 | 2.795E-03 | 0.812 | 4.596E-03 |
| His-440 | M+1 | 0.055 | 4.232E-03 | 0.047 | 9.179E-04 | 0.071 | 3.330E-03 | 0.058 | 3.612E-03 | 0.079 | 4.839E-03 |
| H18-440 | M+2 M+2 | 0.027 | 1.822E-03 | 0.022 | 2.179E-03 | 0.036 | 2.402E-03 | 0.027 | 1.590E-03 | 0.042 | 2.163E-03 |
| His-440 | M+3 M+4 | 0.038 | 9.074E-04 | 0.032 | 9.731E-04 7.217E-04 | 0.040 | 2.021E-03 5.517E-04 | 0.035 | 1.471E-04 | 0.048 | 6.396E-04 |
| His-440 | M+5 | 0.016 | 6.389E-04 | 0.013 | 3.869E-04 | 0.014 | 4.941E-04 | 0.012 | 8.099E-04 | 0.011 | 4.956E-04 |
| His-440 | M+6 | 0.001 | 2.831E-04 | 0.001 | 2.520E-04 | 0.001 | 3.943E-04 | 0.000 | 3.612E-04 | 0.000 | 1.400E-04 |
| Ile-200 | M+0 | 0.859 | 1.114E-03 | 0.885 | 9.018E-04 | 0.826 | 1.307E-03 | 0.864 | 2.857E-03 | 0.807 | 9.733E-04 |
| Ile-200 | M+1 | 0.038 | 3.968E-04 | 0.034 | 5.744E-04 | 0.057 | 1.387E-03 | 0.050 | 2.182E-03 | 0.075 | 8.657E-04 |
| fle-200 | M+2 | 0.082 | 7.766E-04 | 0.065 | 3.457E-04 | 0.094 | 4.016E-04 | 0.069 | 6.309E-04 | 0.097 | 6.888E-04 |
| 11e-200 Ile 200 | M+3 M+4 | 0.017 | 2.073E-04 | 0.013 | 1.061E-04 6.100E.05 | 0.019 | 1.738E-04 | 0.014 | 3.132E-04 | 0.017 | 3.678E-04 |
| 11e-200 Ile-200 | M+4 M+5 | 0.003 | 1.373E-04 6.075E-05 | 0.002 | 4.236E-05 | 0.003 | 7.314E-03 5.801E-05 | 0.002 | 1.139E-04 6.801E-05 | 0.003 | 1.291E-04 5 338E 05 |
| Leu-274 | M+0 | 0.842 | 8.555E-04 | 0.875 | 1.677E-03 | 0.813 | 2.007E-03 | 0.852 | 5.227E-03 | 0.809 | 2.346E-03 |
| Leu-274 | M+1 | 0.051 | 1.097E-03 | 0.041 | 1.899E-03 | 0.068 | 2.039E-03 | 0.056 | 4.421E-03 | 0.066 | 1.840E-03 |
| Leu-274 | M+2 | 0.092 | 6.231E-04 | 0.072 | 7.846E-04 | 0.101 | 5.817E-04 | 0.077 | 1.007E-03 | 0.107 | 8.957E-04 |
| Leu-274 | M+3 | 0.010 | 3.020E-04 | 0.009 | 1.679E-04 | 0.012 | 1.312E-04 | 0.010 | 4.354E-04 | 0.013 | 2.845E-04 |
| Leu-274 | M+4 | 0.004 | 9.750E-05 | 0.004 | 1.787E-04 | 0.005 | 1.364E-04 | 0.004 | 8.379E-05 | 0.005 | 1.128E-04 |
| Leu-274 | M+5 | 0.000 | 1.074E-04 | 0.000 | 6.585E-05 | 0.001 | 9.298E-05 | 0.000 | 9.645E-05 | 0.001 | 7.141E-05 |
| Lys-431 Lys-431 | M+0 M+1 | 0.846 | 1.740E-03 2.254E-03 | 0.875 | 3.888E-03 | 0.812 | 3.891E-03 3.982E-03 | 0.853 | 3.967E-03 5.255E-03 | 0.794 | 2.218E-03 2.019E-03 |
| Lys=431 | M+2 | 0.040 | 2.517E-03 | 0.042 | 1.603E=03 | 0.003 | 3.038E-03 | 0.052 | 3.271E-03 | 0.072 | 1.546E=03 |
| Lys-431 | M+2 M+3 | 0.051 | 1.258E-03 | 0.039 | 1.256E-03 | 0.056 | 1.139E-03 | 0.038 | 1.399E-03 | 0.048 | 7.768E-04 |
| Lys-431 | M+4 | 0.001 | 5.495E-04 | 0.001 | 1.074E-03 | 0.002 | 4.057E-04 | 0.001 | 4.545E-04 | 0.003 | 1.205E-03 |
| Lys-431 | M+5 | 0.002 | 5.656E-04 | 0.001 | 5.356E-04 | 0.002 | 5.198E-04 | 0.000 | 2.647E-04 | 0.001 | 4.245E-04 |
| Lys-431 | M+6 | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 |
| Met-320 | M+0 | 0.915 | 1.005E-01 | 0.933 | 7.293E-02 | 0.814 | 6.578E-03 | 0.928 | 7.937E-02 | 1.000 | 4.419E-08 |
| Met-320 Mot-320 | M+1 M+2 | 0.052 | 7.160E-02 1.222E-02 | 0.041 | 4.511E-02 1.610E-02 | 0.102 | 9.025E-03 | 0.041 | 4.593E-02 2.060E-02 | 0.000 | 4.486E-08 |
| Met=320 | M+3 | 0.010 | 1.810E-02 | 0.013 | 1.206E=02 | 0.040 | 4 471E-03 | 0.010 | 1.171E-02 | 0.000 | 0.000E+00 |
| Met-320 | M+4 | 0.004 | 6.758E-03 | 0.002 | 2.926E-03 | 0.004 | 3.451E-03 | 0.001 | 1.870E-03 | 0.000 | 0.000E+00 |
| Met-320 | M+5 | 0.008 | 9.015E-03 | 0.001 | 3.268E-03 | 0.001 | 1.837E-03 | 0.001 | 1.773E-03 | 0.000 | 0.000E + 00 |
| Phe-336 | $^{\mathrm{M}+0}$ | 0.810 | 3.311E-03 | 0.850 | 2.089E-03 | 0.770 | 2.718E-03 | 0.807 | 1.068E-02 | 0.766 | 1.739E-03 |
| Phe-336 | $^{M+1}$ | 0.040 | 3.024E-03 | 0.032 | 1.535E-03 | 0.061 | 2.605E-03 | 0.058 | 1.027E-02 | 0.056 | 1.596E-03 |
| Phe-336 | M+2 | 0.046 | 1.835E-03 | 0.036 | 1.319E-03 | 0.054 | 1.398E-03 | 0.044 | 1.098E-03 | 0.060 | 1.062E-03 |
| Phe-336 Pho 336 | M+3 M+4 | 0.067 | 5.878E-04 7 201E 04 | 0.053 | 4.226E-04 7 101E 04 | 0.074 | 1.529E-03 0.748E-04 | 0.061 | 1.856E-03 5.601E-04 | 0.075 | 9.133E-04 3.603E-04 |
| Phe-336 | M+4 M+5 | 0.024 | 2.895E-04 | 0.020 | 3.894E-04 | 0.027 | 9.748E=04 2.821E=04 | 0.020 | 4 702E-04 | 0.030 | 4.034E-04 |
| Phe-336 | M+6 | 0.004 | 2.618E-04 | 0.003 | 2.484E-04 | 0.004 | 2.484E-04 | 0.003 | 1.238E-04 | 0.005 | 1.960E-04 |
| Phe-336 | M+7 | 0.002 | 2.171E-04 | 0.001 | 1.332E-04 | 0.002 | 1.873E-04 | 0.001 | 2.396E-04 | 0.002 | 1.276E-04 |
| Phe-336 | M+8 | 0.000 | $0.000\mathrm{E}{+00}$ | 0.000 | $0.000 \mathrm{E}{+00}$ | 0.000 | $0.000\mathrm{E}{+00}$ | 0.000 | 0.000E + 00 | 0.000 | 1.141E-05 |
| Phe-336 | M+9 | 0.000 | 0.000E + 00 | 0.000 | 0.000E+00 | 0.000 | $0.000 \mathrm{E}{+00}$ | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 |
| Pro-286 | M+0 | 0.865 | 1.491E-03 | 0.884 | 1.626E-03 | 0.834 | 2.155E-03 | 0.867 | 1.683E-03 | 0.814 | 1.780E-03 |
| Pro-286 Pro-286 | M+1 M+2 | 0.045 | 1.421E-03 8 713E 04 | 0.045 | 1.278E-03 9.787E-04 | 0.062 | 2.114E-03 1.018F-02 | 0.057 | 1.881E-03 1.961E-03 | 0.081 | 1.202E-03 1.978E-02 |
| Pro-286 | M+3 | 0.020 | 6.241E-04 | 0.015 | 6.414E-04 | 0.021 | 7.249E-04 | 0,016 | 6.849E-04 | 0.019 | 6.094E-04 |
| Pro-286 | M+4 | 0.004 | 5.591E-04 | 0.003 | 3.881E-04 | 0.004 | 5.576E-04 | 0.003 | 5.908E-04 | 0.005 | 2.993E-04 |
| Pro-286 | M+5 | 0.001 | 2.546E-04 | 0.000 | 3.194E-04 | 0.001 | 2.386E-04 | 0.000 | 1.980E-04 | 0.001 | 2.314E-04 |
| Ser-390 | $^{\mathrm{M}+0}$ | 0.926 | 2.752E-03 | 0.945 | 2.232E-03 | 0.914 | 2.593E-03 | 0.934 | 4.186E-03 | 0.907 | 2.597E-03 |
| Ser-390 | M+1 | 0.022 | 2.837E-03 | 0.013 | 3.392E-03 | 0.027 | 2.418E-03 | 0.022 | 4.058E-03 | 0.033 | 2.747E-03 |
| Ser-390 | M+2 M+2 | 0.021 | 1.056E-03 | 0.015 | 1.349E-03 | 0.023 | 1.067E-03 | 0.018 | 1.440E-03 | 0.025 | 8.984E-04 |
| Ser-390 Thr-404 | M+3 M+0 | 0.031 | 0.418E-04 2.713E-03 | 0.026 | 3.878E-04 1.778E-03 | 0.036 | 0.087E-04 2.511E-03 | 0.026 | 7.491E-04 8.432E-03 | 0.035 | 7.091E-04 2.286E-03 |
| Thr-404 | M+0 M+1 | 0.068 | 2.081E-03 | 0.063 | 2.445E-03 | 0.087 | 3.752E-03 | 0.083 | 1.045E-02 | 0.101 | 1.860E-03 |
| Thr-404 | M+2 | 0.031 | 1.712E-03 | 0.028 | 1.288E-03 | 0.038 | 2.383E-03 | 0.035 | 2.951E-03 | 0.056 | 1.697E-03 |
| Thr-404 | M+3 | 0.032 | 1.453E-03 | 0.021 | 4.553E-04 | 0.036 | 1.413E-03 | 0.020 | 1.148E-03 | 0.024 | 1.016E-03 |
| Thr-404 | M+4 | 0.000 | $0.000\mathrm{E}{+00}$ | 0.000 | $0.000\mathrm{E}{+00}$ | 0.000 | $0.000\mathrm{E}{+00}$ | 0.000 | $0.000\mathrm{E}{+00}$ | 0.000 | $0.000\mathrm{E}{+00}$ |
| Tyr-466 | M+0 | 0.820 | 4.341E-03 | 0.858 | 3.717E-03 | 0.779 | 7.490E-03 | 0.827 | 4.299E-03 | 0.775 | 3.563E-03 |
| 1 yr-466 Twr 466 | M+1 M+2 | 0.033 | 3.134E-03 | 0.027 | 4.244E-03 | 0.052 | 5.207E-03 | 0.045 | 4.067E-03 | 0.046 | 2.948E-03 |
| 1 yr-400 Tyr-466 | M+2 M+3 | 0.047 | 1.833E-03 1.067E-03 | 0.036 | 1.934E-03 1.449E-03 | 0.055 | 3.081E-03 1.065E-03 | 0.041 | 1.024E-03 2.127E-03 | 0.061 | 2.808E-03 1.017E-03 |
| Tyr-466 | M+4 | 0.024 | 9.120E-04 | 0.018 | 6.356E-04 | 0.028 | 7.953E-04 | 0.021 | 1.052E-03 | 0.031 | 9.899E-04 |
| Tyr-466 | M+5 | 0.007 | 7.686E-04 | 0.007 | 8.202E-04 | 0.009 | 9.056E-04 | 0.007 | 6.027E-04 | 0.010 | 6.855E-04 |
| Tyr-466 | M+6 | 0.004 | 4.356E-04 | 0.003 | 4.505E-04 | 0.005 | 4.586E-04 | 0.004 | 2.627E-04 | 0.005 | 4.722E-04 |
| Tyr-466 | M+7 | 0.001 | 1.486E-04 | 0.001 | 3.328E-04 | 0.001 | 1.458E-04 | 0.001 | 4.547E-04 | 0.002 | 3.671E-04 |
| Tyr-466 | M+8 | 0.000 | 4.309E-05 | 0.001 | 3.921E-04 | 0.000 | 3.580E-04 | 0.001 | 2.226E-04 | 0.001 | 9.012E-05 |
| Tyr-466 | M+9 M+0 | 0.001 | 3.107E-04 | 0.000 | 3.071E-04 | 0.000 | 3.830E-04 | 0.000 | 3.040E-04 | 0.000 | 1.836E-04 |
| vai-288 Val-288 | M+0 M+1 | 0.885 | 7.441E-04 1.049E-02 | 0.907 | 1.020E-03 | 0.858 | 2.424E-03 2.308E-02 | 0.887 | 4.239E-03 3.544E-03 | 0.852 | 1.027E-03 |
| Val-288 | M+2 | 0.013 | 8.292E-04 | 0.042 | 5.884E-04 | 0.043 | 2.336E-03 | 0.047 | 1.112E-03 | 0.043 | 7.956E-04 |
| Val-288 | M+3 | 0.045 | 4.637E-04 | 0.035 | 1.714E-04 | 0.051 | 3.972E-04 | 0.036 | 3.035E-04 | 0.052 | 5.016E-04 |
| Val-288 | M+4 | 0.001 | 2.030E-04 | 0.001 | 1.200E-04 | 0.002 | 1.872E-04 | 0.001 | 1.739E-04 | 0.002 | 3.099E-04 |
| Val-288 | M+5 | 0.004 | 1.756E-04 | 0.003 | 9.497E-05 | 0.005 | 1.374E-04 | 0.003 | 1.761E-04 | 0.005 | 1.294E-04 |

Table A.8.: ¹³C-labeling Data for Five Taxadiene Producing Strains. Labeling patterns of protein-bound amino acids was experimentally determined in duplicate for five taxadiene producing strains.

A.2.4. Metabolic Model Used for the Software 13CFlux2

An exemplary model for the analysis of ¹³C labeling data is provided below. All required ".fml" files were generated using a Matlab script. All calculations were performed with the software 13CFlux2 [155]. 13CFlux2 is a Linux-based software, which is operated via the terminal command line. 13CFlux2 offers a great variety of functions. In this work, the software was used to calculate the intracellular flux distribution best matching experimentally determined exchange rates and labeling data. Five different 13CFlux2 functions were used to estimate flux distributions. First, the ".fml" file must be signed using the function *fmlsiqn*. The resulting file is then initialized using the function *sscanner*, which chooses a set of free fluxes and initialize the flux values with the analytical center of the specified constraints (exchange and growth rates). In a third step, the function *ssampler* is used to sample uniformly distributed, random flux distributions from the stoichiometry of the metabolic network given in the ".fml" file. Each sampled flux distribution is used as a starting point for the optimization problem which is performed by the function *multifitfluxes*. For each flux distribution, *multifitfluxes* generates a ".fwdsim" file, which contains the fitted flux distribution. Finally, the function *collectfitdata* is used for collecting together the results from multiple ".fwdsim" files into a single HDF5 file. Further analysis of the fitted flux distributions is performed in Matlab using the generated HDF5 file. The process described above was fully automatized using a series of python scripts and Matlab workflows.

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                             \label{eq:XBNPKM6aH1IkYtVXxgbRnlestwpQ/d2UUfe9ESe4A7UIKrKqVVPeio5zsb1CEhbcA/QDWgpwwY0P86PuU4tpEnvAFK4apMNEAX2zSiPrTMcN7bXdidY7lzZk2Kia+UkMOf766wf/XUj+4
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id="accoa_c"/>
id="ac c"/>
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22
                                              <pool
                                                                     atoms="2"
                                                                     atoms="6
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23
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                                                                                                             id="fum c"/>
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atoms = "4"
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                                                                                                            Id="asn_DASH_L_c"/>
id="lys_DASH_L_c"/>
id="lys_DASH_L_c"/>
id="2ddg6p_c"/>
id="g3p_c"/>
id="6pgc_c"/>
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<pool id="fadh2_
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id="mal_DASH_L_c"/>
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id="g6p_c"/>
id="3pg_c"/>
id="ser_DASH_L_c"/>
id="gly_c"/>
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<pool atoms="1" id="mlthf_c"/>
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47
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| 48 | $<$ pool atoms="3" id="pep_c"/> |
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| 49 | $<$ pool atoms="6" id="glc_DASH_D_c"/> |
| 50 | <pre><pre>cpool atoms="5" id="ru5p DASH D c"/></pre></pre> |
| 51 | <pre><pool atoms="1" id="10fthf c"></pool></pre> |
| 52 | $<$ pool atoms="5" id="prpp $c^{-n}/>$ |
| 53 | <pre><pre>pool atoms="6" id="his DASH L c"/></pre></pre> |
| 54 | <pool atoms="2" id="glx c"/> |
| 55 | <pre><pre>pool atoms="4" id="thr DASH L c"/></pre></pre> |
| 56 | <pre><pre>pool atoms="6" id="ile DASH L c"/></pre></pre> |
| 57 | <pre><pre>cpool atoms="6" id="leu DASH L c"/></pre></pre> |
| 58 | <pre><pre>cpool atoms="1" id="methf c"/></pre></pre> |
| 59 | \leq pool atoms="3" id="cvs DASH L c"/> |
| 60 | <pre><pre>cpool atoms="5" id="met DASH_L_c"/></pre></pre> |
| 61 | <pre><pre>choose="6" id="f6p_c"/></pre></pre> |
| 62 | $\langle pool atoms = 4^{\circ} id = 8^{\circ} p_{o} \rangle$ |
| 63 | $\langle pool atoms = 9 id = bb = DSH L c'' / $ |
| 64 | <pre><pre>cpool atoms="5" id="pro_DASH_L_c"/></pre></pre> |
| 65 | <pre></pre> |
| 66 | $<$ pool atoms="5" id="sy5p_DASH_D_c"/> |
| 67 | <pre><pre>cpool atoms="7" id="s7p_c"/></pre></pre> |
| 68 | $\langle pool atoms = 1 $ id $= 17 $ $C_{2} $ $c_{1} / >$ |
| 60 | $\langle pool atoms = 0 id = 1TK C_2 c'' / \rangle$ |
| 70 | \sim pool atoms = 2 if $a = 10^{-2} c^{-7}/\gamma$ |
| 71 | <pre><pre>cpool atoms="10" id="tup DASH L c"/></pre></pre> |
| 72 | $\langle pool atoms = 5 id = 0 DASH = c / \rangle$ |
| 72 | <pre> <pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre> |
| 74 | $\langle \text{pool} \text{atoms} = 0 \text{id} = \text{gl}(0) / 2$ |
| 75 | <pre><pre>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>></pre></pre> |
| 76 | <pre><pre>cpool atoms="5" id="Xylose c"/></pre></pre> |
| 77 | <pre> /metabolitemols</pre> |
| 78 | <pre></pre> // metabontepools/ // action bidirectional="falso" id="26dap DASH MSVN"> |
| 70 | <pre>creation ordineterional = raise Id= 200ap DASH MSH*> ////////////////////////////////////</pre> |
| 19 | <pre><reduct 0#1241="" 0#124<="" cig_="" td=""></reduct></pre> |
| 00 | $\langle reduct \ clg = 0 \# 102 \ 0 \# 202 \ 0 \# 002 \ 1 = pyr \ c' / 2$ |
| 01 | $\langle reduct \ clg = 0.74203 \ 0.7203 \ 0.7403 \ 0.7403 \ clg = 30000 \ clg = 0.7200 \ clg = 0.720$ |
| 82 | $\langle \text{reduct } 1d = \text{atp c} / \rangle$ |
| 83 | <reduct 1d="asp_DASH_L_c" crg="C#104 C#204 C#304 C#404"></reduct> |
| 84 | <reduct id="nadph_c"></reduct> |
| 85 | <reduct id="nadph_c"></reduct> |
| 86 | <pre><rproduct ctg="C#104 C#204 C#302 C#202 C#202 C#102" id="26dap_DASH_M_c"></rproduct></pre> |
| 81 | $< r product crg = -C_{H} - C_{H} - 203 - C_{H} - 203 - C_{H} - 403 - 104 - succ - c^{-}/>$ |
| 00 | <pre></pre> |
| 09 | |
| 01 | <pre><reaction _="" aconta_aconta_<br="" biuntectional="title"><reaction _="" aconta_aconta_<br="" biuntectional="title"><reaction _="" aconta_aconta_<br="" biuntectional="title"></reaction></reaction></reaction></pre> |
| 92 | $\langle reader erg = -e_{rr}er = -$ |
| 93 | |
| 94 | <pre><reaction bidirectional="false" id="AKGDH"></reaction></pre> |
| 95 | <reduct cfg="C#1@1 C#2@1 C#3@1 C#4@1 C#5@1" id="akg c"></reduct> |
| 96 | <rproduct id="nadh c"></rproduct> |
| 97 | <pre>crproduct cfg="C#2@1 C#3@1 C#4@1 C#5@1" id="succoa c"/></pre> |
| 98 | <rproduct cfg="C#1@1" id="co2 c"></rproduct> |
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| 100 | <reaction bidirectional="false" id="ALATA_L"></reaction> |
| 101 | <reduct cfg="C#1@1 C#2@1 C#3@1 C#4@1 C#5@1" id="glu_DASH_L_c"></reduct> |
| 102 | <reduct cfg="C#1@2 C#2@2 C#3@2" id="pyr c"></reduct> |
| 103 | $<$ rproduct cfg="C#101 C#201 C#301 C#401 C#501" id="akg_c"/> |
| 104 | <pre><rproduct crg="C#102 C#202 C#302" id="aia_DASH_L_c"></rproduct></pre> |
| 106 | |
| 107 | <pre><reaction bidirectional="taise" ind="Argoin</pre"></reaction></pre> |
| 108 | <pre>creduct cig = 0#191 0#291 0#391 0#391 0#391 10= glu DASH L C /> creduct cig= 0#192 0#390 0#409 0#4091 0#502" id="du" DASH L C" /></pre> |
| 100 | $\langle reduct \ clg = 0 \# 102 \ cl \# 202 \ cl \# 102 \ cl \#$ |
| 110 | Creduct dig of the of t |
| 111 | $\langle reduct id = atp = c / \rangle$ |
| 110 | <pre><reduct c="" id="abp"></reduct> <reduct id="abp c"></reduct></pre> |
| ⊾⊥⊿ 119 | <pre><reduct id="ap" t=""></reduct> <reduct id="atp c"></reduct></pre> |
| 114 | <pre><reduct c="" id="abp"></reduct> <reduct id="abp c"></reduct></pre> |
| L14 115 | $\langle reduct id = ab - c / \rangle$ |
| 116 | <reduct $1d=$ nadph $c' >$ |
| 117 | $\langle reduct \ clg = 0 + 1 = 4 + 1 = 4 = 0 = 0 = 0 / 2$ |
| 118 | $<$ rorduct erg $ \sigma_{\mu}$ as σ_{μ} |
| 110 | $\langle rproduct cfg = (\mathcal{F}_{1}) = (\mathcal{F}_{2}) =$ |
| 120 | <rproduct cfg="C#102 C#202 C#202 C#402 C#50" id="attractor" |
| 121 | <rproduct cfg="C#1@5 C#2@5 C#3@5 C#4@5" id="fum c"/> |
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| 123 | <reaction bidirectional="false" id="ASNN"></reaction> |
| 124 | <reduct id="atp c"></reduct> |
| 125 | <reduct id="atp c"></reduct> |
| 126 | <reduct cfg="C#1@1 C#2@1 C#3@1 C#4@1" id="asp DASH L c"></reduct> |
| 127 | <reduct id="nh4_c"></reduct> |
| 128 | <rproduct cfg="C#1@1 C#2@1 C#3@1 C#4@1" id="asn_DASH L c"></rproduct> |
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| 130 | <reaction bidirectional="false" id="ASPTA"></reaction> |
| 131 | <reduct cfg="C#1@1 C#2@1 C#3@1 C#4@1 C#5@1" id="glu_DASH_L_c"></reduct> |
| 132 | <reduct cfg="C#1@2 C#2@2 C#3@2 C#4@2" id="oaa_c"></reduct> |
| 133 | <rproduct cfg="C#101 C#201 C#201 C#401 C#401 C#501" id="akg_c"></rproduct> |
| 134 | <rproduct cfg="C#1@2 C#2@2 C#3@2 C#4@2" id="asp_DASH_L_c"></rproduct> |
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| 130 | <reaction didirectional="laise" ld="AlfM"></reaction> |
| 120 | <pre> (reduct id= atp_c//></pre> |
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<reduct cfg="C#102 C#202" id="accoa_c"/>
<rproduct cfg="C#401 C#301 C#201 C#202 C#102 C#101" id="cit_c"/>
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\begin{array}{c} 141 \\ 142 \end{array}
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158 \\ 159
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172
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A.2. Strain Design Algorithms for Target Identification

