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# Strain hardening behavior of additively manufactured and annealed AlSi3.5Mg2.5 alloy



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#### ABSTRACT

The ductility of the Al alloys produced by additive manufacturing (AM) has become a critical property, as the AM Al alloys are increasingly used in the automotive industry. However, the ductility of as-built AM Al alloys is relatively low, even with optimized AM conditions. The post-annealing treatment provides an efficient way to improve ductility. Previous investigation has shown that the annealed AM AlSi3.5Mg2.5 alloy possesses superior ductility. However, the plastic deformation micro-mechanisms of the annealed AM AlSi3.5Mg2.5 alloy possesses superior ductility. The evolutions of phase stresses, dislocation density, and crystallite size in the annealed AM AlSi3.5Mg2.5 alloy during tensile deformation were analyzed. The experimental investigation reveals that the dislocation density in the Al matrix of the annealed AM AlSi3.5Mg2.5 alloy increases slowly in the early plastic deformation stage, and it reaches a saturated level upon the following uniform deformation. The crystallite size decreases quickly in the early deformation stage, and then it decreases slowly. The Kocks-Mecking model and the Voce model can capture the strain hardening behavior well. The determined physical constitutive equations can be applied in continuum mechanical computer simulations.

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#### 1. Introduction

As the Al alloys are increasingly applied in the automotive industry, their ductility has become a critical property. During an automotive crash incident, the folding and bending components are desirable for energy absorption. Hence, high ductility is crucial to guarantee energy adsorption capacity and vehicle safety. Al components produced via additive manufacturing (AM) that have optimized geometry and reduce the usage of fasteners can provide an excellent lightweight benefit to the automotive industry.

However, the as-built AM Al alloys usually show relatively low ductility [1]. On the one hand, the low ductility is partially associated with defects like the non-negligible porosity, which can be

https://doi.org/10.1016/j.jallcom.2021.162890 0925-8388/© 2021 The Author(s). Published by Elsevier B.V. CC\_BY\_NC\_ND\_4.0 minimized through optimizing the AM conditions [2,3]. On the other hand, the ductility decreases when the strength is high due to a strength-ductility trade-off. Hence, the AM conditions should be optimized to obtain high ductility. Furthermore, a post-heat treatment, e.g., annealing treatment, can be employed.

Compared with the well-known AM AlSi10Mg alloy, a novel AM AlSi3.5Mg2.5 alloy free of rare-earth elements possesses better ductility [4,5]. For instance, Lutz et al. [5] reported that the total elongation of the laser powder bed fusion (LPBF) AlSi3.5Mg2.5 after annealing is 26.7  $\pm$  1.3%, about 31% higher than that of the annealed LPBF AlSi10Mg. Knoop et al. [4] showed that the tight bending angle of the annealed LPBF AlSi3.5Mg2.5 is 96.5  $\pm$  3.0°, almost twice that of the annealed LPBF AlSi10Mg. Additionally, a high strain hardening exponent *n* = 0.18 is measured for the annealed LPBF AlSi3.5Mg2.5 [5], about twice those of the casting Al-Si-Mg alloys [6,7]. Although previous results have indicated a superior ductility of the annealed LPBF AlSi3.5Mg2.5 alloy is not improved much compared with the total elongation [5], limiting its extensive industrial

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Fig. 1. Macroscopic mechanical properties of HTD and HTS upon the in-situ tests: (a) engineering stress-strain curves; (b) true stress-strain and hardening coefficient curves.

applications. Hence, it is essential to clarify the underlying micromechanisms of its plastic deformation to enhance the uniform elongation of the annealed LPBF AlSi3.5Mg2.5 alloy in the future.

Note that the eutectic cell boundaries dissolve after heat treatment at elevated temperatures, and larger  $Mg_2Si$  and Si particles form in the AM Al-Si-Mg alloys [5,8,9]. Such a microstructure variation alters the strain hardening behavior and the dislocation activities [10]. For example, the aging treatment disintegrates the cellular-dendrite pattern and promotes precipitation of  $Mg_2Si$  and Si, increasing strength. The isolated  $Mg_2Si$  and Si particles have weaker constraints to the dislocation motions than the cell boundary network [10].

