

1 **AUTONOMOUS VEHICLES AS SENSORS: TRAFFIC STATE ESTIMATION**

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5 **Yunfei Zhang, Corresponding Author**

6 Chair of Traffic Engineering and Control, Technical University of Munich (TUM)

7 Arcisstrasse 21, 80333 Munich, Germany

8 yunfei.zhang@tum.de

9 ORCID:0000-0003-1902-1816

10

11 **Jeremias Gerner**

12 Almotion Bavaria, Technische Hochschule Ingolstadt

13 Ingolstadt, Germany

14 jeremias.gerner@thi.de

15 ORCID:0000-0002-1611-5086

16

17 **Mario Ilic**

18 Chair of Traffic Engineering and Control, Technical University of Munich (TUM)

19 Arcisstrasse 21, 80333 Munich, Germany

20 mario.ilic@tum.de

21 ORCID: 0000-0003-2457-698X

22

23 **Stefanie Schmidtner**

24 Almotion Bavaria, Technische Hochschule Ingolstadt

25 Ingolstadt, Germany

26 stefanie.schmidtner@thi.de

27 ORCID:0000-0003-2300-2159

28

29 **Klaus Bogenberger**

30 Chair of Traffic Engineering and Control, Technical University of Munich (TUM)

31 Arcisstrasse 21, 80333 Munich, Germany

32 klaus.bogenberger@tum.de

33 ORCID:0000-0003-3868-9571

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1 ABSTRACT

2 Integrating autonomous vehicles (AVs) as sensors presents a novel approach to traffic state esti-
3 mation, leveraging both moving and parked cars to enhance data collection and analysis. This
4 paper explores the effectiveness of using AVs as traffic sensors, comparing the performance of
5 a Weighted Spatio-Temporal Estimation (WSTE) method against two baseline methods with and
6 without complete historical data. We employ a camera-based detection system to identify partici-
7 pants in a microscopic traffic simulation, explicitly model the parked vehicles, and gather data from
8 moving and parked observers at varying penetration rates. By comparing the estimation accuracy
9 of link-level densities from observers and lanes, we demonstrate that moving and parked vehicles
10 can complement each other using the new camera-based detection method, especially with differ-
11 ent penetration rates. Our Weighted Spatio-Temporal Estimation method has also been proven to
12 reach high accuracy, with even one observation from the historical data.

13

14 *Keywords:* Autonomous Vehicles as Sensors (AVaS), Autonomous Vehicles, Traffic State Estima-
15 tion, Detection, Extended Floating Car Data (xFCD)

1 INTRODUCTION

2 Background and Motivation

3 Traffic state estimation plays a critical role in traffic engineering. Precise estimation and predic-
4 tion can significantly benefit traffic control measures and long-term planning. Accurate traffic state
5 estimation is fundamental for improving road safety, reducing congestion, and optimizing trans-
6 portation infrastructure. In recent years, research methodologies have expanded to include both
7 model-based and data-driven approaches, mainly due to the huge number of available data sets.

8 Collecting traffic data forms the foundation for practical traffic state estimation. Tradi-
9 tionally, traffic data collection methods, such as manual counting and loop detectors, have been
10 labor-intensive and cost-prohibitive. However, the rise of autonomous vehicles (AVs) and intelli-
11 gent transportation systems (ITS) has introduced novel methodologies leveraging sensor data from
12 diverse sources. AVs, equipped with advanced sensor technologies such as LiDARs, radars, and
13 cameras, can collect variant traffic data. These vehicles typically serve as moving observers, per-
14 sistentlly acquiring real-time traffic data while circulating in complex urban road networks.

15 Motivated by the fact that the data from AVs are already there, we propose an innovative
16 approach known as Autonomous Vehicles as Sensors (AVaS) (1), given AVs' inherent data collec-
17 tion capabilities. This approach utilizes AVs in both motion and parked states to compile valuable
18 data for traffic state estimation, unlike traditional Floating Car Data (FCD) or Extended Floating
19 Car Data (xFCD), which relies solely on vehicles in motion and provides information only about
20 the ego-vehicle, AVaS benefits from both moving and parked observers within the network. Addi-
21 tionally, on-board vehicle sensors offer supplementary information about other road users. Since
22 AVs can be centrally regulated, they can be strategically assigned to specific locations to gather
23 data, mainly when not privately owned, such as Autonomous Mobility on Demand (AMoD) fleets.

24 By applying the AVaS idea, traffic state estimation can be expanded to include microscopic
25 and macroscopic scales. On the microscopic scale, AVs can estimate traffic states such as densities
26 and link speeds for individual road segments. Concurrently, these data can be aggregated for
27 macroscopic traffic parameters like average speed, volume, and density at the cluster or network
28 level.

29 This study aims to explore the potential of leveraging AVs as sensors for link-level traffic
30 state estimation, specifically for density estimation. By simulating the data collection process
31 using real sensor attributes (2) and applying the AVaS concept to a real-world traffic network in
32 Ingolstadt, Germany, we seek to estimate and predict traffic states using both moving and parked
33 vehicles.

34 Literature Review

35 Traffic state estimation (TSE) methods highly depend on the available data types. While traditional
36 TSE methods rely on stationary detector data, more modern approaches use probe vehicle (PV)
37 data of different types. Table 1 gives an overview of the use of different sensor types for TSE.

38 Using traffic data from moving vehicles for traffic engineering and control originated in
39 1954 when Wardrop and Charlesworth (13) introduced the moving observer (MO) method. This
40 technique involved estimating speed and traffic flow through manual observations of surrounding
41 traffic in both directions, including counting the number of vehicles overtaking or being overtaken
42 and oncoming vehicles. With advancements in vehicle sensor technology over the past decades,
43 onboard sensors in Connected and Autonomous vehicles (CAVs) can now acquire data on sur-
44 rounding traffic conditions, providing extended Floating Car Data (xFCD) for use in ITS applica-

	Stationary Detectors	Probe Vehicles (PVs)		
		Conventional PVs	PVs with spacing measurement	Automated Vehicles
Installed Sensors	Loop detectors, cameras	Global Positioning System (GPS)	GPS & Long Range Radar (LRR)	GPS, LRR, LiDAR, camera
Collected Raw Data	Vehicle counts over time	PV's trajectory	PV's & proceeding vehicle's trajectory	GPS, LRR, LiDAR, camera
TSE possible	yes	no	yes	yes
Literature	(3, 4)	(5–7)	(8–11)	(1, 12)

TABLE 1: Overview of the usage of different sensor types for traffic state estimation (TSE)

1 tions. Table 2 summarizes and classifies simulation studies conducted in the last years on the MO
2 method.