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| 598 | |
| 599 | <reaction id="BM met DASH L c"></reaction> |
| 600 | <reduct cfg="C#1@9 C#2@9 C#3@9 C#4@9 C#5@9" id="met DASH L c"></reduct> |
| 601 | |
| 602 | <reaction id="BM g6p c"></reaction> |
| 603 | <reduct cfg="C#1@10 C#2@10 C#3@10 C#4@10 C#5@10 C#6@10" id="g6p_c"></reduct> |
| 604 | |
| 605 | <reaction id="BM_akg_c"></reaction> |
| 606 | <reduct cfg="C#1@11 C#2@11 C#3@11 C#4@11 C#5@11" id="akg_c"></reduct> |
| 607 | |
| 608 | <reation id="BM gh DASH L C"></reation> |
| 610 | <pre></pre> |
| 611 | <pre>creation id="BM gh DASH L c"></pre> |
| 612 | <reduct cfr="C#1@13 C#2@13 C#4@13 C#4@13 C#5@13" id="gln_DASH_L_c"></reduct> |
| 613 | <pre></pre> |
| 614 | <pre><reaction id="BM r5p c"></reaction></pre> |
| 615 | <reduct cfg="C#1@14 C#2@14 C#3@14 C#4@14 C#5@14" id="r5p c"></reduct> |
| 616 | |
| 617 | <reaction id="BM_f6p_c"></reaction> |
| 618 | <pre><reduct cfg="C#1@15 C#2@15 C#3@15 C#4@15 C#5@15 C#6@15" id="f6p_c"></reduct></pre> |
| 619 | |
| 620 | <reaction id="BM_pyr c"></reaction> |
| 622 | <pre><reduct 1d="pyr_c" crg="C#1010 C#2010 C#3010"></reduct></pre> |
| 623 | |
| 624 | $<$ reaction id= $Bm_{gy} = c$ $<$ reduct cfp="c#1017 C#2017" id="gly_c"/> |
| 625 | |
| 626 | <pre><reaction id="BM thr DASH L c"></reaction></pre> |
| 627 | <pre><reduct cfg="C#1@18 C#2@18 C#3@18 C#4@18" id="thr DASH L c"></reduct></pre> |
| 628 | |
| 629 | <reaction id="BM_asp_DASH_L_c"></reaction> |
| 630 | <reduct cfg="C#1@19 C#2@19 C#3@19 C#4@19" id="asp_DASH_L_c"></reduct> |
| 631 | |
| 632 | <reaction id="BM_nadph_c"></reaction> |
| 633 | <pre><reduct id="nadph_c"></reduct></pre> |
| 625 | |
| 636 | $<$ reaction id= m_{-} v_{-} v_{- |
| 637 | |
| 638 | <pre><reaction id="BM 3bg c"></reaction></pre> |
| 639 | <reduct cfg="C#1@21 C#2@21 C#3@21" id="3pg c"></reduct> |
| 640 | |
| 641 | <reaction id="BM_val_DASH_L_c"></reaction> |
| 642 | <pre><reduct cfg="C#1@22 C#2@22 C#3@22 C#4@22 C#5@22" id="val_DASH_L_c"></reduct></pre> |
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| 644 | <reaction id="BM_ala_DASH_L_c"></reaction> |
| 645 | <reduct cfg="C#1@23 C#2@23 C#3@23" id="ala_DASH_L_c"></reduct> |
| 640 647 | |
| 648 | <pre><reat (#3024="" c#3024="" c#5024="" c#6024"="" dm_ine_dash_l_c="" fid_="" foil="" id="ile_DASH_L_c"></reat></pre> |
| 649 | <pre></pre> |
| 650 | <reaction id="BM asn DASH L c"></reaction> |
| 651 | <reduct cfg="C#1@25 C#2@25 C#3@25 C#4@25" id="asn DASH L c"></reduct> |
| 652 | |
| 653 | <reaction id="BM_his_DASH_L_c"></reaction> |
| 654 | <pre><reduct cfg="C#1@26 C#2@26 C#3@26 C#4@26 C#5@26 C#6@26" id="his_DASH_L_c"></reduct></pre> |
| 655 | |
| 000 | <pre><reaction id="BM let DASH L c"> </reaction></pre> <pre></pre> |
| 658 | <pre></pre> |
| 659 | <reaction id="BM accoa c"></reaction> |
| 660 | <reduct_cfp="c#1@28_c#2@28"_id="accoa_c"></reduct_cfp="c#1@28_c#2@28"_id="accoa_c"> |
| 661 | |
| 662 | <reaction id="BM_arg_DASH_L_c"></reaction> |
| 663 | $<\!\! \texttt{reduct cfg} = "C\!\#1@29 \ C\!\#2@29 \ C\!\#3@29 \ C\!\#4@29 \ C\!\#4@29 \ C\!\#6@29" \ id = "arg_DASH_L_c"/>$ |
| 664 | |
| 665 | <reaction id="BM pro DASH L c"></reaction> |
| 667 | <pre><reduct ctg="C#1030 C#2030 C#3030 C#4030 C#5030" id="pro_DASH_L_c"></reduct></pre> |
| 668 | |
| 669 | <pre></pre> |
| 555 | @31" id="trp DASH L c"/> |
| 670 | |
| 671 | |
| 672 | <constraints></constraints> |
| 673 | <net></net> |
| 674 | $<$ textual>BM_phe_DASH_L c=0.0882992;BM_mlthf c=0.2222531;BM_oaa_c=0.170578; |
| | BM IVS DASH L c= 0.0657237 , BM atp c= 10.0800199 jsM set DASH L c= 0.1028488 ; BM g3p c= 0.0047193 ; BM Tr DASH L c= 0.06723489 jsm c= 0.00198485 ; BM c= 0.00198 |
| | BM_gir_DLM_L_C=0.0436479;BM_gep_C=0.025007;DM_llme_DASH_L_C=0.0152405;BM_g0p_C=0.1026489; BM_gir_C=0.0436479;BM_gir_DASH_L_C=0.125425;BM_gr_DASH $\delta_{\rm L}$ = 0.125425;BM_gr_D=0.3789818. |
| | BM f6p c=0.0356207; BM pyr c=0.0416411; BM gly c=0.2919894; BM thr DASH L c=0.1209097: |
| | BM asp DASH L c=0.1148893; BM nadph c=2.6906171; BM cys DASH L c=0.0436479; BM 3pg c=0.3105523: |
| | $BM_val_DASH_L_c=0.2016834; BM_ala_D\overline{A}SH_L_c=0.2448296; B\overline{M}_ile_D\overline{A}SH_L_c=0.1384692;$ |
| | $\mathrm{BM}_\mathrm{asn}_\mathrm{DASH}_\mathrm{L}_\mathrm{c}=0.1148893; \mathrm{BM}_\mathrm{his}_\mathrm{DASH}_\mathrm{L}_\mathrm{c}=0.045153; \mathrm{BM}_\mathrm{leu}_\mathrm{DASH}_\mathrm{L}_\mathrm{c}=0.2147276; \mathrm{BM}_\mathrm{accoa}_\mathrm{c}=0.2147276; \mathrm{BM}_\mathrm{c}=0.2147276; \mathrm{BM}_\mathrm{C}=$ |
| | $=1.259267; BM arg_DASH_L c=0.1409777; BM pro_DASH_L c=0.105357; BM trp_DASH_L c=0.0270918; BM trp_DASH_L c=0.02708; BM trp_DASH_L c=0.02708; BM trp_DASH_L c=0.02708; BM trp_DASH_L c$ |
| 675 | EX_co2_LPAREN_e_RPARENunlabeled &1t;=20 |
| 070 676 | |
| 677 | <pre> <textual></textual></pre> |
| 678 | |
| | |

```
679
                  </constraints>
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<constraints>
<constraints</constraints>
<constraints>
<c
680
681
682
683
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685
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688
689
                                    < label cfg = "111011">0.0016 < /label>
690
                           </input>
                          </input>
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<label cfg="000000">0.9358</label>
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<label cfg="000010">0.0107</label>
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<label cfg="001000">0.0107</label>
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<label cfg="100000">0.0107</label>
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699
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                          </input>
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<label cfg="01000">0.01076</label>
<label cfg="00100">0.01076</label>
<label cfg="00100">0.01076</label>
<label cfg="00100">0.01076</label>
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700
701
702
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706
707
                           </\operatorname{input}>
                          ("input pool="co2 c unlabeled" type="isotopomer">
    (label cfg="0">0.989</label>

(label cfg="1">0.011</label>
708
709
710
711
712
713
714
                           </input>
                           <input pool="so4_c_ext"/
<input pool="nh4_c_ext"/
<input pool="o2_c_ext"/>
715
                           <measurement>
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717
718
719
                                  < model >
                                           720
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                                                   722
                                                    </group>
                                                    724
725
726
727
                                                    </pro>
</pro>
{group>
<group id="ms_group_4" scale="auto">
<textual>gly_c[1,2]#M0,1,2</textual>
728
729
                                                    </group>
730
                                                    <group
                                                                      id="ms
                                                                                                            5" scale=
                                                             <textual>his_DASH_L_c[1,2,3,4,5,6] #M0,1,2,3,4,5,6</textual>
731
732
733
                                                    </group>
<group id="ms
                                                                                                          6" scale="auto
                                                                                          group
734
                                                              <textual>ile_DASH_L_c[2,3,4,5,6] #M0,1,2,3,4,5</textual>
735
                                                    </group>
                                                    </group>
<group id="ms_group_7" scale="auto">
<textual>leu_DASH_L_c[2,3,4,5,6]#M0,1,2,3,4,5</textual>
736
737
738
739
                                                          group>
                                                    740
741
742
                                                    </group>
                                                    743
744
                                                   </group>
</group>
<group id="ms_group_10" scale="auto">
<textual>phe_DASH_L_c[1,2,3,4,5,6,7,8,9]#M0,1,2,3,4,5,6,7,8,9</textual>

745
746
747
                                                    748
749
750
                                                    </group>
                                                            toup id="ms_group_12" scale="auto">
<textual>ser_DASH_L_c[1,2,3]#M0,1,2,3</textual>
751
                                                    <group id="ms_group</pre>
                                                    </r></group>
753
754
                                                                                                            13" scale="auto
                                                                                           group
755
                                                             <textual>thr_DASH_L_c[1,2,3,4] # M0,1,2,3,4</textual>
                                                    </group>
<group id="ms_group
                                                                                                           14" scale="auto">
757
758
                                                             clup id= ms_group_ifscale= arro<textual>tyr_DASH_L_c[1,2,3,4,5,6,7,8,9]#M0,1,2,3,4,5,6,7,8,9</textual>
                                                    </group>
</group id="ms_group_15" scale="auto">
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759
761
762
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763
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                                           <fluxmeasurement>
<netflux id="fm_Glucose">
764
765
                                                           <textual>EX_glc_LPAREN_e_RPAREN_</textual>
766
                                                    </ netflux>
<netflux id="fm_Xylose">
767
768
                                                    <textual>Pentose_Uptake</textual>
</netflux>
769
770
```
A.2. Strain Design Algorithms for Target Identification

| 771 | | |
|-----|---|--|
| 111 | III x measurement | |
| 772 | | |
| 773 | $\langle data \rangle$ | |
| 774 | <datum id="fm Glucose" stddev="0.2552">5.8296 | |
| 775 | \leq datum id="fm Xylose" stddey="0.48">2.277 | |
| 776 | \leq datum id="ms_group_1" stddey="0.0098765" weight="0">0.8623 | |
| 777 | | |
| 779 | datum id- ms_group 1 stddov- 0.00002444 weight- 12150.0122 (datum) | |
| 110 | datum id ms_group_1 still to $\operatorname{correct}$ weight 2 0.00123 / datum | |
| 119 | <pre><datum id="ms_group_1" stddev="0.0079651" weight="3">0.1105</datum></pre> | |
| 780 | $<$ datum id="ms_group_2" stddev="0.0082325" weight="0">0.7323 | |
| 781 | $<$ datum id="ms_group_2" stddev="0.0017888" weight="1">0.1086 | |
| 782 | <datum id="ms group 2" stddev="0.0024468" weight="2">0.0894 | |
| 783 | <pre><datum id="ms group 2" stddev="0.002975" weight="3">0.0586</datum></pre> | |
| 784 | <pre><datum id="ms group 2" stddev="0.0010218" weight="4">0.0111</datum></pre> | |
| 785 | $<$ datum id="ms_group_3" stddey="0.0083226" weight="0">0.6666 | |
| 786 | datum id="ms_group_3" stddey="0.0034515" weight="1">0.1053 | |
| 797 | datum id="ms_group_2" atddov="0.0028640" woight="2">0.1687_/datum> | |
| 700 | Catum Id ms_group_3 stddev= 0.0028049 weight= 2.0.1087 | |
| 100 | clatum id= ms_group 5" stable = 0.0017457" weight = 5 >0.0452 <td></td> | |
| 789 | <datum id="ms_group_3" stddev="0.00014063" weight="4">0.0118</datum> | |
| 790 | <pre><datum id="ms_group_3" stddev="0.00040113" weight="5">0.0045</datum></pre> | |
| 791 | $<$ datum id="ms_group_4" stddev="0.0076784" weight="0">0.8572 | |
| 792 | <pre><datum id="ms group 4" stddev="0.00088828" weight="1">0.0243</datum></pre> | |
| 793 | <pre><datum id="ms group 4" stddev="0.0067902" weight="2">0.1185</datum></pre> | |
| 794 | <pre><datum id="ms_group_5" stddev="0.020841" weight="0">0.7336</datum></pre> | |
| 795 | \leq datum id="ms_group 5" stddey="0.007452" weight="1">0.1165 \leq datum> | |
| 706 | datum id="ms_group_5" stddoy="0.0040407" woight="2">0.0376/datum> | |
| 707 | <pre>cdatum id="me_group_5" stddov="0.00540f" weight="2">0.0605//datum></pre> | |
| 700 | detum id= ins group 5 stdeev= 0.0054950 weight= 5.20.00252 / datum> | |
| 198 | catum id = ms_group_5" stddev="0.00064921" weight="4">0.0124 | |
| 799 | <pre><datum id="ms_group_5" stddev="0.003035" weight="5">0.034</datum></pre> | |
| 800 | $<$ datum id="ms_group_5" stddev="0.00016856" weight="6">0.0034 | |
| 801 | <pre><datum id="ms_group_6" stddev="0.011413" weight="0">0.6671</datum></pre> | |
| 802 | <pre><datum id="ms_group_6" stddev="0.00015775" weight="1">0.1072</datum></pre> | |
| 803 | <pre><datum id="ms group 6" stddev="0.0081215" weight="2">0.1689</datum></pre> | |
| 804 | <pre><datum id="ms group 6" stddev="0.0020657" weight="3">0.0428</datum></pre> | |
| 805 | <pre><datum id="ms_group_6" stddey="0.00078686" weight="4">0.0098</datum></pre> | |
| 806 | $datum id="ms_group_6" stddey="0.00028126" weight="5">0.0043$ | |
| 807 | $\langle datum id=ms group 7" stddey="0.015476" weight="0.0507/datum>$ | |
| 001 | Catum id_ ms_group_1 stddev_ 0.015910 weight=0.00597 (datum) | |
| 808 | | |
| 809 | clatum id= ms_group_7" stallev="0.010022" weight= 2 >0.1351 | |
| 810 | <datum id="ms_group_7" stddev="0.0019916" weight="3">0.0306</datum> | |
| 811 | <datum id="ms_group_7" stddev="0.00085108" weight="4">0.0147</datum> | |
| 812 | <pre><datum id="ms_group_7" stddev="0.00031291" weight="5">0.0024</datum></pre> | |
| 813 | $<$ datum id="ms_group_8" stddev="0.011261" weight="0">0.6487 | |
| 814 | $<$ datum id="ms_group_8" stddev="0.0010794" weight="1">0.1045 | |
| 815 | $<$ datum id="ms_group_8" stddev="0.0035929" weight="2">0.1243 | |
| 816 | <pre><datum id="ms_group_8" stddev="0.0042259" weight="3">0.0965</datum></pre> | |
| 817 | <pre><datum id="ms group 8" stddev="0.001673" weight="4">0.016</datum></pre> | |
| 818 | <pre><datum id="ms group 8" stddev="0.00068325" weight="5">0.0088</datum></pre> | |
| 819 | <datum id="ms group 8" stddev="6.5616e-06" weight="6">0.0012 | |
| 820 | < datum id="ms group 9" stddey="0.0057048" weight="0">0.6414 | |
| 821 | <pre><datum id="ms_group_9" stddey="0.00021786" weight="1">0.1828</datum></pre> | |
| 822 | <pre><datum id="ms_group_9" stddey="0_00067911" weight="2">0_0943</datum></pre> | |
| 823 | datum id="ms_group_0"_stddey="0.0033826"_weight="3">0.0622 | |
| 824 | datum id_ ms_group_0" stddov="0.0013483" weight="0.00178 | |
| 925 | datum id= mg_group_0 stddov= 7.70220.05% wright= 5%0.0015 | |
| 020 | Catum Id ms_group_9 stdev= 10 verses weight= 0 v0.0167 (datum) | |
| 020 | clatum id= ms_group_10* state = 0.020735* weight = 0.50107 <td></td> | |
| 821 | <a <="" a="" href="datum"> group 10" stddev="0.0018001" weight="1"><0.0538 | |
| 828 | <datum id="ms_group_10" stddev="0.0053606" weight="2">0.0902</datum> | |
| 829 | <pre><datum id="ms_group_10" stddev="0.0074037" weight="3">0.1525</datum></pre> | |
| 830 | <pre><datum id="ms_group_10" stddev="0.0027818" weight="4">0.0406</datum></pre> | |
| 831 | $<$ datum id="ms_group_10" stddev="0.0018944" weight="5">0.0224 | |
| 832 | <pre><datum id="ms_group_10" stddev="0.00071459" weight="6">0.0145</datum></pre> | |
| 833 | <pre><datum id="ms_group_10" stddev="0.00047423" weight="7">0.0061</datum></pre> | |
| 834 | <pre><datum id="ms group 10" stddev="0.00012597" weight="8">0.0008</datum></pre> | |
| 835 | <pre><datum id="ms group 10" stddev="0.00013908" weight="9">0.0003</datum></pre> | |
| 836 | <pre><datum id="ms group 11" stddev="0.0068072" weight="0">0.6718</datum></pre> | |
| 837 | <pre><datum id="ms group 11" stddev="0.0014376" weight="1">0.1094</datum></pre> | |
| 838 | <pre><datum id="ms group 11" stddey="0.0031831" weight="2">0.1562</datum></pre> | |
| 830 | $\langle datum id="ms_group_l1" stddev="0.0013378" weight="2">0.045/(datum)$ | |
| 8/0 | <pre>cdstum id="ms_group_11" stddoy="0.00152207" weight= 0.200440</pre> /datum/ | |
| 8/1 | d_{1} d_{2} d_{2} d_{3} d_{3} d_{4} d_{4 | |
| 041 | $\tau_{\rm uatum}$ rue ms_group if studev=0.00051055 Weight="5">0.0044 | |
| 842 | cuatum id="ms_group_12" stadev="0.0073209" weight="0">0.8249 | |
| 843 | $< atum id = ms_{group} 12^{"} stddev = 0.00059233" weight = 1^{"} 0.0503 < datum > 0.00059233 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.0005923 = 0.00059233 = 0.0005923 = 0.00059233 = 0.0005923 = 0.00059233 = 0.00059233 = 0.00059233 = 0.00059233 = 0.00059233 = 0.00059233 = 0.00059233 = 0.00059233 = 0.0005923 =$ | |
| 844 | $<$ datum 1d="ms_group_12" stddev="0.00095619" weight="2">0.05 | |
| 845 | <pre><datum id="ms_group_12" stddev="0.0057724" weight="3">0.0748</datum></pre> | |
| 846 | $<$ datum id="ms_group_13" stddev="0.0064421" weight="0">0.7055 | |
| 847 | <pre><datum id="ms_group_13" stddev="0.00033316" weight="1">0.1371</datum></pre> | |
| 848 | <pre><datum id="ms_group_13" stddev="0.0021757" weight="2">0.0856</datum></pre> | |
| 849 | <pre><datum id="ms group 13" stddev="0.0038007" weight="3">0.0661<!--/datum--></datum></pre> | |
| 850 | <pre><datum id="ms group 13" stddev="0.00079882" weight="4">0.0057</datum></pre> | |
| 851 | < datum id="ms group 14" stddey="0.026183" weight="0">0.632 | |
| 852 | <pre><datum id="ms_group_14" stddev="0.0036002" weight="1">0.0422</datum></pre> | |
| 853 | $d_{atum} = d_{atum} = 14$ $stddey = 0.0067108$ weight = 1/0.0122/datum/ | |
| 854 | α atum id="ms_group 14" studey="0.0007100" weight= 2">0.1012 | |
| 004 | detum id="ms_group_14" studev="0.0077767" weight= 5-20.1545 | |
| 000 | $\alpha_{1} = m_{2} m_{2} m_{1}^{2} m_{1}^{2} m_{2}^{2} m_{1}^{2} m_{1$ | |
| 856 | $<$ atum $1d = ms_{group} - 14"$ $stddev = 0.0011994"$ weight = $5">0.0247$ | |
| 857 | <pre><datum id="ms_group_14" stddev="0.00091415" weight="6">0.0145</datum></pre> | |
| 858 | $<$ datum $1d = ms_{group} 14$ " stddev="0.0006957" weight="7">0.0055 | |
| 859 | <pre><datum id="ms_group_14" stddev="0.00012668" weight="8">0.0016</datum></pre> | |
| 860 | $<$ datum id="ms_group_14" stddev="0.00019422" weight="9">0.0001 | |
| 861 | <pre><datum id="ms_group_15" stddev="0.0076514" weight="0">0.7464</datum></pre> | |
| 862 | $<$ datum id="ms_group_15" stddev="0.001291" weight="1">0.0185 | |