When the LPBF AlSi3.5Mg2.5 is annealed at 380 °C for one hour, the isolated Mg<sub>2</sub>Si and Si particles have even larger sizes and thereby weaker interactions with dislocations [5]. Meanwhile, the annealing treatment causes static recovery, reducing the dislocation density and, in turn, the strength significantly. Then one question arises: How do the dislocations behave in this annealed microstructure during plastic deformation? This study explores the plastic deformation micro-mechanisms of the annealed LPBF AlSi3.5Mg2.5 alloy to reveal the relationship between the dislocation density and the strain hardening behavior.

The annealed LPBF AlSi3.5Mg2.5 alloy was subjected to an in-situ neutron diffraction experiment. The direct-aged LPBF AlSi3.5Mg2.5 alloy was also investigated for comparison. The dislocation density in the Al matrix was analyzed via the convolutional multiple whole profile (CMWP) approach [11,12]. The phase stresses of Al, Mg<sub>2</sub>Si, and Si were separated. The strain hardening behavior of the Al matrix was qualified by the Kocks-Mecking model [13] and the Voce model [13,14]. The present investigation provides valuable insights into the ductility of the annealed LPBF AlSi3.5Mg2.5 alloy. Meanwhile, the determined physical constitutive equations can be applied for continuum mechanical computer simulations (i.e., finite element analysis of printed components), capable of predicting the novel alloy's mechanical behavior under various loading conditions.

#### 2. Experimental procedure and methodology

#### 2.1. Material and LPBF process

The AlSi3.5Mg2.5 specimens were manufactured vertically using a Concept Laser M2 UP1 cusing laser system (400 W). The LPBF parameters can be found in the previous investigation [10]. The asbuilt cylindrical specimens have a diameter of 14 mm and a length of 104 mm. The specimens (namely HTD) were subjected to an annealing treatment at 380 °C for one hour after LPBF in a circulation air oven followed by cooling down at ambient air. For comparison, the direct-aged specimens (namely HTS) were also investigated. The aging treatment was conducted at 170 °C for one hour after LPBF. The heat-treated specimens were then machined to remove rough surfaces, resulting in the dog-bone-shaped specimens with a total length of 76 mm. The gauge part of the dog-bone-shaped specimens has a diameter of 6 mm and a gauge length of 30 mm [15].

The direct-aged specimens were employed for comparison. The previous investigation showed that the initial dislocation density is almost the same in HTS and as-built alloy [10]. The residual stresses in HTS are partially released due to the stress relaxation effect upon the heat treatment [10]. This should also be the case in the HTD sample due to a higher treatment temperature. Accordingly, the effect of residual stress is reduced in both HTD and HTS. Besides, the microstructure of HTD is closer to that of HTS. In contrast, the asbuilt Al-Si-Mg alloys possess a cellular-dendritic microstructure, causing complex dislocation activities upon plastic deformation that have been reported in our previous investigations [15–17].

## 2.2. Microstructure characterization, ex-situ tensile tests, and fractography observation

The electron backscatter diffraction (EBSD) samples were prepared via ion milling using a Hitachi ArBlade IM5000 system. The EBSD microstructure was analyzed using the electron microscope Zeiss Auriga with EBSD detector Symmetry (Oxford Instruments). The increment was set to  $0.5 \ \mu m$  [10].

Three HTD specimens were subjected to ex-situ tensile tests at a nominal strain rate of  $1.0 \times 10^{-3} \text{ s}^{-1}$ . For multiphase materials, the elastoplastic deformation at the microscale is inhomogeneous. The localized deformation initiates damage and causes a fracture when the applied strain is large enough. This study used a scanning electron microscope (SEM) to analyze the fractured tensile specimens. The fractured specimen was then analyzed for fractography characterization. A Zeiss LEO 1450VP system was used with an acceleration voltage of 15 kV. The imaging view is parallel to the LD during the tensile test and to the building direction during manufacturing (normal to the base plane of the building platform).