3 Previous work has expanded the MO method into various aspects. From the perspective
4 of transportation modes, Czogalla and Naumann (15) and Kühnel et al. (17) examined the im-
5 pact of different types of moving observers on traffic flow estimation, considering both passenger
6 cars and public transit. When considering the calculated traffic parameters, most reviewed litera-
7 ture primarily focuses on determining instantaneous link-based fundamental traffic flow variables,
8 such as traffic volume, speed, and density. Czogalla and Naumann (15) and Schäfer and Hoyer
9 (19), Schäfer (28) also explored the calculation of link-based travel times from recorded traffic
10 parameters. Additionally, Langer et al. (24) derived queue lengths at intersections from relative
11 flow data collected from oncoming traffic flows.

12 Regarding estimation methods, Florin and Olariu (18) introduced a data-driven approach
13 using machine learning to predict traffic flow characteristics based on continuous data streams from
14 mobile sensors. Guerrieri et al. (22) explored data fusion techniques to enhance the accuracy and
15 completeness of traffic data through multiple moving observers. Furthermore, Ma and Qian (26)
16 integrated machine learning techniques with moving observers to improve prediction accuracy.

17 Overall, past studies focus on using moving observers for traffic data collection. These
18 studies have offered valuable insights into the potential applications and limitations of MO data
19 but have also revealed specific gaps: 1) Current literature emphasizes data collection during mo-
20 tion, with limited exploration of stationary scenarios; 2) The estimation is based on the processed
21 data, i.e., the data have been collected and are ready for estimation, and 3) Estimation for MFD is
22 generally biased, especially for moving observers. To address these research gaps, we introduced
23 our approach, Autonomous Vehicles as Sensors (AVaS) (1, 2). In (1), we first introduced this con-
24 cept and verified the idea in a grid network using the Macroscopic Fundamental Diagram (MFD).

Source	Year	Observer Vehicle		Direction		Recorded Traffic Parameters				Calculated Traffic Parameters				
		Passenger Car	Public Transportation	Same-Directional	Oncoming Traffic	Relative Flow (same-directional)	Relative Flow (oncoming traffic)	Link Travel Time	Avg. Speed (of detected vehicles)	Traffic Volume	Speed	Traffic Density	Travel Time	Queue Lengths at Intersections
Mulligan and Nicholson (14)	2002	x			x		x	x		x				
Czogalla and Naumann (15)	2007		x	x	x	x	x		x			x		
Wolf et al. (16)	2008		x		x					x				
Kühnel et al. (17)	2009	x	x		x	x	x		x					
Florin and Olariu (18)	2016	x		x			x	x		x				
Schäfer and Hoyer (19)	2017	x		x	x	x	x		x	x		x		
Schäfer and Hoyer (20)	2017	x		x	x	x	x		x	x		x		
van Erp et al. (21)	2018	x		x			x			x				
Guerrieri et al. (22)	2019	x		x	x	x	x		x	x				
van Erp et al. (23)	2019	x		x			x			x				
Langer et al. (24)	2020	x			x									x
van Erp et al. (25)	2020	x		x	x	x								
Ma and Qian (26)	2021	x		x	x	x	x			x				
Florin and Olariu (27)	2023	x		x	x	x	x							
Zhang et al. (1)	2023	x		x	x	x	x			x				

TABLE 2: Literature overview of simulation studies on the moving observer method

1 Based on this result, we extended the concept in (2) by simulating the data collection process with
2 sensor attributes and multi-level estimation in a calibrated city-level simulation. However, the lim-
3 itations include: 1) occlusion is not included, and 2) the point estimation is not accurate enough.
4 In this paper, we try to work on these two limitations further.

5 **Contributions and Research Questions**

6 To tackle the current research gaps, we utilize an emulation of a camera-based detection within
7 the microscopic simulation, model the parked vehicles as observers, and improve our local traffic
8 density estimation methods based on spatio-temporal correlations. Therefore, our contributions
9 can be summarized as the following three:

- 10 1. Implementation of camera-based detection: we apply an emulation of a camera-based
11 detection, a neural network architecture trained on a computer vision-based evaluation
12 if vehicles are detectable by the observer based on (12). Compared to distance-based
13 detection methods we used in the previous paper (1, 2), it is more realistic as it includes
14 occlusion.
- 15 2. Modeling parked vehicles as sensors: We model the parked observers by adding parking
16 lots based on real-world demand and use the parked vehicles to detect the surrounding
17 traffic.
- 18 3. Estimation density based on spatio-temporal correlations: instead of focusing on the
19 road section where our observers are located, we utilize all vehicles within a defined
20 area and estimate the link-level density based on the weights from both spatial and
21 temporal perspectives. The results are also compared among different penetration rates.

22 To achieve these three contributions, we develop our research questions accordingly:

- 23 1. How accurately can the camera-based detection method detect surrounding traffic com-
24 pared to distance-based methods?
- 25 2. How much information can parked observers provide to estimate the traffic?
- 26 3. How does our Weighted Spatio-Temporal Estimation (WSTE) method compare to base-
27 line methods?

28 **METHODOLOGY**

29 The methodology can be summarized in Figure 1. With a well-calibrated SUMO simulation, we
30 first simulate both moving and parked observers with different penetration rates. Second, we use
31 two data collection methods, distance- and Neural Network (NN)-based detection methods. With
32 the outputs from moving and parked observers, we applied different estimation methods for point
33 calculation and area estimation. Point estimation targets for the raw data collected from the ob-
34 servers. A ‘detected’ dictionary will be returned at each timestamp for an individual observer.
35 Point estimation refers to estimating the local density based on these data. Area estimation is
36 based on the edges/lanes. Because an edge/lane does not always have an observer, we use an area
37 surrounding the edge/lane to estimate its density. All the observers inside this area will be consid-
38 ered to estimate the densities. Note that the highlighted modules and parameters in the flowchart
39 represent a sensitivity analysis. Therefore, we will compare between:

- 40 1. Moving observers vs. parked observers
- 41 2. Different penetration rates
- 42 3. Distance- vs. NN-based detection
- 43 4. Different area estimation methods

