

## The Power of Oomph:

A loud story about earthquakes, tsunamis, sound, and HPC

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## **Collaborations & Funding**

#### **Technological University of Munich**

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#### Part I: Fully-coupled Earthquake-Tsunami Simulations



#### Earthquake-Tsunami Coupling





#### Earthquake-Tsunami Coupling Workflows

One-way Linked



Figure from: H. Madden et al. "Linked 3-D modelling of megathrust earthquake-tsunami events: from subduction to tsunami run up (2021)

**Fully Coupled** 









## One-way linking vs 3D coupling

Using shallow water equations for tsunami has disadvantages:

- No dispersion (if not using Boussinesq approximation)
- No acoustic waves (i.e., assuming incompressible ocean) -> Potentially dominant in data recorded by offshore instruments
- Only works in **shallow water** limit

Fully-coupled elastic-acoustic model solves entirely new class of earthquake-tsunami problem

Compares well with one-way linking under certain conditions

Detailed model comparison: Abrahams, Lauren S., et al. "Comparison of methods for coupled earthquake and tsunami modelling." *Geophysical Journal International* 234.1 (2023)



#### Example: Palu, Sulawesi September 2018

- Mw 7.5 strike-slip earthquake
  Propagation at supershear speed crossing narrow Palu Bay
- Followed by unexpected and localized tsunami
- Complicated geometry: bath-tub like bay, very shallow water (average 600 m)
- Details: L. Krenz et al. "3D Acoustic-Elastic Coupling with Gravity: The Dynamics of the 2018 Palu, Sulawesi Earthquake and Tsunami". Proceedings of the International Conference for High Performance Computing, Networking, Storage and Analysis, 2021





#### SeisSol

#### What

- (An)Isotropic elastic wave propagation
- Acoustic wave propagation
- Viscoelastic wave propagation
- Poroelasticity
- Off-fault plasticity
- Dynamic earthquake rupture How
- Numerics: ADER-DG
- Unstructured tetrahedral meshes with local time-stepping
- Optimized Hybrid MPI + OpenMP Parallelization

Available (open-source) at https://github.com/SeisSol/SeisSol/





#### **Two-Way Elastic-Acoustic Coupling**



Based on 2D model of (Lotto and Dunham, 2015) Here: First 3D implementation! With:

- $\eta(x, y, t)$  sea surface height
- Ocean at rest at z = 0

Figures in 2D for illustration, all simulations are 3D



#### **Ocean Model**



Linear acoustic medium, q = (u, v, w, p) Treated as special case of elastic wave equation with stress tensor  $\sigma_{ij} = -p \ \delta_{ij}$ , density  $\rho$  and  $g = 9.81 \frac{m}{s^2}$ .

Free surface

 $p(x, y, \eta) = 0$ 

Typically solved by moving mesh. Following (Lotto, Dunham 2015),linearized to:  $p(x, y, z = 0) = \rho g \eta(x, y)$  $\frac{\partial \eta}{\partial t} = v_z$ 



#### The ADER-DG Approach

Solve linear hyperbolic equations of the form

 $\frac{\partial q}{\partial t} + A \frac{\partial q}{\partial x} + \mathbf{B} \frac{\partial q}{\partial y} + \mathbf{C} \frac{\partial q}{\partial z} = 0$ 

with q vector of variables, x = (x, y, z) position, t time, A(x), B(x), C(x) flux matrices.

**Discontinuous Galerkin** (DG) divides domain into disjoint elements, approximates solutions by piecewise-polynomials.

Elements are connected by solving the Riemann problem exactly.

**ADER**-Approach uses element-local Taylor expansion for time integration instead of Runge-Kutta procedures.

Advantages: One-step scheme, arbitrary order in time and space



## Modeling Goals & Resulting Challenges

Goals

• Capture **entire process**: earthquake rupture, generation and propagation of seismic waves, ocean acoustic waves and tsunamis

- High resolution in 3D Earth (10 Hz) and ocean (15 Hz)
- Complex geometry, including bathymetry/topography
- 3D solid-fluid coupling

Challenges

- Resolution leads to large setups: ≈ 250 billion degrees of freedom
- Vastly different element sizes =⇒ vastly different time step size
- · Geometry requires unstructured meshes



#### Palu: Our setup

- Added **water layer** to existing earthquake model (Ulrich et al., 2019).
- **Fully coupled** model (including plasticity,seismic and acoustic waves, dynamic,earthquake rupture)
- Two meshes: M (89 million elements), L (518 million elements)
- Poly. Order 5, 46 and 261 billion degrees of freedom
- M: 5.3 hours on **1000 nodes** of SuperMUC-NG for 100s simulated time
- L: 5.5 hours on 3072 nodes of SuperMUC-NG for 30s simulated time





