## Combining a Helmholtz solver with the Flame Describing Function to assess combustion instability in a premixed swirled combustor

C. F. Silva<sup>1,a</sup>, F. Nicoud<sup>2,b</sup>, T. Schuller<sup>3,c,d</sup>, D. Durox<sup>4,c,d</sup>, S. Candel<sup>5,c,d,e</sup>

<sup>a</sup> Technische Universität München D-85747 Garching, Germany <sup>b</sup> Université Montpellier II, 34095 Montpellier, France <sup>c</sup> CNRS, UPR 288 Laboratoire d'Energétique Moléculaire et Macroscopique, Combustion (EM2C) Grande Voie des Vignes, 92295 Châtenay-Malabry, France <sup>d</sup> Ecole Centrale Paris, 92295 Châtenay-Malabry, France <sup>e</sup> Institut Universitaire de France

## Abstract

Limit cycles of combustion instabilities can be estimated by studying the nonlinear behavior of flame dynamics. In the present study the flame describing function (FDF) framework is combined with a linear acoustic Helmholtz solver in order to estimate the growth rate of the acoustic perturbations in a swirled combustor. It is assumed that when this growth rate equals the inherent dissipation of the system, acoustic oscillation amplitudes cease to grow and a stationary state, i.e., limit cycle, is reached. In the same way, the FDF is combined with an analytical acoustic model for a quasi-1D version of the combustor. Numerical and analytical results are compared to experimental data and a reasonable agreement is obtained in terms of frequency, growth rate and amplitude of oscillations at the limit cycle.

*Keywords:* Combustion instabilities, Flame Describing Function (FDF), Helmholtz solver, limit cycle.

<sup>1</sup>Corresponding author. Post-doctoral fellow, Technische Universität München

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Email address: kamilosilva@gmail.com (C. F. Silva )

<sup>&</sup>lt;sup>2</sup>Professor, Université Montpellier II, I3M - CNRS UMR 5149 - CC51

<sup>&</sup>lt;sup>3</sup>Professor, Ecole Centrale Paris and CNRS

<sup>&</sup>lt;sup>4</sup>Professor, Ecole Centrale Paris and CNRS

<sup>&</sup>lt;sup>5</sup>Professor, Ecole Centrale Paris and CNRS, also with Institut Universitaire de France