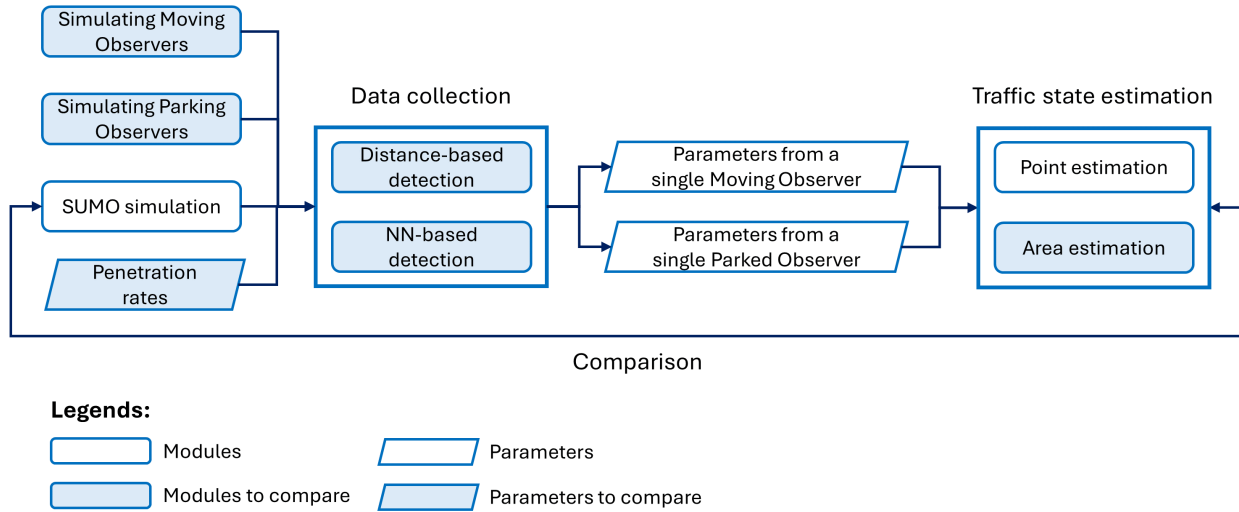


FIGURE 1: Flowchart of the methodology

1 Simulating Moving and Parked Observers

2 In our research, we detect other traffic participants from both Moving Observers (MO) and Parked
 3 Observers (PO). For the MO, we classify each spawned vehicle as an observer or a non-observer
 4 based on the investigated penetration rate. The vehicle routes remain unchanged and adhere to
 5 the traffic demand specifications defined in (29). Since the traffic network of Ingolstadt, created
 6 in (29), does not include parked vehicles, we adapt the network to enable roadside parking on
 7 all edges, as illustrated in Figure 3. We define a parking density, representing the proportion of
 8 parking spots randomly occupied by vehicles. During the simulation, parked vehicles do not affect
 9 the traffic demand of moving vehicles.

10 Detection and Data Collection

11 To accurately estimate the capabilities of AVaS for traffic state estimation in a microscopic simula-
 12 tion, it is essential to identify which vehicles can be recognized by the corresponding moving and
 13 parked observers, as would be the case in a real-world scenario with corresponding sensors and 3D
 14 object detection algorithms. As the first detection method, we use a distance-based method as in
 15 the previous work (2). The Distance-based detection computes the Euclidean distance between the
 16 ego and nearby vehicles. A vehicle is added to the detected list if the distance lies within specific
 17 thresholds (detection ranges) $d_l^{f/b}$ for lane l in both forward f and backward b directions. In this
 18 paper, we select three different distances $[25, 50, 100]$ meters for $d_l^{f/b}$. This time, we do not differ-
 19 entiate vehicles from different lanes or even the opposite direction instead of detecting vehicles in
 20 the same lane. This simplification significantly accelerates the simulation and calculation.

21 However, This distance-based detection overestimates real-world sensors' detection capabilities, as
 22 analyzed in (30). We apply an alternative approach introduced in (12) to address this. This method-
 23 ology approximates camera-based detection of other traffic participants, using the KITTI (31)
 24 thresholds as a reference. We at this moment utilize the NN approach presented in the paper
 25 for fast inference. To implement this approach, we first generate a dataset, which is subsequently
 26 used to train the neural networks. Following the methodology outlined in (12), the dataset is cre-
 27 ated by converting the two-dimensional SUMO simulation into a three-dimensional point-cloud

1 representation. This involves utilizing the polynomial representations of buildings from SUMO
 2 and employing realistic three-dimensional meshes for the vehicles, as shown in Figure 2. We at-
 3 tach emulated camera sensors to both parked and moving vehicles within this representation. In
 4 this study, we have mounted four camera sensors on the observers, specifically at the front, rear,
 5 left, and right sides. The point cloud data of the vehicles and buildings are subsequently projected
 6 onto the camera plane of the emulated sensors. This projection produces a depth-image-like rep-
 7 resentation on the camera plane, including object assignments for the projected points as shown
 8 in Figure 2. Using the KITTI thresholds, we can approximate which vehicles would be detectable
 9 in a comparable real-world scenario, utilizing real-world RGB-camera sensors and state-of-the-
 10 art 3D object detection algorithms. With this so-called computer-vision approach, it is, therefore,
 11 possible to determine which other traffic participants are detectable and available for the traffic
 12 state estimation by the moving and parking observers. The projection of the point clouds onto the
 13 camera plane is computationally expensive, which results in a reduction of the simulation speed of
 14 up to 10 seconds for each observer. Consequently, we use the computer vision approach solely to
 15 generate a dataset for training neural networks, which then emulate the computer vision process
 16 directly from a Bird’s Eye View (BEV) representation of the simulation. Each data point consists
 17 of the BEV representation, where an example is shown in Figure 2, of the current traffic situa-
 18 tion centered around the observer, the two-dimensional vector from the observer to the vehicle for
 19 which detectability is to be determined, and the corresponding binary detectable label derived from
 20 the computer vision approach. In this fashion, we generate 100,000 data points. With these data
 21 points, we then train the NNs where we specifically use an adapted version of the Vision Trans-
 22 former presented in (32). After training, the model achieves an accuracy of over 94% on the test
 23 split, i.e., in 94% of the cases, the NNs correctly determine if a vehicle is detectable according to
 24 the computer vision approach. The significant benefit of the NN approach is the inference speed,
 25 i.e., the duration it takes to determine if a vehicle is detectable by the observer. On average, the
 26 NN approach requires 0.05 seconds to determine the detectability of all surrounding vehicles per
 27 observer.