#### 2.3. In-situ neutron diffraction experiments

The in-situ neutron diffraction experiment was conducted at the TAKUMI engineering neutron diffractometer of the Japan Proton Accelerator Research Complex (J-PARC) [18]. The specimens were subjected to monotonic tensile tests at room temperature with a nominal strain rate of  $1.1 \times 10^{-5}$  s<sup>-1</sup>. This strain rate is slower than that of the ex-situ tensile tests to guaranty a sufficient acquisition time of neutron diffraction pattern. The applied strain was recorded

#### Table 1

Mechanical properties of the HTD and HTS specimens.

Material	έ, S <sup>-1</sup>	$\sigma_{\rm y}$ , MPa	$\sigma_{ m uts}$ , MPa	EL, %	Reference
HTD	$1.1 \times 10^{-5}$ for in-situ 1.0 × 10 <sup>-3</sup> for ex-situ	77.3 106.0 ± 2.6	141.1 184.0 ± 1.4	- 29.0 ± 1.9	This work This work
HTS	$1.1 \times 10^{-5}$ for in-situ $1.0 \times 10^{-3}$ for ex-situ	381.7 417.1 ± 2.8	462.5 505.3 ± 3.5	9.1 11.0 ± 0.4	This work [10]

Footnote:  $\dot{\varepsilon}$  is the tensile strain rate,  $\sigma_v$  the 0.2% offset yield strength,  $\sigma_{uts}$  the tensile strength, and EL the max plastic strain measured from the strain-stress curve.

using an Epsilon extensometer. The incident beam had a size of  $5 \times 6 \text{ mm}^2$ , and the radial collimators had a width of 5 mm.

The neutron diffraction spectrums were analyzed using the MAUD software to obtain the quantitative contents of all phases [19]. The lattice parameter of each phase was determined using Z-Rietveld software [20] based on the Rietveld refinement method. The average lattice strain  $\bar{\varepsilon}_s^i$  in direction *s* (*s* = loading direction (LD) or transversal direction (TD)) of phase i ( $i = Al, Mg_2Si$ , or Si) is calculated by

$$\bar{\varepsilon}_{s}^{i} = \frac{a_{s}^{i}}{a_{s,0}^{i}} - 1 \tag{1}$$

where  $a_s^i$  is the refined lattice parameter and  $a_{s,0}^i$  the corresponding reference lattice parameter. The LD phase stress  $\bar{\sigma}_{LD}^{i}$  is approximately calculated by

$$\bar{\sigma}_{\rm LD}^i = E_{\rm bulk}^i \bar{\varepsilon}_{\rm LD}^i \tag{2}$$

where  $E_{\text{bulk}}^i$  is the Young's modulus of phase *i*. The CMWP approach was applied to determine the dislocation density and crystallite size of the Al matrix. This CMWP approach developed by Ribarik and Ungar [11,12] has been successfully applied to determine the dislocation densities in various alloys, such as Al alloys [12,21], bainitic steels [22,23], and zirconium hydride [24].

#### 3. Results

#### 3.1. Macroscopic mechanical properties

Fig. 1(a) shows the engineering stress-strain curves of HTD and HTS under in-situ tensile loading. HTD was loaded until 10.4% strain, while the following necking stage was not investigated due to local deformation. HTS was loaded until fracture. The true stress-strain curves ( $\sigma_t$  versus  $\varepsilon_t$ ) and hardening coefficients ( $\Theta = d\sigma_t/d\varepsilon_t$ ) are shown in Fig. 1(b). According to the Considère necking condition  $\Theta = \sigma_t$  [25], the determined uniform strain  $\varepsilon_N$  of HTD and HTS is 9.1% and 5.8%, respectively. The in-situ measured yield and tensile strengths of HTD are 77.3 and 141.1 MPa, respectively. These properties of HTS are 381.7 and 462.5 MPa, respectively. The mechanical properties of HTD and HTS at different tensile strain rates are summarized in Table 1.