A. Appendix for Strain Engineering

```
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871
                                                      </simulation>
872
                                        </configuration>
873 </ fluxml>
```

A.2.5. Constraint-based Assessment of Taxadiene Production Potential

Table A.9 contains confidence intervals for the taxadiene export reaction, calculated using the method described in Section 2.1.2

Table A.9.: Confidence Intervals for Taxadiene Production Flux Calculated Considering ¹³C Labeling Data and Exchange Rates. Minimal and maximal production flux were calculated using an iterative approach. Taxadiene flux was increased (or decreased) until the squared sum of residuals (SSR) surpassed a boundary defined by the minimal SSR + 3.84. Refer to Section 2.1.2 for details. Mean taxadiene production rate was calculated as follows: $10^{(log10(min)+log10(max))/2}$. min and max refer to the minimal and maximal taxadiene flux, respectively.

| | Р | roduction Ra | te | Production Yield | | | | |
|--------------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|--|--|
| | [1 | mmol/gDW h | 1] | [mol/mol] | | | | |
| | min | mean | max | min | mean | max | | |
| HMS_2p | 1.464×10^{-7} | 1.824×10^{-5} | 2.273×10^{-3} | 3.240×10^{-8} | 4.037×10^{-6} | 5.030×10^{-4} | | |
| $\Delta xylE_2P$ | $1.739 	imes 10^{-7}$ | 2.551×10^{-5} | 3.741×10^{-3} | 3.068×10^{-8} | 4.500×10^{-6} | 6.600×10^{-4} | | |
| $\Delta xylE_1P$ | 1.385×10^{-7} | 2.431×10^{-4} | 4.267×10^{-1} | 1.629×10^{-8} | 2.860×10^{-5} | 5.020×10^{-2} | | |
| $\Delta ptsG_2P$ | $1.433 	imes 10^{-7}$ | 2.421×10^{-5} | 4.092×10^{-3} | 2.528×10^{-8} | 4.272×10^{-6} | 7.220×10^{-4} | | |
| $\Delta \text{ptsG}_1\text{P}$ | 1.412×10^{-7} | 7.279×10^{-5} | 3.751×10^{-2} | 1.977×10^{-8} | 1.019×10^{-5} | $5.250 	imes 10^{-3}$ | | |

A.3. Simultaneous Utilization of D-Xylose and Glucose in *E. coli*

A.3.1. Concentration Time Courses for All Strains

Concentration time courses for biomass, glucose, xylose and acetate for six different strains are shown in Table A.10. Measurements are provided in duplicates. Table A.11 contains experimental re-characterization of parent strains $\Delta ptsG$ Empty and HMS Empty.

A.3.2. ¹³C Labeling Data

 13 C Labeling data for the six strains used in the sugar cu-utilization studies is given in Table A.12. Experimental data was kindly provided by Claudia Huber at **Bio**.

| Time, [h] | OD | | Glucos | Glucose, [mmol/l] | | Xylose, [mmol/l] | | , [mmol/l] |
|------------|-------|-------|--------|-------------------|--------|------------------|--------|------------|
| r nne, [n] | 1 | 2 | 1 | 2 | 1 | 2 | 1 | 2 |
| | | | | HMS p1 | x | | | |
| 0 | 0.079 | 0.067 | 13.138 | 12.901 | 17.205 | 17.057 | 0.000 | 0.000 |
| 3 | 0.338 | 0.288 | 11.559 | 11.841 | 17.015 | 17.220 | 2.597 | 2.276 |
| 5 | 0.912 | 0.824 | 7.483 | 8.499 | 16.072 | 16.638 | 7.978 | 6.811 |
| 7 | 2.204 | 2.120 | 0.000 | 0.000 | 11.306 | 13.110 | 15.569 | 15.335 |
| | | | | HMS p3 | x | | | |
| 0 | 0.088 | 0.092 | 12.928 | 12.895 | 17.201 | 17.096 | 0.000 | 0.000 |
| 3 | 0.204 | 0.136 | 11.798 | 12.479 | 16.849 | 17.310 | 1.988 | 1.386 |
| 5 | 0.474 | 0.232 | 9.884 | 11.877 | 16.179 | 17.197 | 4.351 | 2.807 |
| 7 | 1.308 | 0.544 | 4.606 | 0.046 | 14.260 | 0.063 | 9.370 | 1.944 |
| | | | | $\Delta ptsG p$ | 1x | | | |
| 0 | 0.053 | 0.051 | 12.916 | 12.825 | 17.009 | 17.057 | 0.000 | 0.000 |
| 3 | 0.156 | 0.152 | 12.415 | 12.549 | 16.692 | 16.694 | 0.930 | 0.959 |
| 5 | 0.386 | 0.354 | 11.511 | 11.770 | 15.295 | 15.387 | 3.125 | 2.808 |
| 7 | 1.048 | 0.980 | 8.906 | 10.034 | 11.063 | 12.359 | 8.606 | 7.348 |
| | | | | $\Delta ptsG p$ | 3x | | | |
| 0 | 0.082 | 0.079 | 12.817 | 12.772 | 16.654 | 16.593 | 0.000 | 0.000 |
| 3 | 0.168 | 0.175 | 12.713 | 12.300 | 16.446 | 15.812 | 1.148 | 1.277 |
| 5 | 0.352 | 0.378 | 12.308 | 11.820 | 14.766 | 13.920 | 3.267 | 3.747 |
| 7 | 0.868 | 0.952 | 11.499 | 10.921 | 10.205 | 8.678 | 7.939 | 9.109 |
| | | | | HMS Em | pty | | | |
| 0 | 0.097 | 0.098 | 13.847 | 14.173 | 18.277 | 18.701 | 0.000 | 0.000 |
| 3 | 0.239 | 0.240 | 12.077 | 11.781 | 16.592 | 16.261 | 1.008 | 1.086 |
| 5 | 0.373 | 0.379 | 10.870 | 10.704 | 16.425 | 16.341 | 2.663 | 2.751 |
| 7 | 0.586 | 0.610 | 9.025 | 8.653 | 16.301 | 15.993 | 4.871 | 5.141 |
| | | | | $\Delta ptsG Em$ | pty | | | |
| 0 | 0.096 | 0.086 | 12.580 | 12.698 | 16.428 | 16.386 | 0.000 | 0.000 |
| 3 | 0.405 | 0.389 | 12.195 | 12.155 | 14.577 | 14.892 | 0.767 | 0.830 |
| 5 | 1.120 | 1.120 | 10.652 | 10.530 | 10.014 | 10.415 | 1.468 | 1.870 |
| 7 | 2.518 | 2.593 | 5.919 | 5.578 | 1.889 | 1.842 | 1.838 | 1.944 |

 Table A.10.: Concentration Time Courses For Six Strains

Table A.11.: Concentration Time Courses For Parent Strains: Re-measurements.Time, OD Glucose, [mmol/l]Xylose, [mmol/l]Acetate, [mmol/l]

| r nne, | | 0D | | Giuc | ose, min | 101/1] | Луп | se, min | .01/1J | Acetate, [mmoi/i] | | |
|--------|------------|-------|-------|--------|---------------------|---------|--------|---------|--------|-------------------|----------|--------|
| [h] | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 |
| | HMS Empty2 | | | | | | | | | | | |
| 0 | 0.107 | 0.111 | 0.109 | 13.222 | 13.197 | 13.106 | 16.681 | 16.719 | 16.419 | 0.000 | 0.000 | 0.000 |
| 1 | 0.155 | 0.158 | 0.161 | - | - | - | - | - | — | _ | - | - |
| 2 | 0.268 | 0.273 | 0.278 | _ | _ | _ | - | - | _ | _ | - | - |
| 3 | 0.511 | 0.519 | 0.543 | 10.646 | 10.676 | 10.645 | 15.936 | 16.007 | 15.981 | 2.530 | 2.363 | 2.363 |
| 4 | 0.921 | 0.935 | 0.934 | - | - | - | - | - | — | _ | - | - |
| 5 | 1.464 | 1.424 | 1.520 | 4.220 | 3.784 | 3.950 | 15.508 | 15.356 | 15.378 | 6.406 | 6.340 | 6.541 |
| 6 | 2.105 | 2.138 | 2.123 | _ | _ | _ | - | - | _ | _ | - | - |
| 7 | 2.910 | 2.830 | 3.090 | 0.000 | 0.000 | 0.000 | 5.977 | 5.632 | 5.914 | 8.728 | 8.857 | 10.051 |
| | | | | | $\Delta \mathbf{p}$ | tsG Emp | oty2 | | | | | |
| 0 | 0.064 | 0.066 | 0.060 | 13.037 | 13.104 | 13.156 | 16.318 | 16.399 | 16.354 | 0.000 | 0.000 | 0.000 |
| 1 | 0.080 | 0.076 | 0.069 | - | _ | _ | - | - | _ | _ | - | - |
| 2 | 0.105 | 0.101 | 0.092 | - | - | - | - | - | - | - | - | - |
| 3 | 0.150 | 0.147 | 0.138 | 12.514 | 12.449 | 12.492 | 15.329 | 15.207 | 15.322 | 0.000 | 0.000 | 0.000 |
| 4 | 0.242 | 0.240 | 0.216 | - | _ | _ | - | - | _ | _ | - | - |
| 5 | 0.383 | 0.360 | 0.216 | 11.530 | 11.514 | 11.584 | 12.468 | 12.740 | 12.698 | 0.981 | 0.705 | 0.644 |
| 6 | 0.533 | 0.573 | 0.331 | _ | _ | _ | — | _ | — | - | _ | _ |
| 7 | 0.930 | 0.927 | 0.535 | 8.852 | 9.004 | 9.178 | 6.660 | 6.785 | 7.072 | 2.412 | 2.327 | 1.924 |
| | | | | | | | | | | | | |

A. Appendix for Strain Engineering

| | | HMS | Empty | AntsG | Empty | HMS | n1x | HMS | n3x | Apts | - nlx | AntsG | n3x |
|----------------------|------------|-------|------------------------|-------|------------------------|-------|------------------------|-------|------------------------|-------|------------------------|-------|------------------------|
| Amino Acid | Fragment | % | σ | % | σ | % | σ | % | σ | % | σ | % | σ |
| Ala-260 | M+0 | 0.857 | 4.434E-04 | 0.923 | 6.815E-04 | 0.862 | 7.822E-03 | 0.872 | 1.802E-02 | 0.911 | 2.463E-03 | 0.949 | 3.479E-03 |
| Ala-260 | M+1 | 0.014 | 4.323E-04 | 0.010 | 8.531E-04 | 0.015 | 1.615E-03 | 0.014 | 3.245E-03 | 0.012 | 1.212E-03 | 0.008 | 2.467E-03 |
| Ala-260 Ala-260 | M+2 M+3 | 0.012 | 1.982E-04 2.618E-04 | 0.008 | 1.599E-04 4.262E-04 | 0.012 | 9.147E-04 6.218E-03 | 0.011 | 1.547E-03 1.341E-02 | 0.009 | 8.427E-04 1.532E-03 | 0.006 | 6.036E-04 6.941E-04 |
| Asp-418 | M+0 | 0.759 | 2.173E-03 | 0.859 | 2.004E-03 | 0.732 | 6.553E-03 | 0.779 | 3.910E-02 | 0.839 | 6.984E-03 | 0.904 | 4.880E-03 |
| Asp-418 | M+1 | 0.094 | 1.504E-03 | 0.065 | 2.056E-03 | 0.109 | 2.235E-03 | 0.085 | 1.946E-02 | 0.069 | 5.482E-03 | 0.045 | 4.081E-03 |
| Asp-418 | M+2 | 0.085 | 1.220E-03 | 0.047 | 8.150E-04 | 0.089 | 1.916E-03 | 0.070 | 1.188E-02 | 0.051 | 1.532E-03 | 0.031 | 1.856E-03 |
| Asp-418 | M+3 | 0.053 | 4.046E-04 | 0.026 | 2.757E-04 | 0.059 | 2.413E-03 | 0.057 | 5.596E-03 | 0.038 | 6.172E-04 | 0.020 | 7.195E-04 |
| Asp-418 Clu-432 | M+4 M+0 | 0.010 | 1.885E-04 9.711E-04 | 0.002 | 2.194E-04 2.135E-03 | 0.011 | 9.798E-04 7.060E-03 | 0.009 | 2.474E-03 3.916E-02 | 0.003 | 4.629E-04 6.844E-03 | 0.001 | 2.560E-04 4.763E-03 |
| Glu-432 | M+1 | 0.102 | 1.104E-03 | 0.066 | 2.763E-03 | 0.105 | 3.219E-03 | 0.080 | 1.564E-02 | 0.066 | 3.889E-03 | 0.042 | 2.586E-03 |
| Glu-432 | M+2 | 0.168 | 7.077E-04 | 0.097 | 7.856E-04 | 0.169 | 2.894E-03 | 0.155 | 1.501E-02 | 0.113 | 2.302E-03 | 0.073 | 2.099E-03 |
| Glu-432 | M+3 | 0.043 | 3.788E-04 | 0.016 | 6.368E-04 | 0.043 | 1.735E-03 | 0.039 | 6.558E-03 | 0.021 | 1.352E-03 | 0.011 | 8.033E-04 |
| Glu-432 | M+4 | 0.014 | 4.510E-04 | 0.003 | 1.425E-04 | 0.012 | 6.841E-04 | 0.010 | 1.588E-03 | 0.004 | 4.772E-04 | 0.002 | 2.362E-04 |
| Glu-432 Gly-246 | M+5 M+0 | 0.004 | 1.502E-04 4.280E-04 | 0.001 | 9.422E-05 6.503E-04 | 0.004 | 4.350E-04 6.000E-03 | 0.004 | 6.825E-04 1.728E-02 | 0.001 | 1.345E-04 1.366E-03 | 0.001 | 9.866E-05 8.671E-04 |
| Gly-246 | M+1 | 0.029 | 2.275E-04 | 0.016 | 6.754E-04 | 0.024 | 7.335E-04 | 0.023 | 3.172E-03 | 0.017 | 1.098E-03 | 0.011 | 8.399E-04 |
| Gly-246 | M+2 | 0.116 | 3.736E-04 | 0.059 | 3.171E-04 | 0.119 | 5.296E-03 | 0.106 | 1.414E-02 | 0.069 | 1.574E-03 | 0.039 | 4.329E-04 |
| His-440 | M+0 | 0.733 | 1.901E-03 | 0.884 | 2.267E-03 | 0.734 | 1.688E-02 | 0.755 | 3.538E-02 | 0.862 | 4.877E-03 | 0.924 | 5.207E-03 |
| His-440 | M+1 | 0.101 | 1.907E-03 | 0.061 | 2.900E-03 | 0.117 | 7.659E-03 | 0.100 | 1.684E-02 | 0.073 | 5.377E-03 | 0.040 | 4.246E-03 |
| H1s-440 | M+2 M+2 | 0.047 | 6.245E-04 5.600E-04 | 0.010 | 8.228E-04 | 0.038 | 3.513E-03 | 0.039 | 5.358E-03 | 0.011 | 3.966E-03 | 0.005 | 1.542E-03 |
| His-440 | M+4 | 0.000 | 8.053E-05 | 0.034 | 2.328E-04 | 0.003 | 6.548E-04 | 0.030 | 2 713E-03 | 0.034 | 4 954E-04 | 0.020 | 2 723E-04 |
| His-440 | M+5 | 0.035 | 1.938E-04 | 0.009 | 1.505E-04 | 0.034 | 2.394E-03 | 0.035 | 3.920E-03 | 0.016 | 6.045E-04 | 0.009 | 3.208E-04 |
| His-440 | M+6 | 0.005 | 2.197E-04 | 0.000 | 8.030E-05 | 0.003 | 4.935E-04 | 0.004 | 8.892E-04 | 0.001 | 2.352E-04 | 0.000 | 9.922E-05 |
| Ile-200 | M+0 | 0.696 | 5.368E-04 | 0.822 | 2.101E-03 | 0.667 | 8.884E-03 | 0.718 | 4.259E-02 | 0.800 | 5.154E-03 | 0.880 | 1.920E-03 |
| Ile-200 | M+1 | 0.091 | 6.325E-04 | 0.065 | 7.628E-04 | 0.107 | 8.431E-04 | 0.080 | 1.733E-02 | 0.065 | 2.342E-03 | 0.044 | 1.495E-03 |
| IIe-200 II.e. 200 | M+2 M+2 | 0.159 | 1.729E-04 | 0.095 | 1.175E-03 | 0.169 | 0.299E-03 | 0.152 | 1.673E-02 6.227E-02 | 0.110 | 1.869E-03 | 0.065 | 1.264E-03 |
| Ile-200 | M+3 M+4 | 0.038 | 9.602E-05 | 0.015 | 5.270E-05 | 0.043 | 1.695E-03 6.609E-04 | 0.038 | 0.337E-03 | 0.020 | 9.165E-04 1.829E-04 | 0.010 | 4 447E-04 |
| Ile-200 | M+5 | 0.004 | 7.405E-05 | 0.001 | 1.921E-05 | 0.004 | 2.223E-04 | 0.004 | 6.733E-04 | 0.001 | 4.360E-05 | 0.000 | 3.346E-05 |
| Leu-274 | M+0 | 0.686 | 1.351E-03 | 0.815 | 1.756E-03 | 0.660 | 1.238E-02 | 0.699 | 3.836E-02 | 0.787 | 6.876E-03 | 0.872 | 2.491E-03 |
| Leu-274 | M+1 | 0.091 | 1.444E-03 | 0.063 | 1.025E-03 | 0.108 | 2.958E-03 | 0.090 | 1.214E-02 | 0.072 | 4.123E-03 | 0.048 | 2.318E-03 |
| Leu-274 | M+2 | 0.174 | 7.278E-04 | 0.110 | 1.024E-03 | 0.185 | 8.551E-03 | 0.168 | 2.012E-02 | 0.123 | 2.135E-03 | 0.074 | 2.662E-03 |
| Leu-274 Leu-274 | M+3 M+4 | 0.031 | 5.213E-04 | 0.008 | 3.440E-04 | 0.031 | 1.790E-03 | 0.027 | 3.714E-03 | 0.012 | 7.280E-04 | 0.004 | 3.840E-04 |
| Leu-274 | M+5 | 0.013 | 5.968E-05 | 0.004 | 3 242E-05 | 0.013 | 2.514E-04 | 0.013 | 4.332E-04 | 0.003 | 8.311E-05 | 0.002 | 6 790E-05 |
| Lys-431 | M+0 | 0.684 | 2.154E-03 | 0.814 | 3.905E-03 | 0.649 | 9.282E-03 | 0.706 | 4.289E-02 | 0.786 | 5.965E-03 | 0.878 | 4.303E-03 |
| Lys-431 | M+1 | 0.088 | 1.194E-03 | 0.065 | 2.772E-03 | 0.104 | 3.735E-03 | 0.078 | 1.464E-02 | 0.067 | 3.613E-03 | 0.041 | 2.937E-03 |
| Lys-431 | M+2 | 0.115 | 9.071E-04 | 0.071 | 8.617E-04 | 0.124 | 3.645E-03 | 0.106 | 1.270E-02 | 0.081 | 2.679E-03 | 0.049 | 1.403E-03 |
| Lys-431 | M+3 | 0.087 | 4.226E-04 | 0.049 | 6.542E-04 | 0.097 | 3.485E-03 | 0.089 | 9.894E-03 | 0.061 | 8.854E-04 | 0.036 | 7.789E-04 |
| Lys-431 | M+4 | 0.016 | 3.977E-04 | 0.001 | 2.095E-04 | 0.016 | 1.410E-03 | 0.013 | 4.230E-03 | 0.003 | 8.854E-04 | 0.000 | 0.000E+00 |
| Lys-431 Lys-431 | M+5 M+6 | 0.009 | 1.788E-04 1.761E-04 | 0.001 | 0.000E+00 | 0.009 | 0.025E-04 | 0.008 | 1.241E-03 5.612E-04 | 0.002 | $0.000E \pm 00$ | 0.000 | 1.804E-04 0.000E+00 |
| Met-320 | M+0 | 0.688 | 6.278E-03 | 0.810 | 1.531E-03 | 0.641 | 6.083E-03 | 0.699 | 4.676E-02 | 0.779 | 2.572E-03 | 0.867 | 4.377E-03 |
| Met-320 | M+1 | 0.157 | 2.158E-03 | 0.110 | 8.997E-04 | 0.183 | 2.847E-03 | 0.153 | 2.554E-02 | 0.122 | 3.064E-03 | 0.077 | 3.042E-03 |
| Met-320 | M+2 | 0.085 | 1.476E-03 | 0.050 | 7.271E-04 | 0.094 | 2.713E-03 | 0.075 | 1.216E-02 | 0.055 | 1.376E-03 | 0.034 | 2.034E-03 |
| Met-320 | M+3 | 0.054 | 2.044E-03 | 0.026 | 5.467E-04 | 0.062 | 3.083E-03 | 0.056 | 7.303E-03 | 0.038 | 9.150E-04 | 0.020 | 6.745E-04 |
| Met-320 Met-220 | M+4 M+5 | 0.014 | 1.527E-03 | 0.004 | 1.150E-04 | 0.018 | 1.157E-03 | 0.016 | 3.445E-03 | 0.006 | 4.056E-04 | 0.002 | 6.650E-04 |
| Phe-336 | M+0 | 0.642 | 1.271E-03 | 0.000 | 2.399E-03 | 0.617 | 1.612E-02 | 0.003 | 4 447E-02 | 0.001 | 4.030E-03 | 0.000 | 1.993E-03 |
| Phe-336 | M+1 | 0.052 | 1.013E-03 | 0.030 | 2.031E-03 | 0.056 | 1.962E-03 | 0.050 | 5.393E-03 | 0.038 | 1.818E-03 | 0.029 | 8.042E-04 |
| Phe-336 | M+2 | 0.082 | 8.989E-04 | 0.056 | 1.319E-03 | 0.090 | 4.457E-03 | 0.082 | 9.137E-03 | 0.064 | 1.558E-03 | 0.039 | 8.560E-04 |
| Phe-336 | M+3 | 0.133 | 7.613E-04 | 0.087 | 8.181E-04 | 0.152 | 5.832E-03 | 0.135 | 1.564E-02 | 0.101 | 2.051E-03 | 0.060 | 5.451E-04 |
| Phe-336 | M+4 | 0.046 | 3.019E-04 | 0.014 | 8.085E-04 | 0.041 | 2.258E-03 | 0.040 | 7.047E-03 | 0.017 | 6.505E-04 | 0.010 | 6.233E-04 |
| Phe-336 | M+5 M+6 | 0.022 | 2.690E-04 2.696E-04 | 0.000 | 2.474E-04 2.875E-04 | 0.022 | 1.509E-05 6.457E-04 | 0.020 | 3.410E-03 | 0.008 | 2.044E-04 2.063E-04 | 0.003 | 1.027E-04 1.151E-04 |
| Phe-336 | M+0 M+7 | 0.013 | 2.078E-04 | 0.003 | 1.386E-04 | 0.004 | 3.811E-04 | 0.006 | 1.305E-03 | 0.004 | 7.124E-05 | 0.001 | 7.881E-05 |
| Phe-336 | M+8 | 0.001 | 1.836E-04 | 0.000 | 0.000E + 00 | 0.001 | 1.154E-04 | 0.001 | 2.278E-04 | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 |
| Phe-336 | M+9 | 0.000 | 5.768E-05 | 0.000 | 0.000E + 00 | 0.000 | 1.492E-04 | 0.000 | 2.029E-04 | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 |
| Pro-286 | M+0 | 0.701 | 3.194E-03 | 0.824 | 5.201E-03 | 0.672 | 6.054E-03 | 0.725 | 4.085E-02 | 0.800 | 5.682E-03 | 0.876 | 2.853E-03 |
| Pro-286 Pro-286 | M+1 M+2 | 0.095 | 1.727E-03 | 0.067 | 1.498E-03 2.745E-02 | 0.109 | 3.772E-03 | 0.083 | 1.548E-02 | 0.072 | 2.381E-03 3.110E-02 | 0.049 | 1.832E-03 1.723E-02 |
| Pro-286 | M+3 | 0.039 | 6.929E-04 | 0.017 | 5.813E-04 | 0.045 | 2.061E-03 | 0.039 | 6.088E-03 | 0.038 | 1.004E-03 | 0.012 | 2.514E-04 |
| Pro-286 | M+4 | 0.015 | 4.270E-04 | 0.006 | 9.635E-04 | 0.014 | 6.830E-04 | 0.012 | 1.992E-03 | 0.006 | 2.702E-04 | 0.004 | 1.736E-04 |
| Pro-286 | M+5 | 0.004 | 3.393E-04 | 0.001 | 2.084E-04 | 0.004 | 3.092E-04 | 0.004 | 6.673E-04 | 0.001 | 1.323E-04 | 0.000 | 4.366E-05 |
| Ser-390 | M+0 | 0.851 | 2.035E-03 | 0.915 | 4.296E-03 | 0.825 | 6.231E-03 | 0.844 | 1.950E-02 | 0.903 | 2.932E-03 | 0.951 | 3.158E-03 |
| Ser-390 Ser-390 | M+1 M+2 | 0.030 | 1.424E-03 6.824E-04 | 0.024 | 3.353E-03 | 0.050 | 2.335E-03 | 0.044 | 5.015E-03 | 0.025 | 2.248E-03 1.007E-02 | 0.010 | 2.810E-03 0.845E-04 |
| Ser-390 | M+3 | 0.027 | 5.789E-04 | 0.022 | 3.264E-04 | 0.030 | 4.658E-03 | 0.044 | 9.498E-03 | 0.025 | 1.092E-03 | 0.015 | 9.457E-04 |
| Thr-404 | M+0 | 0.748 | 2.060E-03 | 0.854 | 2.469E-03 | 0.706 | 5.359E-03 | 0.757 | 3.921E-02 | 0.820 | 5.313E-03 | 0.884 | 3.150E-03 |
| Thr-404 | M+1 | 0.107 | 2.375E-03 | 0.075 | 1.708E-03 | 0.137 | 1.468E-03 | 0.109 | 2.137E-02 | 0.091 | 4.376E-03 | 0.070 | 3.007E-03 |
| Thr-404 | M+2 | 0.086 | 9.052E-04 | 0.051 | 1.410E-03 | 0.086 | 2.303E-03 | 0.068 | 9.309E-03 | 0.052 | 9.058E-04 | 0.033 | 2.075E-03 |
| Thr-404 Thr-404 | M+3 M+4 | 0.056 | 5.606E-04 | 0.027 | 5.265E-04 | 0.066 | 3.540E-03 | 0.063 | 6.060E-03 | 0.041 | 7.682E-04 | 0.021 | 5.521E-04 |
| 1 nr-404 Tyr-466 | M+4 M+0 | 0.003 | 2.105E-04 1.863E-03 | 0.000 | 9.147E-04 | 0.006 | 9.944E-04 2.031E_02 | 0.003 | 2.804E-03 4.609E-02 | 0.000 | 0.000E+00 4.795E-03 | 0.000 | 0.000E+00 2.872E-03 |
| Tyr-466 | M+1 | 0.046 | 1.459E-03 | 0.027 | 1.489E-03 | 0.042 | 3.027E-03 | 0.039 | 6.364E-03 | 0.027 | 3.973E-03 | 0.018 | 2.979E-03 |
| Tyr-466 | M+2 | 0.092 | 5.484E-04 | 0.064 | 1.033E-03 | 0.101 | 5.269E-03 | 0.093 | 9.656E-03 | 0.076 | 1.009E-03 | 0.047 | 1.577E-03 |
| Tyr-466 | M+3 | 0.123 | 5.727E-04 | 0.082 | 1.102E-03 | 0.134 | 6.144E-03 | 0.120 | 1.457E-02 | 0.092 | 2.246E-03 | 0.054 | 1.725E-03 |
| Tyr-466 | M+4 | 0.048 | 7.538E-04 | 0.014 | 3.424E-04 | 0.044 | 3.848E-03 | 0.043 | 7.657E-03 | 0.018 | 6.630E-04 | 0.010 | 3.478E-04 |
| Tyr-466 | M+5 M+6 | 0.023 | 2.528E-04 | 0.007 | 3.071E-04 | 0.025 | 1.051E-03 | 0.022 | 4.055E-03 | 0.010 | 3.860E-04 | 0.005 | 2.842E-04 |
| 1 yr-400 Twr-466 | M+7 | 0.015 | 0.942E-04 0.654E-05 | 0.003 | 2.138E-04 3.239E-04 | 0.014 | 6.003E-04 | 0.013 | 2.520E-03 1.250E-02 | 0.004 | 3.445E-04 2.321E-04 | 0.002 | 2.499E-04 0.000E±00 |
| Tyr-466 | M+8 | 0.002 | 3.199E-04 | 0.001 | 2.073E-04 | 0.002 | 1.771E-04 | 0.001 | 3.939E-04 | 0.000 | 1.766E-04 | 0.000 | 2.294E-04 |
| Tyr-466 | M+9 | 0.011 | 1.191E-03 | 0.004 | 1.561E-03 | 0.000 | 1.992E-04 | 0.000 | 3.418E-04 | 0.000 | 0.000E + 00 | 0.000 | 0.000E + 00 |
| Val-288 | M+0 | 0.762 | 9.275E-04 | 0.866 | 1.169E-03 | 0.746 | 6.127E-03 | 0.776 | 2.854E-02 | 0.840 | 3.709E-03 | 0.911 | 5.684E-04 |
| Val-288 | M+1 | 0.012 | 1.179E-03 | 0.011 | 8.885E-04 | 0.019 | 1.040E-03 | 0.012 | 1.968E-03 | 0.015 | 2.079E-03 | 0.009 | 1.205E-03 |
| Val-288 | M+2 M+2 | 0.109 | 8.820E-04 | 0.064 | 6.511E-04 | 0.115 | 3.756E-03 | 0.104 | 1.338E-02 | 0.075 | 1.592E-03 | 0.043 | 1.093E-03 |
| vai-288 Val-288 | M+4 | 0.098 | 1.895E-04 | 0.054 | 3.038E-04 8.993E-05 | 0.102 | 2.8/8E-03 6.047E-04 | 0.091 | 4.148E-02 | 0.063 | 8.085E-04 1.915E-04 | 0.035 | 0.845E-04 1.252E-04 |
| Val-288 | M+5 | 0.017 | 1.678E-04 | 0.004 | 5.224E-05 | 0.016 | 6.222E-04 | 0.014 | 2.237E-03 | 0.005 | 2.256E-04 | 0.002 | 8.943E-05 |