FIGURE 2: Visualization of the three-dimensional point cloud surrounding the observer under investigation (left), the corresponding depth image captured by the front camera (center), and the BEV representation of the same scene utilized for the NN approach (right).

28 Traffic State Estimation

29 **Point Calculation** Based on previous studies, we have demonstrated that estimating and predict-
 30 ing speeds v is relatively more straightforward, whereas estimating densities k is generally more
 31 challenging. Consequently, this affects the accuracy of traffic flow calculations, $q = ks$. Therefore,

1 this study specifically focuses on estimating and predicting traffic densities at the link level. For
 2 MO, we estimate the real-time lane density \hat{k} (vehicles/km) of an individual moving observer as
 3 Equation 1.

$$4 \quad \hat{k} = \frac{\hat{n} + 1}{2 \times (d + \frac{L}{2}) \times \bar{n}_l} \times 1000 \quad (1)$$

5 where,

- 6 • \hat{n} : Number of detected vehicles
- 7 • d : Detection distance (m)
- 8 • L : Average car length (m)
- 9 • \bar{n}_l : Number of lanes of the edge

10 However, since a point estimation can be unstable, we cap the estimated density \hat{k} at the
 11 maximum value k_{max} to avoid unrealistic high densities. k_{max} is calculated by the 95% maximum
 12 density from the data. For PO, the density estimation is nearly identical, except the PO itself is not
 13 included in the count.

$$14 \quad \hat{k} = \frac{\hat{n}}{2 \times (d + \frac{L}{2}) \times \bar{n}_l} \times 1000 \quad (2)$$

15 **Area estimation** Area estimation refers to predicting the density of a specific lane by analyzing
 16 the observations from both moving and parked observers within a designated area around that
 17 lane. Unlike point estimation, which focuses on a single observation from a moving or parked
 18 observer, area estimation aggregates data from all relevant observations within the specified area.
 19 To illustrate our Weighted Spatio-Temporal Estimation (WSTE) method, we also develop some
 20 baseline methods to compare.

21 **Baseline, All historical data**

22 For each lane ID i and time interval t , the predicted density $\hat{k}_{i,t}$ is calculated using expo-
 23 nential decay weights:

$$24 \quad \hat{k}_{i,t} = \frac{\sum_{j=1}^N k_{i,t-j \cdot t_0} \cdot w_j}{\sum_{j=1}^N w_j} \quad (3)$$

25 where $k_{i,t-j \cdot t_0}$ is the lane density at the past interval $t - j \cdot t_0$ seconds, w_j is the exponential
 26 decay weight for the j -th past interval, and N is the number of past intervals with available data. t_0
 27 represents the aggregated estimation interval. The exponential decay weight w_j is defined as:

$$28 \quad w_j = \exp(-\lambda \cdot j) \quad (4)$$

29 Where λ is the decay constant determining the decay rate.

30 If no past densities are available for the lane ID i at the specified past intervals, $\hat{k}_{i,t}$ remains
 31 at the same density in the last interval. This approach ensures the predicted density is weighted
 32 more heavily towards recent intervals. This baseline method serves as the high bar for traffic state
 33 estimation because we have all the historical data to predict the next interval.

34 **Baseline, No historical data + MO + PO**

35 For this baseline method, we calculate the predicted density $\hat{k}_{i,t}$ as a weighted mean of the
 36 densities estimated by MO and PO. The weights are denoted by w_{mo} and w_{po} , respectively. The
 37 equation for $\hat{k}_{i,t}$ is given by:

$$\hat{k}_{i,t} = \frac{k_{i,t,mo} \cdot w_{mo} + k_{i,t,po} \cdot w_{po}}{w_{mo} + w_{po}} \quad (5)$$

Where:

- $k_{i,t,mo}$ is the weighted density estimated by MO.
- $k_{i,t,po}$ is the weighted density estimated by PO.

The sum of weights w_{mo} and w_{po} are generated using a Gaussian distribution within a radius r . All MO and PO within the radius r are considered. The distance d is calculated between the MO/PO and the centroid point of the predicted lane. The weights are then calculated based on the distance d using the Gaussian function:

$$w(d) = \exp\left(-\frac{d^2}{2\sigma^2}\right) \quad (6)$$

Where:

- σ is the standard deviation of the Gaussian distribution, often set to a value related to the radius r .

Since this estimation uses the estimation from MO and PO and no historical data have been considered, we use this method as the baseline for the low bar for traffic state estimation.

Weighted Spatio-Temporal Estimation (WSTE)

This method combines the power from both spatial and temporal perspectives. We start with an initial value k_{t_0} , which is the true density at the initial timestamp t_0 . This initial density is from the simulation simulation and is the only information we use from the historical data. We also retrieve the initial observations from MO $k_{i,t_0,mo}$ and/or PO and $k_{i,t_0,po}$.

At each subsequent timestamp, we calculate the difference ($\Delta_{i,t}$) between the observed density at the current timestamp $k_{i,t,mo}$ and $k_{i,t,po}$ and the initial density $k_{i,t_0,mo}$ and PO and $k_{i,t_0,po}$, then use this difference to adjust the initial density proportionally.

The formula for the predicted density $\hat{k}_{i,t}$ at timestamp t is given by:

$$\hat{k}_{i,t} = k_{t_0} \times (1 + \Delta_{i,t,mo}) \quad (7)$$

or

$$\hat{k}_{i,t} = k_{t_0} \times (1 + \Delta_{i,t,po}) \quad (8)$$

Where:

- $\hat{k}_{i,t}$ is the predicted density at timestamp t .
- $\Delta_{i,t,mo}$ is the percentage change in density observed by MO between t_0 and t .
- $\Delta_{i,t,po}$ is the percentage change in density observed by PO between t_0 and t .

The percentage delta $\Delta_{i,t}$ is calculated as:

$$\Delta_{i,t,mo} = \frac{k_{i,t,mo} - k_{i,t_0,mo}}{k_{i,t_0,mo}} \quad (9)$$

or

$$\Delta_{i,t,po} = \frac{k_{i,t,po} - k_{i,t_0,po}}{k_{i,t_0,po}} \quad (10)$$

1 Also, we combine these two differences using the weighted method we mentioned for the
2 baseline. The combined predicted density $\hat{k}_{i,t}$ is given by:

$$3 \hat{k}_{i,t} = \frac{(k_{t_0} \times (1 + \Delta_{i,t,mo})) \cdot w_{mo} + (k_{t_0} \times (1 + \Delta_{i,t,po})) \cdot w_{po}}{w_{mo} + w_{po}} \quad (11)$$

4 By applying these calculations, we can compare the influence from MO-only, PO-only, and
5 the combined influence. Since the point estimation is biased, the idea behind the WSTE is to use
6 the change of observations instead of the observations to estimate the traffic densities.