#### 3.2. Microstructure and phase compositions

Figs. 2(a) and (b) show the EBSD microstructures in the vertical and horizontal sections, respectively. In the vertical section, columnar grains dominate the grain structure, which is typical in AM alloys. From Fig. 2(a), the grain size was analyzed using the equivalent circle diameter. Statistics indicate that the average grain size in the vertical section is 3.8  $\pm$  0.7  $\mu$ m. Note that the grains at the EBSD image borders were excluded during statistics. The average grain size in the horizontal section is  $3.4 \pm 0.6 \,\mu\text{m}$ . These grain sizes are slightly larger than those of the as-built and direct-aged (HTS) samples [10], indicating slight grain growth in the HTD sample

during the annealing treatment. Besides, the pole figures in Figs. 2(a) and (b) show a characteristic < 001 > 1/Z fiber texture, as expected [10].

Based on the Rietveld refinement analysis of the neutron diffraction spectrums, the determined volume fractions of the Al, Mg<sub>2</sub>Si, and Si phases in HTD are 93.07 ± 0.26%, 4.89 ± 0.24%, and 2.04 ± 0.03%, respectively. The corresponding values in HTS are 94.82 ± 0.34%, 3.65 ± 0.24%, and 1.53 ± 0.10%, respectively. Considering different measuring methods and different specimens, the measured phase contents of HTS in this investigation agree with the previous in-situ synchrotron X-ray diffraction experiment [10]. The volume fractions of Al, Mg<sub>2</sub>Si, and Si in the as-built AlSi3.5Mg2.5 alloy are 95.37%, 3.06%, and 1.56%, respectively [10]. Therefore, additional Mg<sub>2</sub>Si and Si precipitate out in HTD upon the annealing treatment.

#### 3.3. Lattice strains and phase stresses

The average lattice strains of the Al, Mg<sub>2</sub>Si and Si phases in HTD and HTS are shown in Figs. 3(a) and (b), respectively. In the macroscopic elastic stage, all lattice strains are proportional to the applied true stress approximately. Significant errors of the Si lattice strains in HTS exist because of the low Si content and the fine Si particle size (Fig. 3(b)). In the macroscopic plastic stage, the magnitudes of the Al lattice strains increase slowly due to plastic deformation. In contrast, the lattice strains of Mg<sub>2</sub>Si and Si in the LD increase rapidly in the macroscopic plastic stage. Moreover, the Mg<sub>2</sub>Si and Si lattice strains of HTS in the LD decrease from the applied true stress of 472.9 MPa, indicating a damaging stage. This phenomenon has also been detected in the previous investigation [10].

The phase stresses in HTD are shown in Fig. 3(c). The average stresses in the Mg<sub>2</sub>Si and Si phases of HTD are higher than that in the Al phase during plastic deformation. The maximum stresses in the Mg<sub>2</sub>Si and Si phases of HTD are about 764 and 814 MPa. respectively. The average phase stresses in HTS are shown in Fig. 3(d). The measured maximum average stresses of Si and Mg<sub>2</sub>Si in HTS are about 2305 and 1690 MPa, respectively.

#### 3.4. Dislocation density and strain hardening behavior

The initial total dislocation density in HTD is about  $1.40 \times$ 10<sup>14</sup> m<sup>-2</sup>. The total dislocation density increases slowly in the early plastic deformation stage and reaches a saturation value of ~ $6.00 \times 10^{14}$  m<sup>-2</sup> at the applied true strains > 3.5% (Fig. 4(a)). In contrast, the dislocation density in HTS increases largely and continuously with the applied true strain during uniform deformation. With the applied true strain increasing from 0% to 5.7%, the total dislocation density in HTS increases significantly from 3.22×10<sup>14</sup> to  $24.67 \times 10^{14}$  m<sup>-2</sup> (Fig. 4(a)). The total dislocation density during plastic deformation in the present HTS is lower than that in the previous investigation [10], which should be associated with different tensile strain rates. In the present investigation, the in-situ



Fig. 2. EBSD microstructure of the LPBF and annealed AISi3.5Mg2.5 alloy: (a) vertical and (b) horizontal sections.