 Table A.12.:
 ¹³C-labeling Data for Strains Used in Sugar Co-Utilization Studies.

 Labeling patterns of protein-bound amino acids was experimentally determined in duplicate

for six strains exhibiting different values for % Carbon Xylose.



Figure A.8.: Estimation of Oxygen Uptake Rate as a Function of Sugar Co-Uptake. Overall, we observe a decrease in the oxygen uptake rate, as % Carbon Xylose increases. For strain HMS p3x, its unusually high substrate uptake (refer to Figure 6.1.C) leads to an *in silico* oxygen uptake rate of zero.

A.3.3. Dependency of Oxygen Uptake Rate on Sugar Co-Utilization

Figure A.8 shows the dependence of *in silico estimated* oxygen uptake for strain families HMS and Δ ptsG on the extent of experimentally determined xylose and glucose coutilization. Oxygen uptake rate for each strain is estimated by minimizing the reaction representing oxygen import from the medium to the cell, while simultaneously constraining reactions in the iJO1366 model representing rates for growth, glucose and xylose uptake, and acetate secretion to match experimentally determined values, as listed in Table 6.2. The biological feasibility of minimization of oxygen uptake as objective function is discussed in Chapter 4.

A.3.4. Experimental Protein Content

Total protein content was experimentally determined in two rounds. In the first round, strains carrying mutated XylE transporters were characterized. In a second round, total protein content of respective parent strains carrying an empty plasmid was determined. Results are shown in Figure A.9.A and B., respectively. Overall, we observe an increase in the total protein content as % Carbon Xylose increases. Additionally, strain family Δ ptsG exhibits a higher total protein content compared to protein contents measured for the strain family XylE. Since the 2-D Quant Kit (provided by GE Healthcare) used for protein measurement is an indirect method, it requires the simultaneous measurement of a protein standard. Thus, absolute protein content might vary between experimental rounds, which is the case for protein levels within the strain family Δ ptsG Empty < Δ ptsG plx < Δ ptsG p3x. By contrast, the observed trend is as follows: Δ ptsG p1x < Δ ptsG Empty exhibits a higher protein content than both daughter strains, we conclude that observed deviations are originated because protein content for strain Δ ptsG Empty was determined

A. Appendix for Strain Engineering

independently from $\Delta ptsG p1x$ and $\Delta ptsG p3x$. Consequently, protein measurements should be repeated for all strains using the same protein standard and experimental set up.



Figure A.9.: **Protein Measurement.** Total protein content for strains carrying XylE mutant transporters in two different genetic backgrounds (A.) and corresponding parent strains (B.). Protein content was determined using the 2-D Quant Kit provided by GE Healthcare for the two strain groups separately.

B.1. Model-based Medium Optimization

B.1.1. Extending Metabolic Models to Allow Taxadiene Synthesis

E. coli Core

The code shown below was used to extend the *E. coli* core model to enable taxadiene production using the non-mevalonate pathway, the mevalonate pathway or both.

```
% Load core model.
model=readCbModel('ecoli_core_model.xml');
 2
 6~\% Add reactions of the MEP pathway. 7~\%
13 % Reaction 2. ispC
 \begin{array}{ll} 14 & \texttt{model}=\texttt{addReaction(model,`ispC`,`dxyl5p[c] + nadph[c] + h[c] -> nadp[c] + 2me4p[c]`);} \\ 15 \end{array} 
16 % Reaction 3. ispD
17
  model=addReaction(model,'ispD',' 2me4p[c] + atp[c] + h[c] -> 4c2me[c] + 2 pi[c] '); %Eigentlich
      ist die Reaktion mit CTP.
18
19 % Reaction 4. ispE
20 model=addReaction(model, 'ispE', '4c2me[c] + atp[c] \rightarrow 2p4c2me[c] + adp[c] + h[c] ');
21
22~\% Reaction 5. ispF
23 model=addReaction(model,'ispF',' 2p4c2me[c] -> 2mecdp[c] + amp[c] ');
24
25 % Reaction 6. ispG
 \begin{array}{l} 26 \\ model=addReaction(model,'ispG',' 2mecdp[c] + nadh[c] -> h2mb4p[c] + h2o[c] + nad[c] '); \\ 27 \end{array} 
28 % Reaction 7. ispH
29 model=addReaction(model, 'ispH', ' h2mb4p[c] + nadh[c] + h[c] \rightarrow dmpp[c] + h2o[c] + nad[c] ');
30
31 % Reaction 8. ispH2
32 model=addReaction(model,'ispH2',' h2mb4p[c] + nadh[c] + h[c] -> ipdp[c] + h2o[c] + nad[c] ');
33
34 % Reaction 9. idi
35 model=addReaction(model, 'idi', 'dmpp[c] <=> ipdp[c]');
36
37
  38
39
  \% Add reactions of the MVA pathway.
40
41
  42
43
44 % Reaction 1. - synthesis of Acetoacetyl.
45 model=addReaction(model,'atoB','2 accoa[c] -> aacoa[c] + coa[c]');
46
47 %Reaction 2. - synthesis of HMGCoA.
48 model=addReaction(model, 'pksg', 'aac
                                  acoa[c] + accoa[c] + h2o[c] -> h[c] + coa[c] + hmgcoa[c]');
49
53 %Reaction
                 synthesis
                          of MVAP
54 model=addReaction(model, 'mvakl', 'mva[c] + atp[c] -> adp[c] + h[c] mvap[c]');
56 %Reaction 5 -
  %Reaction 5 - synthesis of MVAPP
model=addReaction(model, 'mvak2', 'mvap[c] + atp[c] -> adp[c] + mvapp[c]');
58
```

```
59 %Reaction 6 - synthesis of IPP
   \label{eq:model_addReaction(model, `mvad', `mvapp[c] + atp[c] -> adp[c] + co2[c] + pi[c] + ipdp[c]');
60
   62
63
   \% % Add taxadiene synthesis from IPP (ipdp) and DMAPP (dmpp)
64
65
  67
   %Reaction 1. - synthesis of Geranyl diphosphate
model=addReaction(model, 'DMATT', ' dmpp[c] + ipdp[c] -> grdp[c] + 2 pi[c] ');
   %Reaction
68
69
70
71
72
   %Reaction 2. - synthesis of Farnesyl diphosphate
model=addReaction(model,'GRTT',' grdp[c] + ipdp[c] -> frdp[c] + 2 pi[c] ');
73 \\ 74
  %Reaction 3. - synthesis of GGPP
75
76
   model=addReaction(model, 'ggpps', 'frdp[c] + ipdp[c] -> ggpp[c] + 2 pi[c]');
76
77 %Reaction 4. - synthesis of taxadiene
78 model=addReaction(model, 'txs', 'ggpp[c] \rightarrow txdn[c] + 2 pi[c]');
79
   %Reaction 5. - export reaction for taxadiene
model=addReaction(model,'txdnx','txdn[c] -> '); %txdn[e]
80 %Reaction
81
```

E. coli iJO1366

The code shown below was used to extend the *E. coli* genome-scale metabolic reconstruction iJO1366 to enable taxadiene production using the non-mevalonate pathway, the mevalonate pathway or both. Note that the non-mevalonate pathway is an endogenous pathway and thus already contained in the iJO1366 model. Reactions DXPIi, MEPCT, CDPMEX, MECDPS, MECDPDH2, DMPPS, IPDPS should be deleted if theoretical calculations using the mevalonate pathway for taxadiene synthesis are to be performed.

```
% Load Genome Scale Metabolic Reconstruction
      model0=readCbModel('iJO1366.xml');
      %NGAM modification
      model0=changeRxnBounds(model0, 'ATPM', 0, 'b');
      8
  9
      %Control activity of endogeneous MEP Pathway.
\begin{array}{c} 10 \\ 11 \end{array}
      12
13
       if 1 = = 0
                                                               'MEPCT', 'CDPMEX', 'MECDPS', 'MECDPDH2', 'DMPPS', 'IPDPS'};
       rxnRemoveList={ 'DXPIi ',
14
15
       model0=removeRxns(model0, rxnRemoveList);
      end
      18
19
      %Add MVA Pathway. This pathway is composed of 6 reactions.
20
21
     22
23
24
      if 1 == 1 \% MVA aktiv?
      %Reaction 1. - synthesis of Acetoacetyl-coA, is already contained in the
26
27
      %model.
28
29 %Reaction 2. - synthesis of HMGCoA.
      model0 = addReaction(model0, 'pksg', 'aacoa[c] + accoa[c] + h2o[c] -> h[c] + coa[c] + hmgcoa[c]');
30
31
32
     %Reaction 3. - synthesis of MVA
       model0 = addReaction (model0, 'hmgl', 'hmgcoa[c] + 2 nadph[c] + 2 h[c] -> 2 nadp[c] + coa[c] + mva[c] 'hmgcoa[c] + mva[c] + mva[c] 'hmgcoa[c] + mva[c] 'hmgcoa[c] + mva[c] + mva[c] 'hmgcoa[c] + mva[c] 'hmgcoa[c] + mva[c] 'hmgcoa[c] + mva[c] + mva[c] 'hmgcoa[c] + mva[c] + 
                 );
34
35 %Reaction 4. - synthesis of MVAP
      model0=addReaction(model0, 'mvak1', 'mva[c] + atp[c] -> adp[c] + h[c] mvap[c]');
36
     %Reaction 5. - synthesis of MVAPP
38
39
      model0=addReaction(model0, 'mvak2', 'mvap[c] + atp[c] -> adp[c] + mvapp[c]');
40
41
      %Reaction 6.
                                            synthesis
                                                                  of IPP
      model0=addReaction(model0, 'mvad', 'mvapp[c] + atp[c] -> adp[c] + co2[c] + pi[c] + ipdp[c]');
42
43
44
      end
45
     MANTERSTER STERETERSTERETERSTERETERSTERETERSTERETERSTERETERSTERETERSTERETERSTERETERSTERETERSTERETERSTERETERSTE
46
48 %Taxadiene Synthesis
```

B.1.2. Ranking of 180 Substrates According to Yields

Table B.1 provides maximal theoretical taxadiene yields for 180 different growth supporting carbon sources. Two different network configurations are considered. In the first case, IPP and DMAPP synthesis can occur only via the non-mevalonate pathway. In the second case, both the mevalonate and the non-mevalonate pathway are considered. For each substrate and the non-mevalonate pathway, yields are reported in three different basis. When both pathways are considered, only carbon yield is reported. Synergy is calculated as explained in the main text.

| | (MEP+MVA) is also provid | ed. For a | ll calculat | ions, NO | GAM and growt | th rate wer | e set to 0. |
|-----|--|-----------|-------------|----------|---------------|-------------|-------------|
| Nr | Carbon Source | Non-M | evalonate I | Pathway | MEP+MVA. | Synergy, | Best |
| 141 | Garbon Source | Molar | Carbon | Mass | Carbon Yield | [%] | Pathway |
| 1 | Ethanol exchange | 0.088 | 0.879 | 0.519 | 0.925 | 5.205 | MEP+MVA |
| 2 | Glycerophosphoglycerol exchange | 0.250 | 0.833 | 0.278 | 0.833 | 0.000 | MEP |
| 3 | Glycerol 3-phosphate exchange | 0.125 | 0.833 | 0.200 | 0.833 | 0.000 | MEP |
| 4 | sn-Glycero-3-phosphoethanolamine ex- | 0.204 | 0.815 | 0.258 | 0.828 | 1.699 | MEP+MVA |
| | change | | | | | | |
| 5 | Glycerol exchange' | 0.121 | 0.804 | 0.356 | 0.805 | 0.188 | MEP+MVA |
| 6 | Glycerol 2-phosphate exchange | 0.121 | 0.804 | 0.193 | 0.805 | 0.188 | MEP+MVA |
| 7 | Putrescine exchange | 0.159 | 0.793 | 0.479 | 0.793 | 0.000 | MEP |
| 8 | (S)-Propane-1,2-diol exchange | 0.113 | 0.755 | 0.405 | 0.765 | 1.275 | MEP+MVA |
| 9 | Acetaldehyde exchange | 0.074 | 0.742 | 0.459 | 0.798 | 0.000 | MVA |
| 10 | D-Mannitol exchange | 0.220 | 0.735 | 0.329 | 0.740 | 0.696 | MEP+MVA |
| 11 | D-Sorbitol exchange | 0.220 | 0.735 | 0.329 | 0.740 | 0.696 | MEP+MVA |
| 12 | Galactitol exchange | 0.220 | 0.733 | 0.328 | 0.740 | 1.016 | MEP+MVA |
| 13 | Ethanolamine exchange | 0.072 | 0.723 | 0.317 | 0.777 | 0.000 | MVA |
| 14 | Propanal exchange | 0.108 | 0.718 | 0.505 | 0.731 | 1.723 | MEP+MVA |
| 15 | D-Glucose 6-phosphate exchange | 0.213 | 0.711 | 0.225 | 0.714 | 0.420 | MEP+MVA |
| 16 | D-Mannose 6-phosphate exchange | 0.213 | 0.711 | 0.225 | 0.714 | 0.420 | MEP+MVA |
| 17 | D-fructose 6-phosphate exchange | 0.213 | 0.711 | 0.225 | 0.714 | 0.420 | MEP+MVA |
| 18 | D-Glucosamine 6-phosphate exchange | 0.213 | 0.711 | 0.225 | 0.714 | 0.420 | MEP+MVA |
| 19 | Maltohexaose exchange | 1.259 | 0.700 | 0.346 | 0.704 | 0.555 | MEP+MVA |
| 20 | 1.4-alpha-D-glucan exchange | 1.259 | 0.700 | 0.346 | 0.704 | 0.555 | MEP+MVA |
| 21 | D-Glyceraldehyde exchange | 0.105 | 0.698 | 0.316 | 0.706 | 1.224 | MEP+MVA |
| 22 | Glycerophosphoserine exchange | 0.209 | 0.697 | 0.221 | 0.705 | 1.092 | MEP+MVA |
| 23 | Maltopentaose exchange | 1.044 | 0.696 | 0.343 | 0.700 | 0.600 | MEP+MVA |
| 24 | Sucrose exchange | 0.414 | 0.690 | 0.329 | 0.695 | 0.667 | MEP+MVA |
| 25 | Trehalose exchange | 0.414 | 0.690 | 0.329 | 0.695 | 0.667 | MEP+MVA |
| 26 | Dihydroxyacetone exchange | 0.104 | 0.690 | 0.313 | 0.695 | 0.667 | MEP+MVA |
| 28 | Maltotriose exchange | 0.621 | 0.690 | 0.335 | 0.695 | 0.667 | MEP+MVA |
| 27 | Maltose exchange | 0.414 | 0.690 | 0.329 | 0.695 | 0.667 | MEP+MVA |
| 29 | Maltotetraose exchange | 0.828 | 0.690 | 0.338 | 0.695 | 0.667 | MEP+MVA |
| 30 | D-Glucose 1-phosphate exchange | 0.207 | 0.690 | 0.218 | 0.695 | 0.738 | MEP+MVA |
| 31 | D-Glucose exchange' | 0.207 | 0.690 | 0.313 | 0.695 | 0.738 | MEP+MVA |
| 32 | D-Fructose exchange | 0.207 | 0.689 | 0.312 | 0.695 | 0.871 | MEP+MVA |
| 33 | D-Mannose exchange | 0.207 | 0.689 | 0.312 | 0.695 | 0.871 | MEP+MVA |
| 34 | D-Glucosamine exchange | 0.207 | 0.689 | 0.312 | 0.695 | 0.871 | MEP+MVA |
| 35 | Melibiose exchange | 0.412 | 0.687 | 0.328 | 0.692 | 0 709 | MEP+MVA |
| 36 | Lactose exchange | 0.412 | 0.687 | 0.328 | 0.692 | 0.709 | MEP+MVA |
| 37 | beta D-Galactose exchange | 0.205 | 0.683 | 0.310 | 0.689 | 0.753 | MEP+MVA |
| 38 | D-Galactose exchange | 0.205 | 0.683 | 0.310 | 0.689 | 0.753 | MEP+MVA |
| 39 | alpha-D-Galactose 1-phosphate exchange | 0.205 | 0.683 | 0.216 | 0.689 | 0 753 | MEP+MV4 |
| 40 | L-Lyxose exchange | 0.171 | 0.682 | 0.309 | 0.687 | 0.770 | MEP+MVA |
| 41 | L-Xylulose exchange | 0 171 | 0.682 | 0.309 | 0.687 | 0.770 | MEP+MVA |
| 42 | L-Arabinose exchange | 0.171 | 0.682 | 0.309 | 0.687 | 0.770 | MEP+MVA |
| 43 | D-Xylose exchange | 0.171 | 0.682 | 0.309 | 0.687 | 0.770 | MEP+MVA |
| 44 | L-Rhamnose exchange | 0.204 | 0.679 | 0.338 | 0.685 | 0.867 | MEP+MVA |

 Table B.1.: Maximal Taxadiene Yields Calculated for 180 Carbon Sources. The

 E. coli metabolic reconstruction iJO1366 was used for all calculations. Yields are reported

 for the non-mevalonate pathway (MEP). For synergy calculation, the iJO1366 model was

 expanded to consider the mevalonate (MVA) pathway. Synergy was calculated as explained

 in the main text. Refer to Section 7.2. Carbon yield for the simultaneous pathway usage

 (MEP+MVA) is also provided. For all calculations, NGAM and growth rate were set to 0.