7 **Metrics** In this part, we present the equations and explanations for three commonly used error
8 metrics in traffic state estimation: Root Mean Squared Error (RMSE), Coefficient of Determination
9 (R^2), and Mean Absolute Percentage Error (MAPE).

10 **Root Mean Squared Error (RMSE)**

11 The RMSE measures the average magnitude of the errors between the predicted values and
12 the actual values. It is defined as follows:

$$13 \text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2} \quad (12)$$

14 Where:

- 15 • n is the number of observations,
- 16 • y_i is the actual value for the i -th observation,
- 17 • \hat{y}_i is the predicted value for the i -th observation.

18 **Coefficient of Determination (R^2)**

19 The R^2 metric, also known as the Coefficient of Determination, measures the proportion
20 of the variance in the dependent variable that is predictable from the independent variable(s), as
21 shown here:

$$22 R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2} \quad (13)$$

23 Where:

- 24 • y_i is the actual value for the i -th observation,
- 25 • \hat{y}_i is the predicted value for the i -th observation,
- 26 • \bar{y} is the mean of the actual values.

27 **Mean Absolute Percentage Error (MAPE)**

28 The Mean Absolute Percentage Error (MAPE) evaluates the accuracy of a predictive model
29 by calculating the percentage difference between actual and predicted values. We include MAPE
30 alongside Root Mean Square Error (RMSE) to assess errors in terms of absolute volumes and
31 relative percentages.

$$32 \text{MAPE} = \frac{100\%}{n} \sum_{i=1}^n \left| \frac{y_i - \hat{y}_i}{y_i} \right| \quad (14)$$

33 Where:

- 34 • n is the number of observations,
- 35 • y_i is the actual value for the i -th observation,
- 36 • \hat{y}_i is the predicted value for the i -th observation.

1 EXPERIMENTS AND RESULTS

2 In this section, we first describe the simulation environment. Then, we present and discuss the
3 results regarding three research questions.

4 Simulation Description

5 As in (2), we utilize the SUMO simulation in Ingolstadt, Germany, as the whole network was
6 modeled and calibrated in detail (33) as shown in Figure 3. Prior calibrations, including map asso-
7 ciation, traffic light program emulation, and traffic flow calibration, have already been performed
8 on this network in (29).

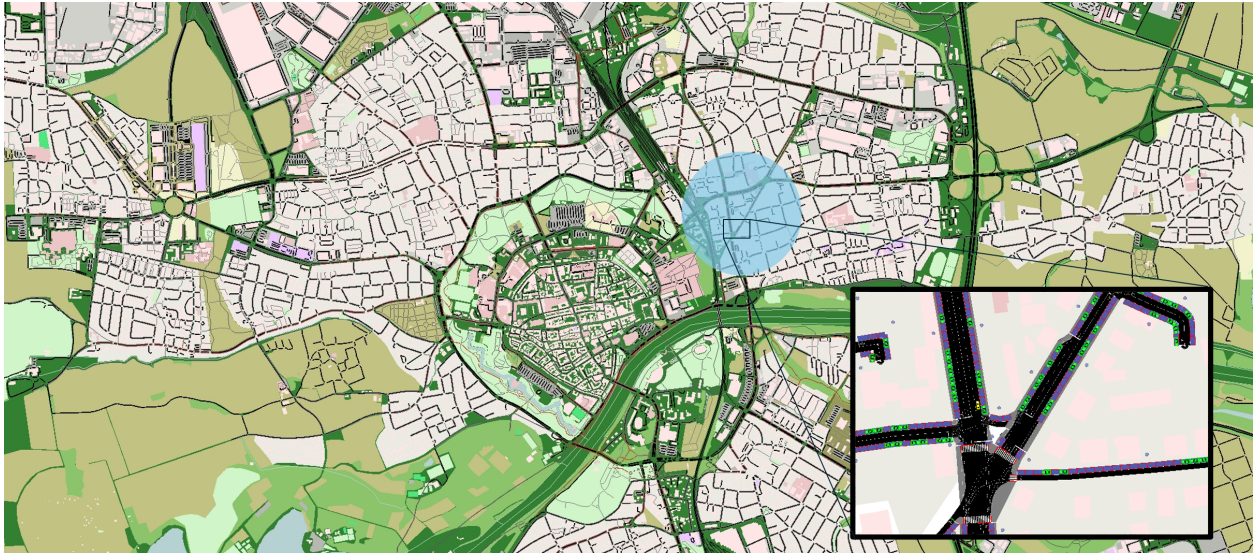


FIGURE 3: SUMO simulation of Ingolstadt, as presented in (29), with the area investigated in this paper highlighted in blue. Additionally, a close-up view illustrates the parked vehicles within the simulation.

9

10 The simulation uses a 5-minute aggregation level to balance efficient results with acceptable
11 temporal resolution. We use the exact interval for all prediction methods, which means $t_0 = 300sec$.
12 Traffic states are evaluated for lanes and edges. We simulate 6 a.m. to 9 a.m. to capture the
13 network accumulation phase while avoiding over-congested networks during the daytime. For
14 both the distance- and NN-based detection, we collect the detected vehicles for the penetration
15 rates [1, 2, 5, 10, 20]% and for a time from 6 a.m. to 9 a.m. with the traffic demand defined
16 in (29). The penetration rates apply to both Moving Observers (MO) and Parked Observers (PO);
17 however, for MO, the penetration rate represents the proportion of MO among all vehicles, while
18 for PO, it indicates the percentage of available parking spots occupied. For simplicity, we assume
19 that 50% of all parking spots are available and then multiply the penetration rates to determine the
20 proportion of PO.