Fig. 3. Microscopic strains and stresses: average lattice strains in (a) HTD and (b) HTS, (d) phase stresses in (c) HTD and (d) HTS. The error bars of average lattice strains of the Al phase are negligible and are therefore not displayed in (a) and (b).

tensile strain rate was  $1.1 \times 10^{-5} \text{ s}^{-1}$ , whereas it was  $1.5 \times 10^{-4} \text{ s}^{-1}$  in the previous investigation [10]. The total dislocation density includes mobile and forest dislocation densities. According to the Orowan equation, the strain rate  $\dot{\epsilon}$  relates to the mobile dislocation density  $\rho_{\rm m}$  via [26].

$$\dot{\varepsilon} = Mb\rho_{\rm m}\bar{\nu},\tag{3}$$

where *M* is the average Taylor factor, *b* the magnitude of the Burgers vector, and  $\bar{v}$  the average dislocation velocity. If the average dislocation velocity is less sensitive to the strain rate  $\dot{\varepsilon}$ , the mobile dislocation density  $\rho_{\rm m}$  will reduce with decreasing  $\dot{\varepsilon}$ . This could be one reason that the current total dislocation density in HTS is lower than that in our previous investigation [10].



Fig. 4. Evolutions of (a) total dislocation density and (b) volume-weighted mean crystallite size d<sub>volume</sub> in HTD and HTS.

As the dislocation density increases during plastic deformation, dislocation walls form to reduce the elastic energy [27]. Hence, the crystallite size decreases with increasing the dislocation density [28–30]. Fig. 4(b) shows that the volume-weighted mean crystallite size  $d_{volume}$  of HTD decreases from 548 to 243 nm with increasing the applied true strain from 0% to 8.7%, and  $d_{volume}$  of HTS decreases from 351 to 77 nm with increasing the applied true strain from 0% to 5.7%.

#### 4. Discussions

#### 4.1. Load transfer mechanism

Fig. 3 reveals that the lattice strains and phase stresses of Mg<sub>2</sub>Si and Si are much lower in HTD than in HTS. For multiphase materials consisting of ductile matrix and stiff constituent phases, the phase stresses depend on the geometrical features of the phases (e.g., the size, aspect ratio, and distribution of stiff particles [31–33]), the constitutive behavior [34] of all phases, and the properties of interfaces between phases [35,36]. In this study, the yield strength and the flow stress are much lower in HTD than in HTS. Previous crystal plasticity investigation showed that the stress in the stiff phase is low when the matrix's yield strength and flow stress are low due to a weak load transfer effect [37]. Moreover, the Mg<sub>2</sub>Si and Si particles have smaller aspect ratios in HTD (where the particles are nearly spherical [5]) than in HTS (where the particles are less spherical [10]), which also contribute to a weaker load transfer effect in HTD [38].

No apparent damaging effect is detected in the Mg<sub>2</sub>Si and Si phases of HTD because the phase stresses are relatively low. In contrast, the lattice strains and phase stresses of Mg<sub>2</sub>Si and Si in HTS are very high. An apparent damaging phenomenon is detected in HTS, i.e., the Mg<sub>2</sub>Si and Si lattice strains in the LD decrease after the applied true stress of 472.9 MPa.

#### 4.2. Strain hardening mechanism

During strain hardening stage, the relationship between dislocation density  $\rho$  and mechanical stress  $\sigma$  can be evaluated by the Taylor equation [39].

$$\sigma = \sigma_0 + M \alpha \mu b \sqrt{\rho}, \tag{4}$$

where  $\sigma_0$  is the initial friction stress, the average Taylor factor M = 3.06 for face-centered cubic metals with random texture [40,41],  $\alpha$  the strengthening coefficient,  $\mu$  the shear modulus ( $\mu = 26.38$  GPa for Al), and *b* the Burgers vector (b = 0.286 nm for Al).