 Non-Mevalonate Pathway

 MEP+MVA.

 Synergy.

 Best

| | Table B. | 1 Continu | ied from pr | evious p | age | | |
|-----|---|-----------|-------------|----------|--------------|----------|-----------------|
| Nr | Carbon Source | Non M | evalonate F | Pathway | MEP+MVA. | Synergy, | Best |
| | | Molar | Carbon | Mass | Carbon Yield | [%] | Pathway |
| 45 | L-Fucose exchange | 0.204 | 0.679 | 0.338 | 0.685 | 0.867 | MEP+MVA |
| 46 | 4-Aminobutanoate exchange | 0.134 | 0.672 | 0.355 | 0.672 | 0.000 | MEP |
| 47 | D-Allose exchange | 0.199 | 0.662 | 0.300 | 0.668 | 0.878 | MEP+MVA |
| 48 | chitobiose exchange | 0.528 | 0.660 | 0.339 | 0.672 | 1.712 | MEP+MVA |
| 49 | D-Ribose exchange | 0.164 | 0.657 | 0.298 | 0.663 | 0.866 | MEP+MVA |
| 50 | alpha-D-Ribose 5-phosphate exchange | 0.164 | 0.657 | 0.196 | 0.663 | 0.866 | MEP+MVA |
| 51 | N-Acetyl-D-glucosamine(anhydrous)N- | 0.623 | 0.656 | 0.355 | 0.667 | 1.575 | MEP+MVA |
| 52 | Acetylmuramic acid exchange N-Acetyl-D-glucosamine 1-phosphate ex- | 0.262 | 0.654 | 0.238 | 0.672 | 2.646 | MEP+MVA |
| | change | | | | | | |
| 53 | N-Acetyl-D-mannosamine exchange | 0.262 | 0.654 | 0.322 | 0.672 | 2.646 | MEP+MVA |
| 54 | N-Acetyl-D-glucosamine exchange | 0.262 | 0.654 | 0.322 | 0.672 | 2.646 | MEP+MVA |
| 55 | N-Acetylmuramate exchange | 0.355 | 0.646 | 0.331 | 0.665 | 2.963 | MEP+MVA |
| 56 | 2(alpha-D-Mannosyl)-D-glycerate exchange | 0.290 | 0.644 | 0.295 | 0.649 | 0.838 | MEP+MVA |
| 57 | Ornithine exchange | 0.160 | 0.642 | 0.328 | 0.642 | 0.000 | MEP |
| 58 | Phenethylamine exchange | 0.254 | 0.635 | 0.566 | 0.661 | 4.111 | MEP+MVA |
| 59 | Phenylacetaldehyde exchange | 0.254 | 0.635 | 0.575 | 0.661 | 4.111 | MEP+MVA |
| 60 | Agmatine exchange | 0.159 | 0.634 | 0.327 | 0.634 | 0.000 | MEP |
| 61 | D-Gluconate exchange | 0.190 | 0.633 | 0.265 | 0.636 | 0.562 | MEP+MVA |
| 62 | D-Alanyl-D-alanine exchange | 0.190 | 0.632 | 0.322 | 0.654 | 3.427 | MEP+MVA |
| 63 | N-Acetylneuraminate exchange | 0.345 | 0.627 | 0.304 | 0.636 | 1.441 | MEP+MVA |
| 64 | L-Idonate exchange | 0.187 | 0.622 | 0.260 | 0.624 | 0.349 | MEP+MVA |
| 65 | D-Alanine exchange | 0.093 | 0.618 | 0.283 | 0.641 | 3.757 | MEP+MVA |
| 66 | L-Alanine exchange | 0.093 | 0.618 | 0.283 | 0.641 | 3.757 | MEP+MVA |
| 67 | L-alanine-L-glutamate exchange' | 0.246 | 0.614 | 0.308 | 0.614 | 0.092 | MEP+MVA |
| 68 | L-alanine-D-glutamate exchange | 0.246 | 0.614 | 0.308 | 0.614 | 0.092 | MEP+MVA |
| 69 | tetradecenoate (n-C14:1) exchange | 0.430 | 0.614 | 0.519 | 0.660 | 0.000 | MVA |
| 70 | hexadecenoate (n-C16:1) exchange | 0.490 | 0.613 | 0.527 | 0.659 | 0.000 | MVA |
| 71 | Propionate exchange | 0.092 | 0.612 | 0.342 | 0.625 | 2.128 | MEP+MVA |
| 72 | D-lactate exchange | 0.092 | 0.612 | 0.281 | 0.625 | 2.128 | MEP+MVA |
| 73 | octadecenoate (n-C18:1) exchange | 0.551 | 0.612 | 0.533 | 0.658 | 0.000 | MVA |
| 74 | L-Galactonate exchange | 0.183 | 0.612 | 0.256 | 0.614 | 0.447 | MEP+MVA |
| 75 | 2-Dehvdro-3-deoxy-D-gluconate exchange | 0.183 | 0.612 | 0.282 | 0.614 | 0.447 | MEP+MVA |
| 76 | D-Galactonate exchange | 0.183 | 0.612 | 0.256 | 0.614 | 0 447 | MEP+MVA |
| 77 | L-Threenine O-3-phosphate exchange | 0.120 | 0.601 | 0.166 | 0.635 | 5 691 | MEP+MVA |
| 78 | L-Threenine exchange | 0.120 | 0.601 | 0.275 | 0.635 | 5 691 | MEP+MVA |
| 70 | octadecanoate (n C18:0) exchange | 0.537 | 0.507 | 0.516 | 0.642 | 0.001 | MVA |
| 80 | Hevadecanoate (n-C16:0) exchange | 0.337 | 0.596 | 0.510 | 0.641 | 0.000 | MVA |
| 00 | tetra decensate (n.C14.0) exchange | 0.417 | 0.590 | 0.308 | 0.620 | 0.000 | MAXA |
| 01 | Dedeements (r. C12:0) exchange | 0.410 | 0.594 | 0.498 | 0.039 | 0.000 | MVA |
| 02 | Dodecanoate (n-C12:0) exchange | 0.335 | 0.592 | 0.480 | 0.037 | 0.000 | IVI V A |
| 83 | Decanoate (n-C10:0) exchange | 0.295 | 0.590 | 0.469 | 0.634 | 0.000 | MVA |
| 84 | octanoate (n-C8:0) exchange | 0.234 | 0.586 | 0.446 | 0.630 | 0.000 | MVA |
| 85 | L-Glutamate exchange | 0.146 | 0.582 | 0.271 | 0.583 | 0.156 | MEP+MVA |
| 86 | L-Glutamine exchange | 0.146 | 0.582 | 0.271 | 0.583 | 0.156 | MEP+MVA |
| 87 | Hexanoate (n-C6:0) exchange | 0.174 | 0.579 | 0.411 | 0.623 | 0.000 | MVA |
| 88 | Phenylpropanoate exchange | 0.260 | 0.577 | 0.474 | 0.592 | 2.551 | MEP+MVA |
| 89 | 5-Dehydro-D-gluconate exchange | 0.173 | 0.575 | 0.243 | 0.579 | 0.667 | MEP+MVA |
| 90 | L-Proline exchange | 0.144 | 0.575 | 0.340 | 0.575 | 0.047 | MEP+MVA |
| 91 | L-Ascorbate exchange | 0.171 | 0.571 | 0.265 | 0.579 | 1.472 | MEP+MVA |
| 92 | Acetoacetate exchange | 0.113 | 0.566 | 0.305 | 0.609 | 0.000 | MVA |
| 93 | Butyrate (n-C4:0) exchange | 0.113 | 0.566 | 0.354 | 0.609 | 0.000 | MVA |
| 94 | L-Lactate exchange | 0.085 | 0.564 | 0.258 | 0.586 | 3.940 | MEP+MVA |
| 95 | L-Arginine exchange | 0.169 | 0.563 | 0.262 | 0.563 | 0.000 | MEP |
| 96 | D-Glucuronate exchange | 0.168 | 0.561 | 0.237 | 0.565 | 0.720 | MEP+MVA |
| 97 | D-Fructuronate exchange | 0.168 | 0.561 | 0.237 | 0.565 | 0.720 | MEP+MVA |
| 98 | D-Glucuronate 1-phosphate exchange | 0.168 | 0.561 | 0.169 | 0.565 | 0.720 | MEP+MVA |
| 99 | D-Galacturonate exchange | 0.168 | 0.561 | 0.237 | 0.565 | 0.720 | MEP+MVA |
| 100 | 3-(3-hydroxy-phenyl)propionate exchange | 0.246 | 0.547 | 0.406 | 0.560 | 2.446 | MEP+MVA |
| 101 | dAMP exchange | 0.273 | 0.546 | 0.226 | 0.549 | 0.431 | MEP+MVA |
| 102 | Deoxyadenosine exchange | 0.273 | 0.546 | 0.296 | 0.549 | 0.431 | MEP+MVA |
| 103 | Deoxvinosine exchange | 0.271 | 0.542 | 0.293 | 0.545 | 0.455 | MEP+MVA |
| 104 | dIMP exchange | 0.271 | 0.542 | 0.224 | 0.545 | 0.455 | MEP+MVA |
| 105 | Reduced glutathione exchange | 0.269 | 0.537 | 0.239 | 0.545 | 1.484 | MEP+MVA |
| 106 | L-Prolinvigivcine exchange | 0.188 | 0.536 | 0.296 | 0.538 | 0.405 | MEP+MVA |
| 107 | (R)-Glycerate exchange | 0.080 | 0.536 | 0.208 | 0.536 | 0.143 | MEP+MVA |
| 108 | 3-hydroxycinnamic acid exchange | 0.238 | 0.529 | 0.397 | 0.542 | 0.000 | MVA |
| 109 | Acetate exchange | 0.053 | 0.527 | 0.243 | 0.567 | 0.000 | MVA |
| 110 | AMP exchange | 0.263 | 0.527 | 0.208 | 0.527 | 0.084 | MEP+MVA |
| 111 | 2'.3'-Cyclic AMP exchange | 0.263 | 0.527 | 0.219 | 0.527 | 0.084 | MEP+MVA |
| 112 | 3'-AMP exchange | 0.263 | 0.527 | 0.208 | 0.527 | 0.084 | MEP+MVA |
| 113 | Adenosine exchange | 0.263 | 0.527 | 0.268 | 0.527 | 0.084 | MEP+MVA |
| 114 | UDP-N-acetyl-D-glucosamine eychange | 0 445 | 0 524 | 0.200 | 0.530 | 1 278 | MEP+MVA |
| 115 | IMP exchange | 0.262 | 0.523 | 0.200 | 0.524 | 0.106 | MEP+MVA |
| 116 | Inosine exchange | 0.262 | 0.523 | 0.265 | 0.524 | 0.106 | MEP+MVA |
| 117 | Succipate exchange | 0.202 | 0.525 | 0.205 | 0.524 | 1 206 | MEDI MWA |
| 119 | Deoxyguanosine exchange | 0.105 | 0.525 | 0.240 | 0.550 | 0.609 | MEP_MVA |
| 110 | dCMP exchange | 0.200 | 0.519 | 0.204 | 0.522 | 0.000 | MED I MAYA |
| 120 | UDPalyaoso ovahango | 0.200 | 0.019 | 0.205 | 0.022 | 0.008 | MED + MVA |
| 120 | 0.2 diaminante di | 0.388 | 0.017 | 0.187 | 0.820 | 0.480 | IVIEIT + IVI VA |
| 121 | 2,5-diaminopropionate exchange | 0.078 | 0.517 | 0.201 | 0.532 | 0.000 | IVI VA |
| 122 | D-Serine exchange | 0.078 | 0.517 | 0.201 | 0.532 | 0.000 | MVA |
| 123 | O-Phospho-L-serine exchange | 0.078 | 0.517 | 0.115 | 0.532 | 0.000 | MVA |
| 125 | L-Serine exchange | 0.078 | 0.517 | 0.201 | 0.532 | 0.000 | MVA |
| 124 | Pyruvate exchange | 0.078 | 0.517 | 0.243 | 0.532 | 0.000 | MVA |
| 126 | UDPgalactose exchange | 0.386 | 0.515 | 0.186 | 0.517 | 0.530 | MEP+MVA |
| 127 | 2-Oxoglutarate exchange | 0.127 | 0.509 | 0.241 | 0.518 | 1.791 | MEP+MVA |
| 128 | 3'-GMP exchange | 0.250 | 0.500 | 0.188 | 0.500 | 0.000 | MEP |
| 129 | 2',3'-Cyclic GMP exchange | 0.250 | 0.500 | 0.198 | 0.500 | 0.000 | MEP |
| 130 | Guanosine exchange | 0.250 | 0.500 | 0.240 | 0.500 | 0.000 | MEP |
| 131 | GMP exchange | 0.250 | 0.500 | 0.188 | 0.500 | 0.000 | MEP |
| 132 | Xanthosine exchange | 0.248 | 0.496 | 0.238 | 0.498 | 0.274 | MEP+MVA |