21 For the *Baseline - All historical data method*, we select N , which is the number of past
22 intervals with available data, as 5. This means we consider the past 25 minutes to predict the next
23 5-minute interval. For the *Baseline, No historical data + MO + PO*, we select the radius r as $50m$
24 to consider all MO and PO within this distance. And the corresponding standard deviation of the

1 Gaussian distribution σ is one-third of the radius r , which is $50/3 \approx 13.3m$.

2 **Results of Detection and Data Collection**

3 First, we compare the point estimation results for different detection methods in Figure 4. Three
4 solid lines stand for the distance-based methods and a dashed line for the camera-based NN
5 method. For moving observers to the left, distance-based detection methods have better perfor-
6 mances as they can detect all vehicles without occlusion; however, we notice two phenomena:
7 first, distance-based methods perform the best when considering all the vehicles within 50 meters;
8 second, the error increases after reaching the lowest point as 2% penetration rates. It implies that
9 with high penetration rates, there could be 1) *Repeated Detection*, i.e., one vehicle can be detected
10 by multiple observers, thus causing overestimating, 2) a short detection distance (25-meter) could
11 result in unstable estimation, while a long one (100-meter) could intensify the repeated detection.
12 These can be because we do not collect the information on which lane or direction the detected
13 vehicle is located, as we explained in Subsection 3.2. The emulation of the camera-based detection
14 generally performs worse than the distance-based detection. This is caused by the reduced number
15 of detected vehicles since the method considers occlusion as it would occur by real-world sensors.

16 However, this trend is different for PO: first, the NN method, which also takes occlu-
17 sions into account, can outperform the short (25-meter) and long (100-meter) range distance-based
18 methods; second, the errors among different methods drop down the lowest point at roughly 10%
19 penetration rate. The most important reason is the vast difference between MO and PO: whether
20 the observer counts itself into density calculation. From the previous study (2), we already proved
21 that MO is biased, especially during an off-peak time, because the section where one MO is located
22 will be at least one vehicle, while most of the section could be empty. This bias can be solved with
23 PO, and *Repeated Detection* could be less common. We also notice that since POs are located at
24 roadside parking spaces, they have fewer possibilities for repeated detection.

25 Note that, in reality, we can never achieve distance-based detection. AVs still rely on
26 cameras and other sensors to detect the surrounding traffic. Therefore, **we will only apply the NN**
27 **detection for the remaining analyses.**

28

29 **Results of Point Estimation**

30 Figure 5 compares the point estimation for MO and PO with different penetration rates. Due to
31 the essence that the detected vehicles can be spread among different lanes, the point estimation is
32 supposed to be and also proved in the figure to be scattered widely. In general, we can conclude that
33 in Figure 5(a), moving observers tend to overestimate the densities, especially when the demand
34 is relatively low, while parked observers have a better estimation of the traffic densities in Figure
35 5(b).

36 Because of the inherent biases in both observers, we do not focus on improving estimating
37 densities for a single observation from an observer. Since the ultimate goal is to estimate or predict
38 the traffic densities at the link level, we try to include these point estimation results in the traffic
39 state estimation with other knowledge.

40 **Results of Traffic State Estimation**

41 Following the methods of TSE, which we introduce in Section 3.3, we compare two baseline
42 methods and three Weighted Spatio-Temporal Estimation (WSTE) methods in Figure 6. Note that

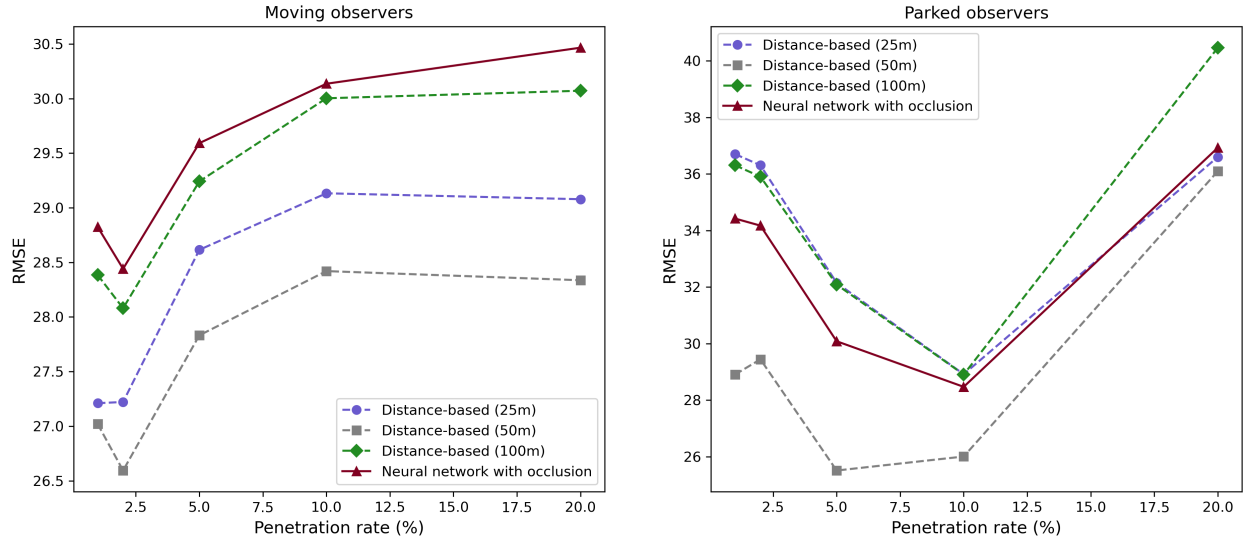


FIGURE 4: Comparison among different detection methods: the NN with occlusion method is not accurate enough as distance-based methods in MO, while can achieve a similar level using PO

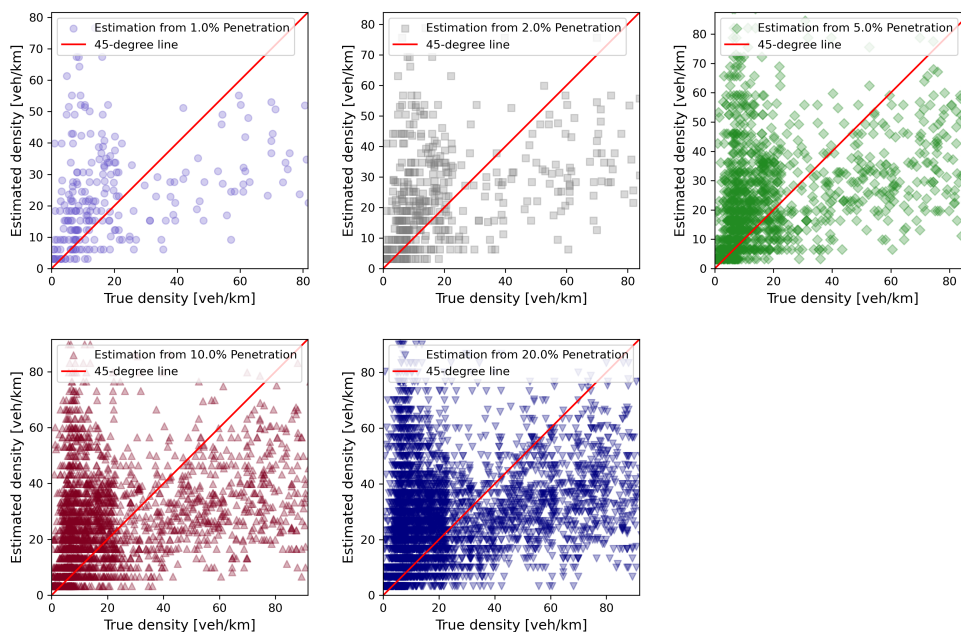
1 two baseline methods are visualized in both figures, while in the correct figure for R^2 , the R^2 value
 2 for *Baseline, No historical data + MO + PO* is below 0 and is invisible from the visualization area.