In this investigation, large measurement errors exist in the LD and TD strains of the Si phase. Moreover, the Si TD strain at the applied true strains > 3.6% cannot be determined. Therefore, Eq. (2) was employed to determine the average stresses in all phases approximately. Figs. 5(a) and (b) show the Al phase stress versus  $\sqrt{\rho}$  relation for HTD and HTS, respectively. Both of them can be predicted by the Taylor equation. The determined values of the strengthening coefficient  $\alpha$  for the Al phase in HTD and HTS are 0.10 and 0.046, respectively. The latter one agrees with the previous value ( $\alpha = 0.047$  for the Al phase in HTS) determined from in-situ synchrotron X-ray diffraction [10].

Furthermore, the strain hardening behavior can be described by the Kocks-Mecking (K-M) model [13,42], which qualifies the relation between dislocation density and plastic strain. The original K-M model reads [13].

$$\frac{d\rho}{d\varepsilon_{\rm p}} = k_1 \sqrt{\rho} - k_2 \rho, \tag{5}$$

where the parameter  $k_1$  is associated with the thermal storage of mobile dislocations, and the parameter  $k_2$  accounts for the dislocation annihilation due to dynamic recovery. With constant parameters  $k_1$  and  $k_2$  at a certain microstructure, Eq. (5) can be integrated into [10].

$$\varepsilon_{\rm p} = k_0 - \frac{2}{k_2} \ln |k_1 - k_2 \sqrt{\rho}|,$$
 (6)

where  $k_0 = (2 \ln |k_1 - k_2 \sqrt{\rho_0}|)/k_2$ , and  $\rho_0$  is the initial dislocation density.

Figs. 5(c) and (d) show the evolutions of Al plastic strain with  $\sqrt{\rho}$ for HTD and HTS, which are well captured by a monotonous K-M model. It can be seen that the  $k_1$  value of HTD is only ~54% of the HTS one, while the  $k_2$  value of HTD is ~128% of the HTS one. Compared with HTS, a much smaller  $k_1$  value in HTD indicates a much lower dislocation storage rate in HTD, while a higher  $k_2$  value in HTD reveals a higher dislocation annihilation rate in HTD. The differences in the  $k_1$  and  $k_2$  parameters between HTD and HTS should be associated with the microstructure. Firstly, a static recovery process occurs during the annealing process, reducing the total dislocation density in HTD. The dislocation densities in Fig. 4(a) show that the initial dislocation density in HTD is only about 43% of that in HTS. Secondly, the Mg<sub>2</sub>Si and Si particles are larger and more spherical in HTD, decreasing the stress concentrations during plastic deformation. Thirdly, the crystallite size is larger in HTD than in HTS (Fig. 4(b)). These results reveal that the densities of dislocation sources and obstacles in HTD are lower than those in HTS. Accordingly, HTD exhibits a lower dislocation-storage rate and a higher dislocationannihilation rate than HTS.



**Fig. 5.** Relationships between the dislocation density, Al phase stress, and plastic strain for (left) HTD and (right) HTS: (a) and (b) Al stress versus  $\sqrt{\rho}$ ; (c) and (d) plastic strain versus  $\sqrt{\rho}$ ; (e) and (f) Al stress versus plastic strain.

Following the K-M model, the relationship between mechanical stress  $\sigma$  and plastic strain  $\varepsilon_p$  can be calculated by the Voce model [13]:

$$\sigma = \sigma_{\rm s} - (\sigma_{\rm s} - \sigma_{\rm c}) \exp(-n_{\rm c} \varepsilon_{\rm p}), \tag{7}$$

where  $\sigma_c$  is the initial yield stress,  $\sigma_s$  the saturation stress, and  $n_c$  the characteristic factor. Figs. 5(e) and (f) show that the relations between  $\sigma$  and  $\varepsilon_p$  can be well captured by the Voce model. Theoretically, this  $k_2/n_c$  ratio should equal two as justified by the K-M model [13,15]. Here, the determined  $k_2/n_c$  values for HTD and HTS are 2.02 and 1.99, respectively. Therefore, the present quantitative analysis of the stain hardening behavior is validated.