B.1. Model-based Medium Optimization

| No. Non. Molar Carbon Mass Carbon Yield Pathway 133 Xunkoine 5'-phosphate exchange 0.248 0.496 0.186 0.198 0.271 MEP+MVA 133 L-Admagne exchange 0.008 0.441 0.020 0.498 0.271 MEP+MVA 135 L-Admagne exchange 0.147 0.489 0.192 0.494 1.008 MEP+MVA 136 D-Gincarate exchange 0.147 0.489 0.192 0.494 1.008 MEP+MVA 137 D-Galactarate exchange 0.146 0.448 0.219 0.494 1.008 MEP+MVA 138 Citrate exchange 0.096 0.480 0.229 0.487 1.537 MEP+MVA 140 Functional exchange 0.071 0.474 0.160 0.490 0.000 MVA 141 Cyscline exchange 0.711 0.474 0.166 0.469 2.128 MEP+MVA 142 D-Qysteine exchange 0.778 0.166 | | Table D. | 1 Continu | led from pr | evious pa | | a | |
|--|---------------|--|-----------|-------------|-----------|--------------|----------|---------|
| Notar Carbon Name Carbon Name Carbon Pathway 134 L'Aaparagine exchange 0.048 0.496 0.186 0.498 1.387 MEP+MVA 134 L'Aaparagine exchange 0.098 0.491 0.202 0.498 1.387 MEP+MVA 135 D'Angaratae exchange 0.147 0.490 0.192 0.494 1.008 MEP+MVA 136 D'Artate exchange 0.146 0.485 0.210 0.484 0.108 0.147 MEP+MVA 139 Cirtate exchange 0.096 0.480 0.229 0.487 1.537 MEP+MVA 140 Cycsteine exchange 0.071 0.474 0.160 0.490 0.000 MVA 144 UD-D-glucuronate exchange 0.071 0.474 0.160 0.490 0.000 MVA 144 D-O-glucuronate exchange 0.278 0.464 0.174 0.464 0.166 0.469 2.128 MEP+MVA 144 D-Maiate exc | \mathbf{Nr} | Carbon Source | Non M | evalonate P | athway | MEP+MVA. | Synergy, | Best |
| 133 Xanthosine 5-phosphate exchange 0.248 0.486 0.486 0.487 0.274 MEP+AVA 134 L-Aspartate exchange 0.098 0.491 0.202 0.498 1.387 MEP+AVA 135 L-Aspartate exchange 0.098 0.491 0.202 0.498 1.387 MEP+AVA 136 L-Aspartate exchange 0.147 449 0.202 0.498 1.387 MEP+AVA 137 Decompart exchange 0.146 0.485 0.210 0.486 0.155 MEP+AWA 138 L-Matate exchange 0.146 0.480 0.229 0.487 1.537 MEP+AWA 140 Forgysteine exchange 0.771 0.474 0.160 0.490 0.000 MVA 141 Cycsteine exchange 0.471 0.474 0.160 0.490 0.000 MVA 142 L-Cysteine exchange 0.471 0.464 0.401 0.451 2.453 MEP+MVA 144 Decoxystidine exchange 0.189< | - 1 0 0 | | Molar | Carbon | Mass | Carbon Yield | [%] | Pathway |
| 134 L-Asparatic exchange 0.098 0.491 0.202 0.498 1.387 MEP+NVA 135 L-Asparatic exchange 0.147 0.490 0.192 0.494 1.008 MEP+NVA 136 D-Glacarate exchange 0.147 0.480 0.192 0.494 1.008 MEP+NVA 137 D-Glacarate exchange 0.146 0.480 0.192 0.494 1.008 MEP+NVA 140 Fumare exchange 0.066 0.480 0.192 0.487 1.537 MEP+NVA 141 Cycsteine exchange 0.171 0.474 0.160 0.490 0.000 MVA 142 L-Cysteine exchange 0.349 0.465 0.165 0.471 1.280 MEP+MVA 144 UD-D-glucuronate exchange 0.492 0.464 0.046 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 0.464 </td <td>133</td> <td>Xanthosine 5'-phosphate exchange</td> <td>0.248</td> <td>0.496</td> <td>0.186</td> <td>0.498</td> <td>0.274</td> <td>MEP+MVA</td> | 133 | Xanthosine 5'-phosphate exchange | 0.248 | 0.496 | 0.186 | 0.498 | 0.274 | MEP+MVA |
| 13b L-Aspartate exchange 0.049 0.491 0.202 0.498 1.387 MEP+AVA 137 D-Galactarate exchange 0.147 0.489 0.192 0.494 1.008 MEP+AVA 138 Citrate exchange 0.147 0.489 0.192 0.494 1.008 MEP+AVA 139 L-Malate exchange 0.146 0.485 0.190 0.486 0.157 MEP+AVA 139 L-Malate exchange 0.096 0.485 0.132 0.487 1.537 MEP+AVA 141 Creating exchange 0.096 0.485 0.487 1.537 MEP+AVA 143 D-Cyclip exchange 0.010 0.478 0.466 0.490 0.000 MVA 144 UDP-b-glucuronate exchange 0.349 0.464 0.166 0.469 2.128 MEP+AWA 145 Fe(III)dicitrate exchange 0.189 0.421 0.227 0.431 2.453 MEP+AWA 144 Deoxyuridine exchange 0.189 0.421 </td <td>134</td> <td>L-Asparagine exchange</td> <td>0.098</td> <td>0.491</td> <td>0.202</td> <td>0.498</td> <td>1.387</td> <td>MEP+MVA</td> | 134 | L-Asparagine exchange | 0.098 | 0.491 | 0.202 | 0.498 | 1.387 | MEP+MVA |
| 136 D-Gincarate exchange 0.147 0.489 0.192 0.494 1.008 MEP+AVA 137 D-Gincarate exchange 0.146 0.489 0.192 0.494 1.008 MEP+AVA 138 C-Malate exchange 0.096 0.480 0.198 0.487 1.537 MEP+AVA 140 Fumarate exchange 0.096 0.480 0.229 0.487 1.537 MEP+AVA 141 Cys-Gly exchange 0.071 0.478 0.183 0.492 0.000 MVA 142 L-Systeine exchange 0.071 0.474 0.160 0.400 0.000 MVA 143 D-Cysteine exchange 0.374 0.464 0.160 0.400 0.000 MEP 144 Dely exchange 0.421 0.422 0.420 0.421 MEP+AVA 144 Decxycytidine exchange 0.189 0.421 0.227 0.431 2.453 MEP+AVA 144 Decxyuridine exchange 0.189 0.421 0.267 0.431 2.453 MEP+AVA 144 Decxyuridine exchange <td>135</td> <td>L-Aspartate exchange</td> <td>0.098</td> <td>0.491</td> <td>0.202</td> <td>0.498</td> <td>1.387</td> <td>MEP+MVA</td> | 135 | L-Aspartate exchange | 0.098 | 0.491 | 0.202 | 0.498 | 1.387 | MEP+MVA |
| 131 D-Galactarate exchange 0.147 0.489 0.192 0.494 1.008 MEP-MVA 133 Chrate exchange 0.996 0.480 0.210 0.486 0.156 MEP-MVA 134 Chrate exchange 0.996 0.480 0.229 0.487 1.537 MEP-MVA 141 Cysteine exchange 0.120 0.478 0.183 0.492 0.000 MVA 142 L-Cysteine exchange 0.071 0.474 0.160 0.490 0.000 MVA 144 L-Dp-te-exchange 0.340 0.474 0.464 0.464 0.000 MEP-MVA 145 Fe(Intrinstructure) 0.478 0.189 0.469 2.128 MEP-MVA 146 Glytine exchange 0.020 0.459 0.166 0.469 2.128 MEP-MVA 147 D-Malate exchange 0.492 0.421 0.227 0.431 2.453 MEP-MVA 148 Decxyuridine exchange 0.189 0.421 0.226 2.351 MEP-MVA 151 dUP exchange 0.179 <td< td=""><td>136</td><td>D-Glucarate exchange</td><td>0.147</td><td>0.489</td><td>0.192</td><td>0.494</td><td>1.008</td><td>MEP+MVA</td></td<> | 136 | D-Glucarate exchange | 0.147 | 0.489 | 0.192 | 0.494 | 1.008 | MEP+MVA |
| 138 Chrate exchange 0.146 0.485 0.210 0.486 0.156 MEP+MVA 140 Fumarate exchange 0.096 0.480 0.229 0.487 1.537 MEP+MVA 140 Fumarate exchange 0.071 0.474 0.183 0.492 0.000 MVA 141 L-Cysteine exchange 0.071 0.474 0.160 0.490 0.000 MVA 144 L-Cysteine exchange 0.071 0.474 0.160 0.490 0.000 MVA 144 DCysteine exchange 0.349 0.465 0.165 0.471 1.280 MEP+MVA 145 Fe[II]/dicitrate exchange 0.349 0.465 0.169 0.431 2.453 MEP+MVA 144 Deoxyuridine exchange 0.189 0.421 0.222 0.331 2.453 MEP+MVA 151 dUMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 152 2.3-Cyclric CMP exchange 0.179 0.397< | 137 | D-Galactarate exchange | 0.147 | 0.489 | 0.192 | 0.494 | 1.008 | MEP+MVA |
| $ \begin{array}{c c c c c c c c c c c c c c c c c c c $ | 138 | Citrate exchange | 0.146 | 0.485 | 0.210 | 0.486 | 0.156 | MEP+MVA |
| 140Fumarate exchange0.0990.4800.2290.4871.337MEP+MVA141Cyseline exchange0.0710.4740.1600.4900.000MVA143D-Cysteine exchange0.0710.4740.1600.4900.000MVA144UDP-D-glucuronate exchange0.3490.4650.1650.4711.280MEP+MVA145Fe(III)dicitrate exchange0.0460.4590.1660.4692.128MEP+MVA146Glycine exchange0.1890.4210.2270.4312.453MEP+MVA149dCMP exchange0.1890.4210.2270.4312.453MEP+MVA150Deoxyuridine exchange0.1890.4210.2270.4312.453MEP+MVA151dUMP exchange0.1880.4170.2462.351MEP+MVA152L-tartrate exchange0.1880.4170.2462.351MEP+MVA1532.3^2.Cyclic CMP exchange0.1790.3970.1600.3970.000MEP1543'-crup exchange0.1790.3970.1600.3970.000MEP155Ui/dine exchange0.1790.3970.1500.3970.000MEP1563'-UMP exchange0.1790.3970.1510.3970.000MEP157Cytline exchange0.1790.3970.1510.3970.000MEP1582.3'.Cyclic UMP exchange0.1790.397 <t< td=""><td>139</td><td>L-Malate exchange</td><td>0.096</td><td>0.480</td><td>0.198</td><td>0.487</td><td>1.537</td><td>MEP+MVA</td></t<> | 139 | L-Malate exchange | 0.096 | 0.480 | 0.198 | 0.487 | 1.537 | MEP+MVA |
| 141 Cys-Gly exchange 0.120 0.478 0.183 0.492 0.000 MVA 142 L-Cysteine exchange 0.071 0.474 0.160 0.490 0.000 MVA 144 UDP-D-glucuronate exchange 0.378 0.464 0.174 0.464 0.000 MEP+MVA 145 Fe(III)dicitrate exchange 0.042 0.459 0.186 0.469 2.128 MEP+MVA 147 D-Malate exchange 0.189 0.421 0.277 0.431 2.453 MEP+MVA 149 Dewycytidine exchange 0.188 0.417 0.246 2.351 MEP+MVA 150 Dewyurdine exchange 0.188 0.417 0.426 2.351 MEP+MVA 151 dUMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 154 3'-crup exchange 0.179 0.397 0.200 0.397 0.000 MEP 154 2'.3'-Cyclic CMP exchange 0.179 0.397 0.200 < | 140 | Fumarate exchange | 0.096 | 0.480 | 0.229 | 0.487 | 1.537 | MEP+MVA |
| 142L-Cysteine exchange 0.071 0.474 0.160 0.490 0.000 MVA143D-Cysteine exchange 0.349 0.465 0.160 0.490 0.000 MVA144UDP-D-glucuronate exchange 0.349 0.465 0.165 0.471 1.280 MEP+MVA145Fe(III)dicitrate exchange 0.020 0.459 0.166 0.469 2.128 MEP+MVA146Glycine exchange 0.092 0.459 0.166 0.469 2.128 MEP+MVA148Deoxycytidine exchange 0.189 0.421 0.227 0.431 2.453 MEP+MVA150Deoxyuridine exchange 0.188 0.417 0.160 0.331 2.453 MEP+MVA151dUP exchange 0.188 0.417 0.160 0.397 0.000 MEP153 2.3^* -Cyclic CM exchange 0.179 0.397 0.160 0.397 0.000 MEP154 3^* -crup exchange 0.179 0.397 0.160 0.397 0.000 MEP155 2.3^* -Cyclic CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP155UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP156 3^* -Cyclic UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP157UP exchange 0.179 0.397 0.151 0.397 0.000 MEP158 2.3^* -C | 141 | Cys-Gly exchange | 0.120 | 0.478 | 0.183 | 0.492 | 0.000 | MVA |
| 143 D-Cysteine exchange 0.071 0.474 0.100 0.490 0.000 MVA 144 UDP-Diglucronate exchange 0.278 0.464 0.174 0.464 0.000 MEP 146 Glycine exchange 0.092 0.459 0.166 0.464 0.074 0.464 0.000 MEP 147 D-Malate exchange 0.092 0.459 0.189 0.461 0.227 0.431 2.453 MEP+MVA 149 dCMP exchange 0.188 0.417 0.669 0.228 $MEP+MVA$ 150 Decxyuridine exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA 151 dUMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 153 $c:mp$ exchange 0.179 0.397 0.100 MEP 154 $:cmp$ exchange 0.179 0.397 0.000 MEP 154 $2::cyclic UMP$ exchan | 142 | L-Cysteine exchange | 0.071 | 0.474 | 0.160 | 0.490 | 0.000 | MVA |
| 144 UDP-D-gincuronate exchange 0.349 0.465 0.165 0.471 1.280 MEP+MVA 145 Fe(III)dicitrate exchange 0.046 0.459 0.166 0.469 2.128 MEP+MVA 146 Glycine exchange 0.092 0.459 0.189 0.461 2.128 MEP+MVA 148 Deoxycytidine exchange 0.189 0.421 0.227 0.431 2.453 MEP+MVA 150 Deoxyuridine exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA 151 dUMP exchange 0.188 0.417 0.160 0.397 0.000 MEP 152 L-tartrate exchange 0.179 0.397 0.160 0.397 0.000 MEP 153 2: 3'-Cyclic LMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 154 3'-cmp exchange 0.179 0.397 0.190 0.397 0.000 MEP 154 3'-cmp exchange 0.179 0.397 0.190 0.397 0.000 MEP 155 <t< td=""><td>143</td><td>D-Cysteine exchange</td><td>0.071</td><td>0.474</td><td>0.160</td><td>0.490</td><td>0.000</td><td>MVA</td></t<> | 143 | D-Cysteine exchange | 0.071 | 0.474 | 0.160 | 0.490 | 0.000 | MVA |
| 14bFe(111)dicitrate exchange 0.278 0.404 0.174 0.404 0.000 MEP146Glycine exchange 0.092 0.459 0.166 0.469 2.128 MEP+MVA147D-Malate exchange 0.092 0.459 0.189 0.469 2.128 MEP+MVA148Dexycytidine exchange 0.189 0.421 0.227 0.431 2.453 MEP+MVA150Dexyuridine exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA151dUMP exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA152L-tartate exchange 0.179 0.397 0.160 0.397 0.000 MEP1543'-cryclic CMP exchange 0.179 0.397 0.160 0.397 0.000 MEP1543'-cryclic UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP155Uridine exchange 0.179 0.397 0.151 0.397 0.000 MEP156UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP156UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP15612'.VMP exchange 0.179 0.397 0.151 0.397 0.000 MEP15612'.UMP exchange 0.179 0.337 0.151 0.397 0.000 MEP15612-UMP exchange 0.179 | 144 | UDP-D-glucuronate exchange | 0.349 | 0.465 | 0.165 | 0.471 | 1.280 | MEP+MVA |
| 146 Glycme exchange 0.046 0.469 0.166 0.469 2.128 MEP+MVA 147 D-Malate exchange 0.189 0.421 0.227 0.431 2.453 MEP+MVA 148 Dexycytidine exchange 0.189 0.421 0.127 0.431 2.453 MEP+MVA 150 Dexyuridine exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA 151 dUMP exchange 0.188 0.417 0.167 0.426 2.351 MEP+MVA 152 L-tartrate exchange 0.179 0.397 0.160 0.397 0.000 MEP 153 2',3'-Cyclic CMP exchange 0.179 0.397 0.199 0.397 0.000 MEP 154 3'-cmp exchange 0.179 0.397 0.151 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 166 C-UP exchange 0.179 0.397 0.151 0.397 0.000 MEP 155 UMP exchange < | 145 | Fe(III)dicitrate exchange | 0.278 | 0.464 | 0.174 | 0.464 | 0.000 | MEP |
| 147 D-Malate exchange 0.092 0.499 0.189 0.469 2.128 MEP+MVA 148 Dexycytidine exchange 0.189 0.421 0.227 0.431 2.453 MEP+MVA 150 Dexyuridine exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA 151 dUMP exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA 152 L-tartrate exchange 0.180 0.402 0.148 0.413 0.000 MEP 153 $2', 3'-Cyclic CMP$ exchange 0.179 0.397 0.160 0.397 0.000 MEP 156 $2', 3'-Cyclic UMP$ exchange 0.179 0.397 0.160 0.397 0.000 MEP 158 $2', 3'-Cyclic UMP$ exchange 0.179 0.397 0.151 0.397 0.000 MEP 158 $2', 3'-Cyclic UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151$ | 146 | Glycine exchange | 0.046 | 0.459 | 0.166 | 0.469 | 2.128 | MEP+MVA |
| 148 Dexycytidine exchange 0.189 0.421 0.127 0.431 2.453 MEP+MVA 150 Dexyuridine exchange 0.188 0.412 0.169 0.431 2.453 MEP+MVA 150 Dexyuridine exchange 0.188 0.417 0.167 0.426 2.351 MEP+MVA 152 L-tartrate exchange 0.188 0.417 0.160 0.397 0.000 MEP 153 2',3'-Cyclic CMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 154 3'-cmp exchange 0.179 0.397 0.160 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.159 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 156 3'-UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP 155 UMP exchange < | 147 | D-Malate exchange | 0.092 | 0.459 | 0.189 | 0.469 | 2.128 | MEP+MVA |
| 149 dCMP exchange 0.189 0.421 0.169 0.431 2.453 MEP+MVA 150 Deoxyuridine exchange 0.188 0.417 0.224 0.426 2.351 MEP+MVA 151 Letartate exchange 0.080 0.402 0.148 0.413 0.000 MVA 153 2',3'-Cyclic CMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 154 3'-cmp exchange 0.179 0.397 0.120 0.397 0.000 MEP 155 Cytidine exchange 0.179 0.397 0.150 0.397 0.000 MEP 158 2',3'-Cyclic UMP exchange 0.179 0.397 0.150 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP 162 L-alanine-D-glutamate-meso-2.6- | 148 | Deoxycytidine exchange | 0.189 | 0.421 | 0.227 | 0.431 | 2.453 | MEP+MVA |
| 150 Decxyurdine exchange 0.188 0.417 0.124 0.426 2.351 MEP+MVA 151 dUMP exchange 0.188 0.417 0.167 0.426 2.351 MEP+MVA 152 L-tartrate exchange 0.080 0.402 0.148 0.413 0.000 MVA 153 2',3'-Cyclic CMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 154 3'-cmp exchange 0.179 0.397 0.200 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.150 0.397 0.000 MEP 156 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP 162 L-alanine-D-glutamate-meso-2,6- 0.334 0.371 0.144 | 149 | dCMP exchange | 0.189 | 0.421 | 0.169 | 0.431 | 2.453 | MEP+MVA |
| 151 dUMP exchange 0.188 0.417 0.167 0.426 2.351 MEP+MVA 152 L-tartrate exchange 0.080 0.402 0.148 0.413 0.000 MEP 153 2',3'-Cyclic CMP exchange 0.179 0.397 0.160 0.397 0.000 MEP 154 3'-cmp exchange 0.179 0.397 0.120 0.397 0.000 MEP 159 Uridine exchange 0.179 0.397 0.159 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP 162 L-alanine-D-glutamate-meso-2,6- 0.334 0.376 1.334 MEP+MVA 164 dTMP exchange 0.036 0.357 0.13 | 150 | Deoxyuridine exchange | 0.188 | 0.417 | 0.224 | 0.426 | 2.351 | MEP+MVA |
| 152L-tartrate exchange 0.080 0.402 0.148 0.413 0.000 MVA153 2^3 , C-yclic CMP exchange 0.179 0.397 0.160 0.397 0.000 MEP154 3^3 -cmp exchange 0.179 0.397 0.120 0.397 0.000 MEP157Cytiline exchange 0.179 0.397 0.200 0.397 0.000 MEP158 2^3 , Cyclic UMP exchange 0.179 0.397 0.159 0.397 0.000 MEP155UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP160CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP161D-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP162L-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP163T-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP163Thymidine exchange 0.183 0.367 0.166 0.376 2.339 MEP+MVA164dTMP exchange 0.183 0.367 0.156 0.376 2.339 MEP+MVA165Glycolate exchange 0.0017 0.345 0.156 0.345 0.000 MEP164dTMP exchange 0.003 0.338 0.179 0.341 0.840 MEP+MVA165Hycolate exchange 0.0078 $0.$ | 151 | dUMP exchange | 0.188 | 0.417 | 0.167 | 0.426 | 2.351 | MEP+MVA |
| 1532',3'-Cyclic CMP exchange0.1790.3970.1600.3970.000MEP1543'-cmp exchange0.1790.3970.2000.3970.000MEP157Cytidine exchange0.1790.3970.1990.3970.000MEP1582',3'-Cyclic UMP exchange0.1790.3970.1510.3970.000MEP155UMP exchange0.1790.3970.1510.3970.000MEP1563'-UMP exchange0.1790.3970.1510.3970.000MEP161D-tartrate exchange0.1790.3970.1510.3970.000MEP162L-alanine-D-glutamate-meso-2,6-0.3340.3710.1980.3761.434MEP+MVA163Thymidine exchange0.1830.3670.1560.3762.339MEP+MVA164dTMP exchange0.0360.3570.1300.3570.000MEP165Glycolate exchange0.0360.3570.1300.3570.000MEP166Formaldehyde exchange0.2030.3380.1790.3410.840MEP+MVA168psicoelysine exchange0.2030.3380.1790.3410.840MEP+MVA168psicoelysine exchange0.2030.3380.1790.3110.300MEP171Adenine-D-glutamate-meso-2,6-0.2390.3180.1670.3120.000MEP167fructoselysine exchan | 152 | L-tartrate exchange | 0.080 | 0.402 | 0.148 | 0.413 | 0.000 | MVA |
| 1543'-cmp exchange0.1790.3970.1510.3970.000MEP157Cytidine exchange0.1790.3970.2000.3970.000MEP158U'rdine exchange0.1790.3970.1590.3970.000MEP158UMP exchange0.1790.3970.1510.3970.000MEP160CMP exchange0.1790.3970.1510.3970.000MEP161D-tartrate exchange0.1790.3970.1510.3970.000MEP162L-alanine-D-glutamate-meso-2,6-0.3740.3910.1440.4010.000MVA163Thymidine exchange0.1830.3670.2060.3762.339MEP+MVA164dTMP exchange0.1830.3670.1560.3762.339MEP+MVA165Glycolate exchange0.0170.3450.1560.3450.000MEP166Formaldehyde exchange0.0170.3450.1560.3450.000MEP167fuctoselysine exchange0.2030.3380.1790.3410.840MEP+MVA168psicoselysine exchange0.2030.3380.1670.3120.000MEP170sn-Glycero-3-phosphocholine exchange0.1250.3130.1320.3130.000MEP171Adenine exchange0.0680.2760.2240.000MEP173sn-Glycero-3-phosphocholine exchange0.065< | 153 | 2',3'-Cyclic CMP exchange | 0.179 | 0.397 | 0.160 | 0.397 | 0.000 | MEP |
| 157 Cytidine exchange 0.179 0.397 0.200 0.397 0.000 MEP 159 Uridine exchange 0.179 0.397 0.199 0.397 0.000 MEP 158 2',3'-Cyclic UMP exchange 0.179 0.397 0.159 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.078 0.391 0.144 0.401 0.000 MVA 162 L-alanine-D-glutamate-meso-2,6- 0.334 0.367 0.206 0.376 2.339 MEP+MVA 163 Thymidine exchange 0.183 0.367 0.130 0.357 0.000 MEP+MVA 164 dTMP exchange 0.183 0.367 0.130 0.357 0.000 MEP+MVA 165 Glycolate exchange 0.017 0.345 0.156 0.345 0.000 MEP 166 Formaldehyde exchange< | 154 | 3'-cmp exchange | 0.179 | 0.397 | 0.151 | 0.397 | 0.000 | MEP |
| 158 2)3'-Cyclic UMP exchange 0.179 0.397 0.199 0.397 0.000 MEP 158 2)3'-Cyclic UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.078 0.391 0.144 0.401 0.000 MVA 162 L-alanine-D-glutamate-meso-2,6- 0.334 0.367 0.206 0.376 2.339 MEP+MVA 163 Glycolate exchange 0.183 0.367 0.130 0.357 0.000 MEP+MVA 164 dTMP exchange 0.017 0.345 0.156 0.376 2.339 MEP+MVA 165 Glycolate exchange 0.017 0.345 0.167 0.341 0.840 MEP+MVA 166 Formatleky | 157 | Cytidine exchange | 0.179 | 0.397 | 0.200 | 0.397 | 0.000 | MEP |
| 158 2',3'-Cyclic UMP exchange 0.179 0.397 0.159 0.397 0.000 MEP 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 156 3'-UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.078 0.391 0.144 0.401 0.000 MVA 162 L-alanine-D-glutamate-meso-2,6- 0.334 0.371 0.198 0.376 1.434 MEP+MVA 163 Thymidine exchange 0.183 0.367 0.206 0.376 2.339 MEP+MVA 164 dTMP exchange 0.017 0.345 0.156 0.345 0.000 MEP 165 Glycolate exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 166 Formaldehyde exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine e | 159 | Uridine exchange | 0.179 | 0.397 | 0.199 | 0.397 | 0.000 | MEP |
| 155 UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 160 CMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 156 3'-UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.078 0.391 0.144 0.401 0.000 MVA 162 L-alanine-D-glutamate-meso-2,6- 0.334 0.371 0.198 0.376 1.434 MEP+MVA 163 Thymidine exchange 0.183 0.367 0.206 0.376 2.339 MEP+MVA 164 dTMP exchange 0.036 0.357 0.130 0.357 0.000 MEP 165 Glycolate exchange 0.017 0.345 0.156 0.345 0.000 MEP 166 Formaldehyde exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.167 0.313 0.000 MEP 170 sn-Glycero-3-phosphocho | 158 | 2',3'-Cyclic UMP exchange | 0.179 | 0.397 | 0.159 | 0.397 | 0.000 | MEP |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | 155 | UMP exchange | 0.179 | 0.397 | 0.151 | 0.397 | 0.000 | MEP |
| 156 3'-UMP exchange 0.179 0.397 0.151 0.397 0.000 MEP 161 D-tartrate exchange 0.078 0.391 0.144 0.401 0.000 MVA 162 L-alanine-D-glutamate-meso-2,6- 0.334 0.371 0.198 0.376 1.434 MEP+MVA diaminoheptanedioate-D-alanine exchange 0.183 0.367 0.206 0.376 2.339 MEP+MVA 164 dTMP exchange 0.183 0.367 0.156 0.376 2.339 MEP+MVA 165 Glycolate exchange 0.036 0.357 0.130 0.357 0.000 MEP+MVA 166 Formaldehyde exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.167 0.319 0.238 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.310 0.840 MEP+MVA | 160 | CMP exchange | 0.179 | 0.397 | 0.151 | 0.397 | 0.000 | MEP |
| | 156 | 3'-UMP exchange | 0.179 | 0.397 | 0.151 | 0.397 | 0.000 | MEP |
| 162 L-alanine-D-glutamate-meso-2,6- 0.337 0.371 0.198 0.376 1.434 MEP+MVA diaminoheptanedioate-D-alanine exchange 0.183 0.367 0.206 0.376 2.339 MEP+MVA 163 Thymidine exchange 0.183 0.367 0.156 0.376 2.339 MEP+MVA 164 dTMP exchange 0.036 0.357 0.130 0.357 0.000 MEP+MVA 165 Glycolate exchange 0.017 0.345 0.156 0.345 0.000 MEP+MVA 166 Formaldehyde exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.312 0.000 MEP 170 sn-Glycero-3-phosphocholine exchange 0.078 0.312 0.157 0.312 0.000 MEP 172 Hypoxanthine exchange 0.078 0.312 0.156 0.312 0.000 MEP < | 161 | D-tartrate exchange | 0.078 | 0.391 | 0.144 | 0.401 | 0.000 | MVA |
| diaminoheptanedioate-D-alanine exchange 163 Thymidine exchange 0.183 0.367 0.206 0.376 2.339 MEP+MVA 164 dTMP exchange 0.183 0.367 0.156 0.376 2.339 MEP+MVA 165 Glycolate exchange 0.036 0.357 0.130 0.357 0.000 MEP+MVA 166 Formaldehyde exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.319 0.238 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.313 0.167 0.310 0.238 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.313 0.167 0.312 0.000 MEP 170 sn-Glycero-3-phosphocholine exchange 0.125 0.278 0.120 0.278 0.000 | 162 | L-alanine-D-glutamate-meso-2,6- | 0.334 | 0.371 | 0.198 | 0.376 | 1.434 | MEP+MVA |
| | | diaminoheptanedioate-D-alanine exchange | | | | | | |
| | 163 | Thymidine exchange | 0.183 | 0.367 | 0.206 | 0.376 | 2.339 | MEP+MVA |
| 165 Glycolate exchange 0.036 0.357 0.130 0.357 0.000 MEP+MVA 166 Formaldehyde exchange 0.017 0.345 0.156 0.345 0.000 MEP 167 fructoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.319 0.238 MEP+MVA 169 sn-Glycero-3-phosphocholine exchange 0.125 0.313 0.132 0.313 0.000 MEP 170 sn-Glycero-3-phosphocholine exchange 0.125 0.313 0.132 0.313 0.000 MEP 171 Adenine exchange 0.078 0.312 0.156 0.312 0.000 MEP 172 Hypoxanthine exchange 0.125 0.278 0.102 0.278 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.276 0.125 0.276 0.000 | 164 | dTMP exchange | 0.183 | 0.367 | 0.156 | 0.376 | 2.339 | MEP+MVA |
| 166 Formaldehyde exchange 0.017 0.345 0.156 0.345 0.000 MEP 167 fructoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.319 0.238 MEP+MVA diaminoheptanedioate exchange 0.125 0.313 0.167 0.312 0.313 0.000 MEP 170 sn-Glycero-3-phosphocholine exchange 0.125 0.313 0.132 0.313 0.000 MEP 171 Adenine exchange 0.078 0.312 0.157 0.312 0.000 MEP 172 Hypoxanthine exchange 0.125 0.278 0.102 0.278 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.276 0.125 0.276 0.000 MEP 174 Gua | 165 | Glycolate exchange | 0.036 | 0.357 | 0.130 | 0.357 | 0.000 | MEP+MVA |
| 167 fructoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 168 psicoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.319 0.238 MEP+MVA diaminoheptanedioate exchange 0.125 0.313 0.167 0.319 0.238 MEP+MVA 170 sn-Glycero-3-phosphocholine exchange 0.078 0.312 0.157 0.312 0.000 MEP 171 Adenine exchange 0.078 0.312 0.156 0.312 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.069 0.276 0.125 0.276 0.000 MEP 174 Guanine exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.068 0.271 0.121 0.200 MEP 175 butanesulfonate exchange 0.068 0.271 0.121 0.000 MEP 175 | 166 | Formaldehyde exchange | 0.017 | 0.345 | 0.156 | 0.345 | 0.000 | MEP |
| 168 psicoselysine exchange 0.203 0.338 0.179 0.341 0.840 MEP+MVA 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.319 0.238 MEP+MVA 170 sn-Glycero-3-phosphocholine exchange 0.125 0.313 0.132 0.313 0.000 MEP 171 Adenine exchange 0.078 0.312 0.157 0.312 0.000 MEP 172 Hypoxanthine exchange 0.078 0.312 0.156 0.312 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.278 0.102 0.278 0.000 MEP 174 Guanine exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.069 0.271 0.199 0.294 0.000 MEP 175 butanesulfonate exchange 0.068 0.271 0.121 0.271 0.000 MEP 176 Xanthine exchange< | 167 | fructoselysine exchange | 0.203 | 0.338 | 0.179 | 0.341 | 0.840 | MEP+MVA |
| 169 L-alanine-D-glutamate-meso-2,6- 0.239 0.318 0.167 0.319 0.238 MEP+MVA diaminoheptanedioate exchange 0.125 0.313 0.167 0.319 0.238 MEP+MVA 170 sn-Glycero-3-phosphocholine exchange 0.125 0.313 0.132 0.313 0.000 MEP 171 Adenine exchange 0.078 0.312 0.157 0.312 0.000 MEP 172 Hypoxanthine exchange 0.078 0.312 0.156 0.312 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.278 0.102 0.278 0.000 MEP 174 Guanine exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.069 0.276 0.125 0.276 0.000 MEP 176 Xanthine exchange 0.068 0.271 0.121 0.271 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP <td>168</td> <td>psicoselysine exchange</td> <td>0.203</td> <td>0.338</td> <td>0.179</td> <td>0.341</td> <td>0.840</td> <td>MEP+MVA</td> | 168 | psicoselysine exchange | 0.203 | 0.338 | 0.179 | 0.341 | 0.840 | MEP+MVA |
| diaminoheptanedioate exchange 170 sn-Glycero-3-phosphocholine exchange 0.125 0.313 0.132 0.313 0.000 MEP 171 Adenine exchange 0.078 0.312 0.157 0.312 0.000 MEP 172 Hypoxanthine exchange 0.078 0.312 0.156 0.312 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.276 0.102 0.278 0.000 MEP 174 Guanine exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.055 0.273 0.109 0.294 0.000 MVA 176 Xanthine exchange 0.179 0.210 0.080 0.210 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.000 MEP 178 | 169 | L-alanine-D-glutamate-meso-2,6- | 0.239 | 0.318 | 0.167 | 0.319 | 0.238 | MEP+MVA |
| 170 sn-Glycero-3-phosphocholine exchange 0.125 0.313 0.132 0.313 0.000 MEP 171 Adenine exchange 0.078 0.312 0.157 0.312 0.000 MEP 172 Hypoxanthine exchange 0.078 0.312 0.156 0.312 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.278 0.102 0.278 0.000 MEP 174 Guanine exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.055 0.273 0.109 0.294 0.000 MEP 176 Xanthine exchange 0.068 0.271 0.121 0.271 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 178 Allantoin ex | | diaminoheptanedioate exchange | | | | | | |
| 171 Adenine exchange 0.078 0.312 0.157 0.312 0.000 MEP 172 Hypoxanthine exchange 0.078 0.312 0.156 0.312 0.000 MEP 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.278 0.102 0.278 0.000 MEP 174 Guanine exchange 0.069 0.276 0.125 0.278 0.000 MEP 175 butanesulfonate exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.068 0.271 0.121 0.274 0.000 MEP 176 Xanthine exchange 0.068 0.271 0.121 0.271 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 178 Allantoin exchange 0.036 0.179 0.061 0.179 0.000 MEP 178 L-Tryptophan exchange 0.080 0.165 0.106 0.149 0.000 MVA 1 | 170 | sn-Glycero-3-phosphocholine exchange | 0.125 | 0.313 | 0.132 | 0.313 | 0.000 | MEP |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | 171 | Adenine exchange | 0.078 | 0.312 | 0.157 | 0.312 | 0.000 | MEP |
| 173 sn-Glycero-3-phospho-1-inositol exchange 0.125 0.278 0.102 0.278 0.000 MEP 174 Guanine exchange 0.069 0.276 0.125 0.278 0.000 MEP 175 butanesulfonate exchange 0.055 0.273 0.109 0.294 0.000 MVA 176 Xanthine exchange 0.068 0.271 0.121 0.271 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 178 Allantoin exchange 0.036 0.179 0.061 0.179 0.000 MEP 179 L-Tryptophan exchange 0.080 0.179 0.061 0.179 0.000 MEP 180 Formate exchange 0.033 0.060 0.018 0.061 0.000 MVA | 172 | Hypoxanthine exchange | 0.078 | 0.312 | 0.156 | 0.312 | 0.000 | MEP |
| 174 Guanine exchange 0.069 0.276 0.125 0.276 0.000 MEP 175 butanesulfonate exchange 0.055 0.273 0.109 0.294 0.000 MVA 176 Xanthine exchange 0.068 0.271 0.121 0.271 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 178 Allantoin exchange 0.036 0.179 0.061 0.179 0.000 MEP+MVA 179 L-Tryptophan exchange 0.080 0.145 0.166 0.149 0.000 MVA 180 Formate exchange 0.003 0.060 0.018 0.061 0.000 MVA | 173 | sn-Glycero-3-phospho-1-inositol exchange | 0.125 | 0.278 | 0.102 | 0.278 | 0.000 | MEP |
| 175 butanesulfonate exchange 0.055 0.273 0.109 0.294 0.000 MVA 176 Xanthine exchange 0.068 0.271 0.121 0.271 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 178 Allantoin exchange 0.036 0.179 0.061 0.179 0.000 MEP 179 L-Tryptophan exchange 0.080 0.145 0.106 0.149 0.000 MVA 180 Formate exchange 0.033 0.060 0.018 0.061 0.000 MVA | 174 | Guanine exchange | 0.069 | 0.276 | 0.125 | 0.276 | 0.000 | MEP |
| 176 Xanthine exchange 0.068 0.271 0.121 0.271 0.000 MEP 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 178 Allantoin exchange 0.036 0.179 0.061 0.179 0.000 MEP 179 L-Tryptophan exchange 0.080 0.145 0.106 0.149 0.000 MVA 180 Formate exchange 0.03 0.060 0.018 0.061 0.000 MVA | 175 | butanesulfonate exchange | 0.055 | 0.273 | 0.109 | 0.294 | 0.000 | MVA |
| 177 UDP-N-acetyl-D-galactosamine exchange 0.179 0.210 0.080 0.210 0.000 MEP 178 Allantoin exchange 0.036 0.179 0.061 0.179 0.000 MEP+MVA 179 L-Tryptophan exchange 0.080 0.145 0.106 0.149 0.000 MVA 180 Formate exchange 0.003 0.060 0.018 0.061 0.000 MVA | 176 | Xanthine exchange | 0.068 | 0.271 | 0.121 | 0.271 | 0.000 | MEP |
| 178 Allantoin exchange 0.036 0.179 0.061 0.179 0.000 MEP+MVA 179 L-Tryptophan exchange 0.080 0.145 0.106 0.149 0.000 MVA 180 Formate exchange 0.003 0.060 0.018 0.061 0.000 MVA | 177 | UDP-N-acetyl-D-galactosamine exchange | 0.179 | 0.210 | 0.080 | 0.210 | 0.000 | MEP |
| 179 L-Tryptophan exchange 0.080 0.145 0.106 0.149 0.000 MVA 180 Formate exchange 0.003 0.060 0.018 0.061 0.000 MVA | 178 | Allantoin exchange | 0.036 | 0.179 | 0.061 | 0.179 | 0.000 | MEP+MVA |
| 180 Formate exchange 0.003 0.060 0.018 0.061 0.000 MVA | 179 | L-Tryptophan exchange | 0.080 | 0.145 | 0.106 | 0.149 | 0.000 | MVA |
| | 180 | Formate exchange | 0.003 | 0.060 | 0.018 | 0.061 | 0.000 | MVA |