3 For RMSE, *Baseline, All historical data* leads with the slightest error. In comparison,
 4 without historical data, *Baseline, No historical data + MO + PO* still tends to have not too big
 5 error thanks to the spatial weights. However, both baselines have no significant improvements in
 6 accuracy after the penetration rates reach 5%, implying the limitations of both observers. *Weighted*
 7 *Spatio-Temporal Estimation (WSTE)* have entirely different trends. With only the true density at
 8 the first timestamp, *Initial historical data + MO* can reduce the error by increasing penetra-
 9 tion rates to 10%. The error increases again at 20%, most probably due to the *Repeated Detection*
 10 thus, overestimation. *Initial historical data + PO*, on the other hand, constantly reduces errors
 11 with increased penetration rates. The resulting mixed method *Initial historical data + MO + PO*
 12 is more towards the *Initial historical data + MO* side, implying the higher weights from the MO
 13 side.

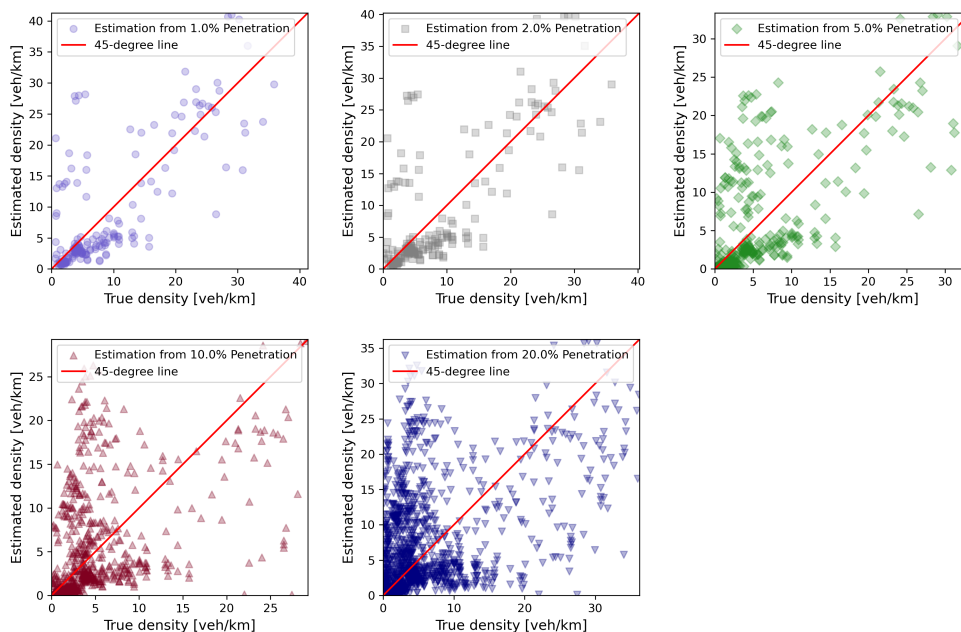
14 Results for R^2 are different, especially for *Baseline, No historical data + MO + PO*. The
 15 negative R^2 indicates that this baseline method might not compete with an estimation based on the
 16 historical average. This might be because without knowing any true densities, the point estimation
 17 from AVaS is unstable. For our WSTE method, we can observe that *Initial historical data + PO*
 18 benefits from the increased penetration rates, while *Initial historical data + MO* is the opposite.
 19 The drop in R^2 value for MO indicates that the variance due to overestimation (*Repeated Detection*)
 20 becomes bigger than the variation of the traffic state. PO always have available spots even with the
 21 increased penetration rates, and this fact makes PO more reliable in avoiding *Repeated Detection*.
 22 That leads to our thinking that we can combine a fleet of MO and PO with different penetra-
 23 tion rates in the future TSE study.

24

25 An overview of all metrics of all scenarios is listed in Table 3. For *Initial historical data +*
 26 *PO* and *Initial historical data + MO*, the overall best penetration rates are bold, again highlighting



((a)) Results of point estimation for moving observers



((b)) Results of point estimation for parked observers

FIGURE 5: Comparison of point estimation for different penetration rates using NN detection methods: MO tend to be more scattered than PO

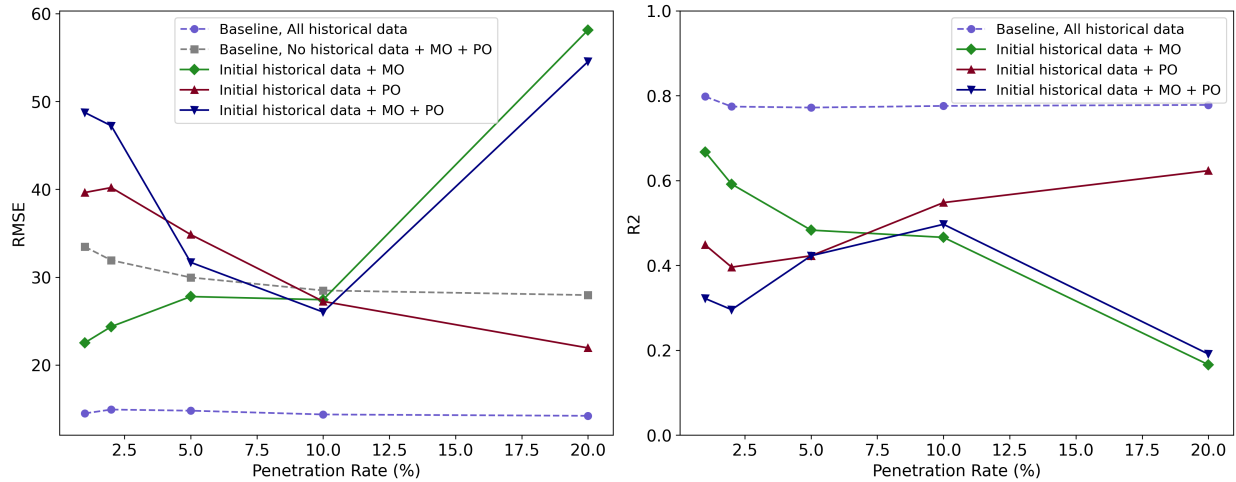


FIGURE 6: Comparison among different estimation methods: compared to two baselines with & without all historical data, our Weighted Spatio-Temporal Estimation (WSTE) method can reach high accuracies with RMSE and R^2 with just initial historical data.