#### 4.3. Fracture mechanism

The average lattice strains of the Al,  $Mg_2Si$  and Si phases in Fig. 3 indicate heterogeneous deformation at the microscale. After the yield point, the dislocation density in the Al phase increases upon the plastic deformation (Fig. 4). Since the stiff  $Mg_2Si$  and Si particles act as obstacles for dislocation motions, dislocations accumulate around the second phase particles [43,44]. Consequently, the stiff

Mg<sub>2</sub>Si and Si particles serve as void nucleation sites at large plastic deformation [45,46]. Here, the fracture surface of an ex-situ HTD specimen tested at  $1.0 \times 10^{-3}$  s<sup>-1</sup> strain rate is characterized by SEM. An overview of the cone fracture is shown in Fig. 6(a), and a zoomed view of the center part is shown in Fig. 6(b). The fracture surface of HTD is no longer along the melt pool boundary, different from those of the as-built and HTS states [10,47]. This behavior is associated with the distribution of second phase particles, which are much more homogeneous in HTD than in the as-built alloy [48]. A highmagnification view of the center part shows the equiaxial dimples clearly (Fig. 6(c)). Many dimples contain spherical particles, as indicated by the white arrows in Fig. 6(c). These results suggest that the fracture mode of HTD is a ductile fracture with the mechanism of void nucleation, growth, and coalescence. Moreover, the particles inside dimples confirm that the second phase particles serve as void nucleation sites. A high-magnification view of the marginal area of the cone fracture is shown in Fig. 6(d), where the traces of shear sliding are clear.

The K-M model analysis in Figs. 5(c) and (d) reveals that the dislocation storage rate of HTD is much lower than that of HTS, while the dislocation annihilation rate of HTD is higher than that of HTS. Accordingly, the accumulation of dislocations around the Mg<sub>2</sub>Si and



Fig. 6. Fractographs of the ex-situ HTD specimen tested at 1.0×10<sup>-3</sup> s<sup>-1</sup> strain rate: (a) an overview of the cone fracture, (b) a zoomed view of the center area, high-magnification views of the (c) center area, and (d) marginal area.

Si particles is more difficult in HTD than in HTS. Therefore, the void nucleation is slower in HTD than in HTS. This mechanism contributes to the higher elongation of HTD compared with HTS.

#### 5. Conclusions

- (1) According to the evolutions of lattice strains in the phases, no noticeable damage effects are observed in Mg<sub>2</sub>Si and Si of HTD during uniform deformation. The damaging effect is detected in the Mg<sub>2</sub>Si and Si phases of HTS, agreeing with the previous investigation [10]. The fracture surfaces of HTD and HTS indicate a ductile fracture mode.
- (2) The total dislocation density in HTD increases slowly with the applied true strains < 3.5%, and then it remains almost constant during the following uniform deformation. In contrast, the dislocation density in HTS increases rapidly with the applied strain. The initial crystallite size is larger in HTD than in HTS. For both HTD and HTS, the crystallite sizes decrease quickly in the early deformation stage, and then it decreases slowly.
- (3) The dislocation storage rate is much lower in HTD than in HTS, while the dislocation annihilation rate is higher in HTD than in HTS. As a result, the dislocation accumulation around the Mg<sub>2</sub>Si and Si particles is more difficult in HTD than in HTS, contributing to a higher ductility in HTD. The identified K-M and Voce models can be used in advanced crystal plasticity models for predicting the printed components' mechanical behavior under various loading conditions, as demonstrated in the references [49–51].

#### **Declaration of Competing Interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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