Table B.1 Continued from previous page

B.1.3. Ranking of 180 Substrates According to Profit

Table B.2 provides a ranking of 180 different growth supporting substrates using profit as performance criteria. Note that for 21 substrates, the molar price was not available.

Table B.2.: Maximal Profit Calculated for 180 Carbon Sources. The E. coli metabolic reconstruction iJO1366 was used for all calculations. Profits are reported for the non-mevalonate pathway (MEP). For all calculations, NGAM and growth rate were set to 0. Additionally, molecular weight, prices on a molar basis and carbon content for each carbon source are provided.

| Nr | Carbon Source | Molecular Weight, | Nr. Carbon | Price, | Profit MEP, |
|-----|----------------------------------|-------------------|------------|------------|---------------------------|
| 141 | Garbon Source | [g/mol] | Atoms | [US\$/mol] | [US\$ Txd/US\$ Substrate] |
| | | | | | |
| 1 | Formaldehyde exchange | 30.026 | 1 | 7.75E-03 | 285,004 |
| 2 | Maltohexaose exchange | 990.870 | 36 | 7.07E-01 | 223,319 |
| 3 | Ethanol exchange | 46.069 | 2 | 5.10E-02 | 220,493 |
| 4 | Maltose exchange | 342.300 | 12 | 2.61E-01 | 203,365 |
| 5 | Acetaldehyde exchange | 44.053 | 2 | 5.21E-02 | 182,370 |
| 6 | Hexadecanoate (n-C16:0) exchange | 255.421 | 16 | 3.12E-01 | 167,338 |
| 7 | D-Gluconate exchange | 195.149 | 6 | 1.49E-01 | 163,707 |
| 8 | octadecanoate (n-C18:0) exchange | 283.475 | 18 | 3.72E-01 | 158,154 |
| 9 | D-Sorbitol exchange | 182.174 | 6 | 1.81E-01 | 155,600 |
| 10 | D-Glucose exchange | 180.158 | 6 | 1.74E-01 | 151,976 |

| | Tal | ble B.2 Continued from | n previous page | | |
|-----|--|------------------------|-----------------|----------------------------------|----------------------------|
| Nr | Carbon Source | Molecular Weight, | Nr. Carbon | Price, | Profit MEP, |
| | Carbon Bource | [g/mol] | Atoms | [US\$/mol] | [US\$ Txd/ US\$ Substrate] |
| 11 | Propanal exchange | 58.080 | 3 | 1.03E-01 | 133,928 |
| 12 | Sucrose exchange | 342.300 | 12 | 4.10E-01 | 129,244 |
| 13 | tetradecanoate (n-C14:0) exchange | 227.367 | 14 | 4.06E-01 | 112,776 |
| 14 | Citrate exchange | 189.102 | 6 | 1.70E-01 | 109,495 |
| 15 | Decanoate (n-C10:0) exchange | 171.200 | 10 | 3.47E-01 | 94,429 |
| 17 | Propionate exchange | 73 072 | 3 | 1.32E-01 1.46E-01 | 80.436 |
| 18 | Ethanolamine exchange | 62 002 | 2 | 1.40E-01 | 76 469 |
| 19 | Butwrate (n-C4:0) exchange | 87.098 | 4 | 1.88E-01 | 70 362 |
| 20 | octanoate (n-C8:0) exchange | 143 206 | 8 | 3 93E-01 | 66.879 |
| 21 | Fumarate exchange | 114.057 | 4 | 1.87E-01 | 65,709 |
| 22 | Lactose exchange | 342.300 | 12 | 8.63E-01 | 61,135 |
| 23 | Glycerol exchange' | 92.095 | 3 | 2.60E-01 | 59,371 |
| 24 | L-Threonine exchange | 119.120 | 4 | 3.25E-01 | 47,386 |
| 25 | Hexanoate (n-C6:0) exchange | 115.152 | 6 | 4.39E-01 | 44,977 |
| 26 | Succinate exchange | 116.073 | 4 | 3.00E-01 | 44,687 |
| 27 | D-Mannitol exchange | 182.174 | 6 | 6.73E-01 | 41,920 |
| 28 | L-Glutamate exchange | 146.123 | 5 | 4.71E-01 | 39,532 |
| 29 | D-Xylose exchange | 150.131 | 5 | 5.57E-01 | 39,200 |
| 30 | D-Fructose exchange | 180.158 | 6 | 7.12E-01 | 37,175 |
| 31 | Glycine exchange | 75.067 | 2 | 1.88E-01 | 31,256 |
| 32 | Phenylacetaldehyde exchange | 120.151 | 8 | $1.08E{+}00$ | 29,764 |
| 33 | L-Alanine exchange | 89.094 | 3 | 4.26E-01 | 27,872 |
| 34 | L-Malate exchange | 132.073 | 4 | 4.53E-01 | 27,148 |
| 35 | L-Aspartate exchange | 132.096 | 4 | 6.22E-01 | 20,215 |
| 36 | Uridine exchange | 244.204 | 9 | 1.34E+00 | 17,075 |
| 37 | L-Ascorbate exchange | 176.126 | 6 | 1.35E+00 | 16,278 |
| 20 | A Amin abutamanta analar an | 140.072 | 4 | 0.51E-01 | 15,809 |
| 39 | 4-Ammobutanoate exchange | 103.121 | 4 | $1.11E \pm 00$ $1.65E \pm 00$ | 12,437 |
| 40 | L-Arginnie exchange | 146 146 | 5 | $1.03E \pm 00$ $1.52E \pm 00$ | 12 225 |
| 41 | Clucolate exchange | 75 044 | 2 | $3.97E_{-0.01}$ | 11 523 |
| 43 | Formate exchange | 45 018 | 1 | 3.53E-01 | 10.871 |
| 44 | Pyruvate exchange | 87 055 | 3 | 9.34E-01 | 10,640 |
| 45 | Inosine exchange | 268.229 | 10 | $3.68E \pm 00$ | 9.107 |
| 46 | D-Mannose exchange | 180.158 | 6 | 3.49E + 00 | 7,591 |
| 47 | Phenethylamine exchange | 122.190 | 8 | 4.95E + 00 | 6,564 |
| 48 | Dodecanoate (n-C12:0) exchange | 199.313 | 12 | 6.18E + 00 | 6,355 |
| 49 | Hypoxanthine exchange | 136.113 | 5 | 1.75E + 00 | 5,707 |
| 50 | Allantoin exchange | 158.117 | 4 | 8.97E-01 | 5,099 |
| 51 | L-Cysteine exchange | 121.160 | 3 | $1.79E{+}00$ | 5,084 |
| 52 | L-Serine exchange | 105.094 | 3 | $2.13E{+}00$ | 4,669 |
| 53 | IMP exchange | 346.193 | 10 | $8.38E{+}00$ | 3,999 |
| 54 | Adenine exchange | 135.128 | 5 | 3.26E + 00 | 3,061 |
| 55 | L-Proline exchange | 115.132 | 5 | $4.61E{+}00$ | 2,947 |
| 56 | Guanine exchange | 151.128 | 5 | 3.12E+00 | 2,837 |
| 57 | D-Ribose exchange | 150.131 | 5 | 8.11E+00 | 2,594 |
| 58 | Cytidine exchange | 243.219 | 9 | 9.81E+00 | 2,332 |
| 59 | D-Galactose exchange | 180.158 | 6 | 1.28E+01 7.61E+00 | 2,053 |
| 61 | (5)-Fropane-1,2-dior exchange | 144.094 | ی ۲ | 1.01E+00 | 1,900 |
| 60 | 2-Oxogiutarate exchange | 144.084 | 5 | $1.02E \pm 01$ | 1,595 |
| 63 | D Alanine exchange | 80.004 | 3 | $7.66E \pm 00$ | 1,500 |
| 64 | L Asparagine exchange | 132 110 | 4 | $8.46E \pm 00$ | 1,045 |
| 65 | D-Galactonate exchange | 195 149 | 6 | $1.68E \pm 01$ | 1,400 |
| 66 | D-lactate exchange | 89.071 | 3 | 9.00E+00 | 1,307 |
| 67 | D-Glucosamine exchange | 180.181 | 6 | 2.05E+01 | 1.289 |
| 68 | Guanosine exchange | 283.244 | 10 | 2.52E + 01 | 1,270 |
| 69 | Putrescine exchange | 90.169 | 4 | 1.65E + 01 | 1,234 |
| 70 | Adenosine exchange | 267.245 | 10 | 2.78E + 01 | 1,214 |
| 71 | Galactitol exchange | 182.174 | 6 | $2.35E{+}01$ | 1,197 |
| 72 | N-Acetyl-D-glucosamine exchange | 221.210 | 8 | 3.05E + 01 | 1,098 |
| 73 | Dihydroxyacetone exchange | 90.079 | 3 | $1.38E{+}01$ | 962 |
| 74 | L-Rhamnose exchange | 164.158 | 6 | 3.09E + 01 | 845 |
| 75 | L-Tryptophan exchange | 204.229 | 11 | 1.31E + 01 | 781 |
| 76 | D-Galactarate exchange | 208.125 | 6 | 2.60E+01 | 722 |
| 77 | D-tartrate exchange | 148.072 | 4 | 1.85E+01 | 541 |
| 78 | 3-hydroxycinnamic acid exchange | 163.153 | 9 | 5.86E + 01 | 521 |
| 19 | Clyaaral 2 phosphata auchara | 342.300 | 12 | 1.22E+02 | 437 |
| 80 | D Soving avalante exchange | 105.004 | 3 | $3.83E \pm 01$ | 403 |
| 82 | Xanthine exchange | 159 119 | 5 | $2.30E \pm 01$ 2.28E ± 01 | 380 |
| 83 | AMP exchange | 345 209 | 10 | 9.60E+01 | 352 |
| 84 | Thymidine exchange | 242.232 | 10 | 7.02E+01 | 334 |
| 85 | CMP exchange | 321.183 | 9 | 8.22E + 01 | 278 |
| 86 | D-Malate exchange | 132.073 | 4 | 4.28E + 01 | 275 |
| 87 | Reduced glutathione exchange | 306.320 | 10 | 1.33E + 02 | 258 |
| 88 | chitobiose exchange | 424.405 | 16 | 2.81E + 02 | 229 |
| 89 | D-Cysteine exchange | 121.160 | 3 | $5.15E{+}01$ | 177 |
| 90 | L-Arabinose exchange | 150.131 | 5 | 1.27E + 02 | 172 |
| 91 | D-Glucose 6-phosphate exchange | 258.122 | 6 | 1.86E + 02 | 147 |
| 92 | D-Mannose 6-phosphate exchange | 258.122 | 6 | 1.86E + 02 | 147 |
| 93 | D-Glucose 1-phosphate exchange | 258.122 | 6 | 1.81E+02 | 146 |
| 94 | alpha-D-Galactose 1-phosphate exchange | 258.122 | 6 | 1.81E + 02 | 145 |
| 95 | Deoxyuridine exchange | 228.205 | 9 | 1.71E + 02 | 140 |
| 96 | (R)-Glycerate exchange | 105.070 | 3 | 8.22E+01 | 125 |
| 97 | butanesulfonate exchange | 137.180 | 4 | 6.09E + 01 | 115 |
| 98 | N A actulnouraminate archange | 208.122 | 0 11 | 2.32E+02 | 109 |
| 39 | N-Acetymeurannate exchange | 3U8.203 | 11 | 4.108+02 | 108 |
| 100 | arpna-D-moose o-phosphate exchange | 220.090 | ы С | 1.900+02 | 100 |