1 that TSE can benefit from different penetration rates from MO and PO.

2 CONCLUSION

3 Summary

4 Originating from the first concept of AV-as-Sensors (AVaS) (1), we simulated the data collection
 5 process in (2). Using the collected data, this study has explored various approaches for traffic
 6 state estimation (TSE). In this study, we 1) implement a new camera-based detection method, 2)
 7 model the parked vehicles in SUMO, and 3) estimate the traffic densities using Weighted Spatio-
 8 Temporal Estimation for moving and parked observers (MO and PO), compared to two baseline
 9 methods. The results show that even with a low penetration rate, MO and/or PO can have a rather
 10 good estimation of local densities with just one initial true observation. Thus, we answer our
 11 research questions raised in Section 2.3 as follows:

- 12 1. *How accurately can the camera-based detection method detect surrounding traffic com-*
 13 *pared to distance-based methods?* From the results in 4.2, we can conclude that com-
 14 *pared to distance-based methods, the camera-based detection method can benefit the*
 15 *traffic state estimation at the same level, especially for PO.*
- 16 2. *How much information can parked observers provide to estimate the traffic?* Compared
 17 *to the overestimation from MO, PO can modify the estimation from the results presented*
 18 *in Section 4.3. Also, from the metrics in Section 4.4, we could see that PO overperforms*
 19 *MO, especially with high penetration rates.*
- 20 3. *How does our Weighted Spatio-Temporal Estimation (WSTE) method compare to base-*
 21 *line methods?* Compared with two baseline methods with all historical data (high bar)
 22 *and AVaS-only data (low bar), our WSTE method can almost reach the same accuracy*
 23 *with ground truth with only one initial true observation.*

Condition			Penetration Rate (%)					
Parked	Moving	Historical Data	Metric	1	2	5	10	20
No	No	All	RMSE	14.49	14.93	14.80	14.37	14.22
			R ²	0.798	0.774	0.772	0.776	0.778
			MAPE	0.390	0.400	0.409	0.429	0.428
Yes	Yes	No	RMSE	33.47	31.93	29.96	28.48	27.96
			R ²	-2.809	-2.592	-2.256	-2.519	-2.586
			MAPE	0.988	0.950	0.858	0.803	0.800
No	Yes	Initial (WSTE)	RMSE	22.53	24.37	27.79	27.43	58.13
			R ²	0.667	0.592	0.483	0.466	0.166
			MAPE	0.735	0.785	0.990	1.066	1.531
Yes	No	Initial (WSTE)	RMSE	39.63	40.20	34.85	27.24	21.95
			R ²	0.448	0.396	0.423	0.548	0.623
			MAPE	1.024	1.053	1.101	1.096	1.294
Yes	Yes	Initial (WSTE)	RMSE	48.74	47.23	31.68	26.03	54.54
			R ²	0.322	0.296	0.423	0.497	0.191
			MAPE	0.949	0.921	1.017	0.992	1.572

TABLE 3: Sensitivity Analysis considering impact of parked and moving vehicles, historical data, and penetration rates: our WSTE methods (bold) perform best with high penetration rates for parked observers and low penetration rates for moving observers.

1 Future Research

2 While this study has addressed all the research questions, we admit that this study focuses on traffic
3 densities at the link level, with certain simplifications in the simulation and detection methods.
4 Besides, traffic state estimation is limited to randomly selecting moving and parked vehicles. To
5 address these limitations, we propose future research with different modules in Figure 1.

6 **Module - Simulation** Now, the parked vehicles are randomly selected for available parking spots,
7 which are randomly modeled in the simulation as well. In the future, we plan to investigate the
8 amount of contributions to traffic state estimation from different locations. Thus, a future strategic
9 vehicle assignment algorithm can be developed, so that idle vehicles can park where they can
10 provide the most information and data for traffic state estimation.

11 **Module - Data collection** The current detection status only uses the information on how many
12 vehicles can be "detected" by the ego observer without further information on which lane or direc-
13 tion they are located. Since the emulation is already based on 3D object detection, in the future,
14 we will utilize this information not only for lane-specific but also for the neighboring lane and
15 opposite-direction traffic density estimation.

16 **Module - Traffic state estimation** We already notice in Section 4.4 that moving and parked ob-
17 servers have different trends of performances with increased penetration rates. In the future, instead
18 of using the same penetration rate for both observers, we will conduct the sensitivity analysis for
19 different penetration rates between moving and parked observers. Also, since moving observers

1 are outnumbering parked observers now, the weighted estimation always has higher weights and
2 influences from moving observers. We will update the weighting system in future research as well.

3 By addressing these different modules, our ultimate goal is to use AV-as-Sensors as a sup-
4 plementary or even replace the current fixed-location detector system for traffic state estimation.
5 We will study the possibilities of using this concept by integrating it into the operation of Au-
6 tonomous Mobility-on-Demand systems.

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12 **AUTHOR CONTRIBUTIONS**

13 The authors confirm contribution to the paper as follows: Study conception and design: Yunfei
14 Zhang, Jeremias Gerner, Mario Ilic, Stefanie Schmidtner, Klaus Bogenberger; Data collection:
15 Jeremias Gerner, Mario Ilic; Analysis and interpretation of results: Yunfei Zhang; Draft manuscript
16 preparation: Yunfei Zhang, Jeremias Gerner, Mario Ilic. All authors reviewed the results and
17 approved the final version of the manuscript.

18 **DECLARATION OF CONFLICTING INTEREST**

19 All authors do not have any conflicts of interest to declare.

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