B.1. Model-based Medium Optimization

| | Tabl | e B.2 Continued from | n previous page | Dutur | D. Ct MED |
|---------------|--|----------------------|-----------------|----------------------------------|--|
| \mathbf{Nr} | Carbon Source | Molecular Weight, | Nr. Carbon | Price, | Profit MEP, [US\$ Twd / US\$ Substants] |
| 101 | Melibiose exchange | 342 300 | 12 | $551E\pm02$ | |
| 101 | dIMP exchange | 330 194 | 12 | $3.68E \pm 02$ | 94 |
| 102 | L-Fucose exchange | 164 158 | 6 | 2.72E+02 | 94 |
| 104 | D-Galacturonate exchange | 193 133 | 6 | 2.33E+02 | 92 |
| 104 | D-Glucuronate exchange | 193.133 | 6 | 2.33E+02 | 92 |
| 106 | Deoxycytidine exchange | 227.220 | 9 | $2.74E \pm 02$ | 88 |
| 107 | L-Xvlulose exchange | 150.131 | 5 | 2.49E + 02 | 88 |
| 108 | Deoxyguanosine exchange | 267.245 | 10 | 4.25E + 02 | 78 |
| 109 | Deoxyadenosine exchange | 251.245 | 10 | 5.53E + 02 | 63 |
| 110 | D-Glucarate exchange | 208.125 | 6 | 3.04E + 02 | 62 |
| 111 | UDP-N-acetyl-D-glucosamine exchange | 605.343 | 17 | 9.56E + 02 | 60 |
| 112 | dAMP exchange | 329.209 | 10 | 6.34E + 02 | 55 |
| 113 | 3'-cmp exchange | 321.183 | 9 | 4.23E + 02 | 54 |
| 114 | D-Glucosamine 6-phosphate exchange | 258.145 | 6 | 5.28E + 02 | 52 |
| 115 | Maltotriose exchange | 504.442 | 18 | 1.61E + 03 | 49 |
| 116 | sn-Glycero-3-phosphocholine exchange | 257.224 | 8 | 3.40E + 02 | 47 |
| 117 | Deoxyinosine exchange | 252.230 | 10 | 7.45E + 02 | 47 |
| 118 | dCMP exchange | 305.184 | 9 | 5.88E + 02 | 41 |
| 119 | Glycerol 3-phosphate exchange | 170.059 | 3 | 4.51E + 02 | 35 |
| 120 | N-Acetyl-D-mannosamine exchange | 221.210 | 8 | 9.64E + 02 | 35 |
| 121 | L-Lyxose exchange | 150.131 | 5 | 6.50E + 02 | 34 |
| 122 | 2',3'-Cyclic CMP exchange | 304.176 | 9 | 7.75E + 02 | 29 |
| 123 | dTMP exchange | 320.196 | 10 | 8.07E + 02 | 29 |
| 124 | D-Glyceraldehyde exchange | 90.079 | 3 | 4.74E + 02 | 28 |
| 125 | 2',3'-Cyclic AMP exchange | 328.201 | 10 | 1.37E + 03 | 25 |
| 126 | UDP-N-acetyl-D-galactosamine exchange | 605.343 | 17 | 9.56E + 02 | 24 |
| 127 | UMP exchange | 322.168 | 9 | 1.02E + 03 | 22 |
| 128 | 3'-AMP exchange | 345.209 | 10 | 1.78E + 03 | 19 |
| 129 | Agmatine exchange | 132.209 | 5 | 1.29E + 03 | 16 |
| 130 | GMP exchange | 361.208 | 10 | 2.03E+03 | 16 |
| 131 | D-Allose exchange | 180.158 | 6 | 1.74E + 03 | 15 |
| 132 | UDPglucose exchange | 564.290 | 15 | $4.19E{+}03$ | 12 |
| 133 | L-Threonine O-3-phosphate exchange | 197.084 | 4 | 1.36E + 03 | 11 |
| 134 | L-alanine-D-glutamate exchange | 217.202 | 8 | 3.80E + 03 | 8 |
| 135 | UDPgalactose exchange | 564.290 | 15 | 7.86E + 03 | 6 |
| 136 | dGMP exchange | 345.209 | 10 | 5.29E + 03 | 6 |
| 137 | Acetoacetate exchange | 101.082 | 4 | 2.98E + 03 | 5 |
| 138 | N-Acetylmuramate exchange | 292.266 | 11 | $1.08E{+}04$ | 4 |
| 139 | Maltopentaose exchange | 828.727 | 30 | $9.61E{+}04$ | 1 |
| 140 | Phenylpropanoate exchange | 149.169 | 9 | $4.30\mathrm{E}{+}04$ | 1 |
| 141 | O-Phospho-L-serine exchange | 183.058 | 3 | $1.79E{+}04$ | 1 |
| 142 | D-Alanyl-D-alanine exchange | 160.173 | 6 | 4.76E+04 | 1 |
| 143 | beta D-Galactose exchange | 180.158 | 6 | 5.55E+04 | 0 |
| 144 | Acetate exchange | 59.045 | 2 | 1.75E+04 | 0 |
| 145 | 5-Denydro-D-gluconate exchange | 193.133 | 6 | 5.95E+04 | 0 |
| 140 | Maitotetraose exchange | 000.385 | 24 | 2.91E+0.00 | 0 |
| 147 | Vanthosine El abardate suchange | 264.229 | 10 | $9.40E \pm 04$ | 0 |
| 140 | dIMP eveloping | 206 160 | 10 | 1.04E+03 | 0 |
| 149 | D Fructuronate exchange | 103 133 | 9 | $8.82E \pm 04$ $8.20E \pm 04$ | 0 |
| 151 | UDP D glucuronate exchange | 577 266 | 15 | $1.78E \pm 05$ | 0 |
| 152 | Glycerophosphoserine exchange | 258 145 | 6 | 1.09E+05 | 0 |
| 153 | 2' 3'-Cyclic UMP exchange | 305 161 | 9 | 9.40E+04 | 0 |
| 154 | N-Acetyl-D-glucosamine 1-phosphate ex- | 299 174 | 8 | 1.41E+05 | Ő |
| | change | | - | | ÷ |
| 155 | 2',3'-Cvclic GMP exchange | 344.201 | 10 | 1.46E + 05 | 0 |
| 156 | Cys-Gly exchange | 178.212 | 5 | 6.99E + 04 | 0 |
| 157 | fructoselysine exchange | 309.340 | 12 | 1.31E + 05 | 0 |
| 158 | 3'-UMP exchange | 322.168 | 9 | 1.38E + 05 | 0 |
| 159 | 3'-GMP exchange | 361.208 | 10 | 1.94E + 05 | 0 |
| 160 | L-Galactonate exchange | 195.149 | 6 | NA | NA |
| 161 | D-Glucuronate 1-phosphate exchange | 271.097 | 6 | NA | NA |
| 162 | 1,4-alpha-D-glucan exchange | 990.870 | 36 | NA | NA |
| 163 | 2,3-diaminopropionate exchange | 105.117 | 3 | NA | NA |
| 164 | 2-Dehydro-3-deoxy-D-gluconate exchange | 177.134 | 6 | NA | NA |
| 165 | 3-(3-hydroxy-phenyl)propionate exchange | 165.169 | 9 | NA | NA |
| 166 | L-alanine-D-glutamate-meso-2,6- | 389.386 | 15 | NA | NA |
| | diaminoheptanedioate exchange | | | | |
| 167 | L-alanine-D-glutamate-meso-2,6- | 460.465 | 18 | NA | NA |
| | diaminoheptanedioate-D-alanine exchange | | | | |
| 168 | L-alanine-L-glutamate exchange | 217.202 | 8 | NA | NA |
| 169 | N-Acetyl-D-glucosamine(anhydrous)N- | 477.446 | 19 | NA | NA |
| | Acetylmuramic acid exchange | | | | |
| 170 | Fe(III)dicitrate exchange | 434.050 | 12 | NA | NA |
| 171 | sn-Glycero-3-phosphoethanolamine ex- | 215.143 | 5 | NA | NA |
| | change | | | | |
| 172 | Glycerophosphoglycerol exchange | 245.146 | 6 | NA | NA |
| 173 | sn-Glycero-3-phospho-1-inositol exchange | 333.209 | 9 | NA | NA |
| 174 | hexadecenoate (n-C16:1) exchange | 253.405 | 16 | NA | NA |
| 175 | L-Idonate exchange | 195.149 | 6 | NA | NA |
| 176 | 2(aipna-D-Mannosyl)-D-glycerate exchange | 267.213 | 9 | IN A | IN A |
| 177 | United and the second s | 281.459 | 18 | IN A | IN A N A |
| 170 | L-r ronnyigiyenie exchange | 200.240 | (| IN A N A | IN A N A |
| 190 | totradozonosto (n.C14:1) | 309.340 305.251 | 12 | IN A N A | IN A N A |
| 100 | terrauecenoare (II-014:1) exchange | 440.001 | 14 | INA | INA |

| Time | 0.0 | DW | Glucose | Taxadiene |
|------|-------|-------|----------|------------------------|
| [h] | OD | [g/l] | [mmol/l] | [mmol/l] |
| 0 | 0.09 | _ | 108.33 | _ |
| 1 | 0.11 | - | - | — |
| 2 | 0.20 | - | — | — |
| 3 | 0.39 | 0.30 | _ | - |
| 4 | 0.68 | 0.50 | 110.56 | — |
| 5 | 1.13 | - | — | — |
| 6 | 1.72 | 1.20 | 103.89 | — |
| 6.5 | 2.00 | - | _ | - |
| 7 | 2.34 | - | — | — |
| 7.5 | 2.90 | - | — | — |
| 8 | 3.48 | 1.67 | 83.33 | — |
| 8.5 | 3.72 | - | — | 0.000 |
| 10.5 | 4.00 | 2.30 | 72.46 | - |
| 12.5 | 4.30 | 2.23 | 69.66 | - |
| 14.5 | 5.15 | 2.70 | 63.48 | 1.515×10^{-3} |
| 24.5 | 8.00 | 4.20 | 66.43 | 8.137×10^{-4} |
| 27.5 | 8.70 | 4.03 | 47.84 | - |
| 30.5 | 9.20 | 4.53 | 62.77 | - |
| 32.5 | 10.10 | 4.13 | 57.75 | 4.452×10^{-3} |
| 48.5 | 12.20 | 4.77 | 18.09 | $6.475 	imes 10^{-3}$ |
| 52.5 | 11.90 | 4.47 | 20.00 | - |
| 56.5 | 11.90 | 4.47 | 12.98 | 8.332×10^{-3} |
| 72.5 | 11.50 | 5.03 | 10.06 | - |
| 76.5 | 14.60 | 5.40 | 0.11 | $7.831 	imes 10^{-3}$ |

Table B.3.: Concentration Time Courses for Batch ID 1. Glucose was added to the bioreactor as follows: 2 g diluted in 4 ml after 14.5 hours; 1 g diluted in 2 ml after 56.5 hours.

B.2. Model-based Fed-batch Optimization

B.2.1. Concentration Time Courses for Process Development

Concentration time courses for OD, glucose, and taxadiene for six different semi-batch fermentations are provided in Tables B.3 to B.8.

B.2.2. Temperature Dependencies of Phases Duration and Exchange Rates

Tables B.9 and B.10 list all formulas used to describe the effect of $T_{production}$ on phase duration and exchange rates, respectively.

B.2.3. Modeling Concentration Time Courses for All Fermentations

Simulated concentration time courses for all six fermentation processes are shown in Figure 8.4 for batch 1 and in Figures B.1 to B.5 for all other batches. Determination coefficients are calculated using following formula

$$R^2 = 1 - \frac{\sum (E_i - S_i)^2}{\sum (E_i - \bar{E})^2}, \quad where \quad \bar{E} = \frac{1}{n} \sum_{i=1}^n E_i.$$

E represents the experimental data set, containing n measurements, \overline{E} is the mean of the measured data and S is the simulated data set. S_i is the corresponding predicted value of

| Time | 00 | DW | Glucose | Taxadiene |
|-------|-------|-------|----------|------------------------|
| [h] | OD | [g/l] | [mmol/l] | [mmol/l] |
| 0 | 0.07 | - | 115.61 | - |
| 2 | 0.26 | - | _ | - |
| 4 | 0.78 | - | — | — |
| 5 | 1.47 | - | — | — |
| 5.5 | 2.04 | 1.27 | 103.27 | — |
| 6.5 | 3.60 | - | — | — |
| 7 | 1.00 | - | _ | 6.491×10^{-4} |
| 7.5 | 4.06 | 2.30 | 89.80 | _ |
| 8.5 | 4.13 | - | — | — |
| 24.75 | 8.33 | 4.20 | 76.98 | 4.309×10^{-3} |
| 27.75 | 8.13 | 4.30 | 77.82 | _ |
| 30.75 | 8.68 | 4.30 | 66.79 | 5.416×10^{-3} |
| 33.33 | 9.23 | - | _ | _ |
| 47 | 10.95 | 4.37 | 63.42 | 6.359×10^{-3} |
| 49.75 | 11.23 | 4.40 | 65.20 | _ |
| 52.25 | 10.65 | 4.40 | 60.07 | _ |
| 54.75 | 10.90 | 4.47 | 65.10 | 6.477×10^{-3} |
| 71.25 | 11.45 | 4.37 | 37.04 | - |
| 73.75 | 11.10 | 4.33 | 34.29 | 7.565×10^{-3} |

Table B.4.: Concentration Time Courses for Batch ID 2. Glucose was added to the bioreactor as follows: 2 g diluted in 4 ml after 8.5 hours; 1.5 g diluted in 3 ml after 33.3 hours.

Table B.5.: Concentration Time Courses for Batch ID 3. Glucose was added to the bioreactor as follows: 2.5 g diluted in 5 ml after 9.25, 27.17 and 47.25 hours; 5 g diluted in 10 ml after 55.5 hours.

| Time | | DW | Glucose | Taxadiene |
|-------|-------|-------|----------|------------------------|
| [h] | OD | [g/l] | [mmol/l] | [mmol/l] |
| 0.00 | | — | 118.00 | - |
| 0.75 | 0.14 | — | 117.83 | — |
| 1.75 | 0.29 | - | _ | _ |
| 3.75 | 0.94 | 0.47 | 109.13 | — |
| 4.75 | 1.50 | — | — | — |
| 5.75 | 2.40 | 0.73 | 98.93 | — |
| 6.25 | 2.72 | - | _ | - |
| 6.75 | 3.13 | - | _ | - |
| 7.25 | 3.26 | 1.40 | 87.82 | 0.000 |
| 9.25 | 4.32 | — | — | — |
| 23.00 | 10.81 | 4.13 | 48.38 | 1.792×10^{-2} |
| 27.17 | 11.84 | 4.47 | 38.65 | - |
| 31.00 | 12.64 | 4.43 | 56.56 | 2.197×10^{-2} |
| 47.25 | 14.00 | 4.67 | 25.82 | - |
| 51.50 | 14.95 | 4.83 | 38.67 | - |
| 55.50 | 14.74 | 4.57 | 37.77 | 2.770×10^{-2} |
| 75.00 | 17.18 | 5.27 | 59.59 | 1.604×10^{-2} |

| Time | OD | DW | Glucose | Taxadiene |
|-------|-------|-------|----------|------------------------|
| [h] | 02 | [g/l] | [mmol/l] | [mmol/l] |
| 0.00 | | 0.06 | 111.01 | - |
| 1.00 | 0.18 | 0.09 | 101.92 | - |
| 2.00 | 0.30 | - | | - |
| 4.00 | 0.84 | 0.30 | 98.38 | - |
| 5.00 | 1.26 | - | | - |
| 6.00 | 1.85 | 0.83 | 92.93 | - |
| 6.75 | 2.62 | - | _ | - |
| 7.25 | 3.21 | 1.17 | 89.80 | 0.000 |
| 9.50 | 6.22 | - | _ | - |
| 10.50 | 7.89 | 2.43 | 42.04 | 1.922×10^{-3} |
| 23.00 | 12.81 | - | _ | - |
| 27.25 | 13.13 | 3.47 | 24.93 | - |
| 31.25 | 12.28 | 2.67 | 31.31 | 1.830×10^{-3} |
| 47.50 | 12.60 | 2.87 | 0.00 | - |
| 51.75 | 14.20 | 3.80 | 0.00 | - |
| 55.75 | 13.00 | 3.87 | 20.86 | 7.340×10^{-4} |
| 75.25 | 12.97 | 4.10 | 0.00 | - |

Table B.6.: Concentration Time Courses for Batch ID 4. Glucose was added to the bioreactor as follows: 5 g diluted in 10 ml after 23 hours; 2.5 g diluted in 5 ml after 27.3, 31.3 and 51.8 hours; 5 g diluted in 10 ml after 55.8 hours; 7.5 g diluted in 15 ml after 75.3 hours.

Table B.7.: Concentration Time Courses for Batch ID 5. Glucose was added to the bioreactor as follows: 2 g diluted in 4 ml after 9.8 hours; 5 g diluted in 10 ml after 30.3 hours and 1 g diluted in 2 ml after 54.3 hours.

| \mathbf{Time} | OD | \mathbf{DW} | Glucose | Taxadiene | |
|-----------------|-------|---------------|----------|------------------------|--|
| [h] | | [g/l] | [mmol/l] | [mmol/l] | |
| 0.00 | 0.10 | | 111.11 | - | |
| 0.50 | 0.15 | - | 112.23 | - | |
| 1.50 | 0.24 | _ | — | — | |
| 2.50 | 0.44 | _ | — | — | |
| 3.50 | 0.80 | 0.49 | 116.46 | — | |
| 4.50 | 1.54 | - | - | - | |
| 5.50 | 3.00 | 1.51 | 105.80 | — | |
| 6.25 | 3.80 | _ | 92.76 | — | |
| 7.25 | 4.25 | _ | — | — | |
| 8.25 | 5.44 | 2.87 | — | — | |
| 9.25 | 5.78 | - | _ | _ | |
| 9.75 | 6.40 | 3.04 | 65.48 | 4.401×10^{-3} | |
| 22.75 | 9.70 | 4.27 | 57.48 | $8.618	imes10^{-3}$ | |
| 24.25 | 10.30 | - | — | — | |
| 25.50 | _ | _ | — | — | |
| 27.00 | 11.10 | 4.56 | 64.93 | 1.116×10^{-2} | |
| 30.25 | 10.80 | 4.53 | 55.46 | 1.377×10^{-2} | |
| 47.00 | 13.20 | 5.07 | 74.61 | _ | |
| 50.75 | _ | - | — | — | |
| 54.25 | 14.05 | 5.18 | 69.62 | 1.729×10^{-2} | |
| 70.50 | 15.40 | 5.44 | - | - | |
| 74.75 | 15.55 | 5.44 | | 1.827×10^{-2} | |

| Time [h] | OD | DW [g/1] | Glucose | Taxadiene [mmol/l] |
|-------------|-------|-------------|---------|------------------------|
| 0.00 | 0.10 | [8/ 1] | 111 11 | |
| 0.50 | 0.16 | 0.11 | 126.05 | _ |
| 1.50 | 0.24 | _ | _ | _ |
| 2.50 | 0.53 | _ | _ | — |
| 3.50 | 0.80 | 0.49 | 114.45 | — |
| 4.50 | 1.54 | _ | _ | _ |
| 5.50 | 2.60 | 1.22 | 105.46 | - |
| 6.25 | 3.40 | - | 84.93 | - |
| 7.25 | | - | _ | - |
| 8.25 | 4.23 | 3.07 | — | — |
| 9.25 | 5.76 | - | — | — |
| 9.75 | 5.97 | 3.24 | 74.97 | 2.075×10^{-3} |
| 22.75 | 6.40 | 4.49 | 39.55 | 1.303×10^{-2} |
| 24.25 | 11.60 | - | _ | — |
| 25.50 | 12.50 | - | - | - |
| 27.00 | 13.00 | 4.76 | 26.63 | 1.614×10^{-2} |
| 30.25 | 14.10 | 5.16 | 12.39 | 2.802×10^{-2} |
| 47.00 | 17.50 | 5.62 | 31.19 | - |
| 50.75 | 18.85 | - | - | - |
| 54.25 | 19.35 | 5.93 | 8.11 | 3.578×10^{-2} |
| 70.50 | 22.20 | 6.24 | 34.54 | - |
| 74.75 | 23.50 | 6.51 | — | 3.598×10^{-2} |

Table B.8.: Concentration Time Courses for Batch ID 6. Glucose was added to the bioreactor as follows: 2 g diluted in 4 ml after 9.75 hours; and 5 g diluted in 10 ml after 30.25 and 54.25 hours.

Table B.9.: Formulas Used to Describe the Effect of Production Temperature on
Phase Duration. x represents $T_{production}$ in °C.

| Phase | Symbol | Equation | R2 |
|---|-------------------|------------------|------|
| Response time | $t_{response}$ | 0.0257x - 0.1612 | 0.87 |
| Duration of second biomass production phase | $t_{biomass2}$ | 18.3 | — |
| Duration of first product formation phase | $t_{production1}$ | -0.9678x + 47.59 | 0.98 |

| on Exchange Rates. | | | | |
|----------------------|----------------|---|-------|--|
| Exchange Rate | Symbol | Equation | R^2 | |
| Crowth | μ_2 | $-7.5724 \times 10^{-5} x^2 + 3.7440 \times 10^{-3} x - 4.2090 \times 10^{-3}$ | 0.99 | |
| GIOWUI | μ_3 | $-1.5319 \times 10^{-5} x^2 + 7.9919 \times 10^{-4} x - 6.5429 \times 10^{-3}$ | 0.99 | |
| Glucose Uptake | $r_{glucose2}$ | $0.0031x^2 - 0.073x + 1.06$ | 0.99 | |
| | $r_{glucose3}$ | $0.0027x^2 - 0.1066x + 1.3083$ | 0.99 | |
| Taxadiene Production | r_{txd1} | $\frac{\frac{c \ x \ e}{R} \frac{-\Delta \tilde{H}}{R}}{1 + e^{\frac{\Delta S}{R}} \ e^{\frac{-\Delta H}{R}x}}$ | 0.85 | |
| | r_{txd2} | 0 | _ | |

Table B.10.: Formulas Used to Describe the Effect of Production Temperature
on Exchange Rates.

x represents $T_{production}$ in Celsius.

Parameter values for the Arrhenius-like equation providing a good fit to the data were calculated as scaling factors modifying the original parameter values used in [57] as follows: $c = 0.3612 \ e^{24.04}$ should be multiplied by 10.36; $\Delta \tilde{H} = 15.000$ should be multiplied by 1.54; R = 1.9872 (gas constant); $\Delta S = 476.46$ should be multiplied by 1.11; $\Delta H = 150.000$ should be multiplied by 1.08.

 E_i . Results are listed in Table B.11. Overall, concentration time courses for biomass are better described by our model.



Figure B.1.: Modeling Time Course Concentrations: Batch 2. Production conditions corresponds to: $T_{production} = 16^{\circ}C$, $t_{induction} = 1$ h. P_{max} amounted to 1.7614×10^{-4} mmol taxadiene/l h



Figure B.2.: Modeling Time Course Concentrations: Batch 3. Production conditions corresponds to: $T_{production} = 22^{\circ}C$, $t_{induction} = 7.25$ h. P_{max} amounted to 7.7892×10^{-4} mmol taxadiene/l h



Figure B.3.: Modeling Time Course Concentrations: Batch 4. Production conditions corresponds to: $T_{production} = 37^{\circ}C$, $t_{induction} = 7.25$ h. P_{max} amounted to 1.8304×10^{-4} mmol taxadiene/l h



Figure B.4.: Modeling Time Course Concentrations: Batch 5. Production conditions corresponds to: $T_{production} = 22^{\circ}C$, $t_{induction} = 6.25$ h. P_{max} amounted to 4.5526×10^{-4} mmol taxadiene/l h



Figure B.5.: Modeling Time Course Concentrations: Batch 6. Production conditions corresponds to: $T_{production} = 27^{\circ}C$, $t_{induction} = 6.25$ h. P_{max} amounted to 9.2615×10^{-4} mmol taxadiene/l h

 Table B.11.: Determination Coefficients for All Batches.
 For average calculation, only positive values are considered.

| Batch ID | Biomass | Glucose | Taxadiene |
|----------|---------|---------|-----------|
| 1 | 0.982 | 0.923 | 0.912 |
| 2 | 0.994 | 0.934 | 0.982 |
| 3 | 0.993 | 0.756 | 0.629 |
| 4 | 0.878 | 0.926 | -0.634 |
| 5 | 0.991 | 0.794 | 0.809 |
| 6 | 0.862 | 0.770 | 0.627 |
| Average | 0.950 | 0.850 | 0.792 |