#### Palu: 3D View at 15s





#### Comparison with One-Way Linking

Left: One-way linking, right: fully-coupled

Shows: Sea surface displacement for t = 1s, ..., 100s

Use identical earthquake model

Matches well overall, with some differences (e.g. at coast, "smoother" tsunami)





#### Part II: Fully-coupled Earthquake-Sound Simulations

#### "Big blast followed by a long 10-second echo." Helsinki, 2018-07-08 20:37

## Enhanced Geothermal System in Helsinki

- Otaniemi project
- Enhanced geothermal system (EGS), stimulated in June and July 2018 in the region of Helsinki
- Thousands of induced, small earthquakes
- Observations of ground shaking and audible disturbances collected by Macroseismic questionnaire of the Institute of Seismology, University of Helsinki
- More details:

Lukas Krenz, Sebastian Wolf, Gregor Hillers, Alice-Agnes Gabriel, Michael Bader; Numerical Simulations of Seismoacoustic Nuisance Patterns from an Induced M 1.8 Earthquake in the Helsinki, Southern Finland, Metropolitan Area. Bulletin of the Seismological Society of America 2023;; 113 (4): 1596–1615. doi: https://doi.org/10.1785/0120220225



# Enhanced Geothermal Systems (EGS)

- 1: Reservoir
- 2: Pump house
- 3: Heat exchanger
- 4: Turbine hall
- 5: Production well
- 6: Injection well
- 7: Hot water to district heating
- 8: Porous rock
- 9: Well
- 10: Solid bedrock

Image from:

Geothermie\_Prinzip.svg: \*Geothermie\_Prinzip01.jpg: "Siemens Pressebild" http://www.siemens.comderivative work: FischX (talk)Geothermie\_Prinzip01.jpg: "Siemens Pressebild" http://www.siemens.comderivative work: Ytrottier, CC BY-SA 3.0





#### Traffic Light System

## **Red**: Stop; $M_L \ge 2.1$ Amber: Be Careful; PGV $\ge 1$ mm/s detected and $M_L \ge 1.0$ ; $M_L \ge 1.2$ Green: Everything's fine

SCIENCE ADVANCES | RESEARCH ARTICLE

#### EARTH SCIENCES

Controlling fluid-induced seismicity during a 6.1-km-deep geothermal stimulation in Finland

Grzegorz Kwiatek<sup>1,2</sup>\*, Tero Saarno<sup>3</sup>, Thomas Ader<sup>4</sup>, Felix Bluemle<sup>1</sup>, Marco Bohnhoff<sup>1,2</sup>, Michael Chendorain<sup>4</sup>, Georg Dresen<sup>1,5</sup>, Pekka Heikkinen<sup>3,6</sup>, Ilmo Kukkonen<sup>6</sup>, Peter Leary<sup>7</sup>, Maria Leonhardt<sup>1</sup>, Peter Malin<sup>1,7</sup>, Patricia Martínez-Garzón<sup>1</sup>, Kevin Passmore<sup>7</sup>, Paul Passmore<sup>7</sup>, Sergio Valenzuela<sup>7</sup>, Christopher Wollin<sup>1</sup>

Design and implementation of a traffic light system for deep geothermal well stimulation in Finland

Thomas Ader • Michael Chendorain • Matthew Free • Tero Saarno • Pekka Heikkinen • Peter Eric Malin • Peter Leary • Grzegorz Kwiatek • Georg Dresen • Felix Bluemle • Tommi Vuorinen



#### Induced Earthquakes & Reports







#### Comparisons with elastic measurements





#### Comparison with sound recordings





#### **Approximating Sound Pressure**

Fully-coupled simulations are **very** expensive

⇒ Use two setups: a fully refined Earth-only model & a fully-coupled model with refinement region

Common approximation for pressure perturbation  $\Delta p$  from vertical velocity v

 $\Delta \mathbf{P} = \rho c \boldsymbol{v}$ 

Workflow:

- 1. Compute acoustic receivers (0.5m above topography) and elastic (directly below)
- 2. For each pair, compute peak sound pressure level (SPL) and peak vertical velocity
- 3. Compute linear regression

$$\Delta P^{\text{peak}} = c_0 + c_1 v^{\text{peak}} + \epsilon$$



#### Predicting Sound Pressure Level from Vertical Velocity





#### PGV and SPL maps SPL Horizontal SPL SPL P Wave PGV S Wave Epicentral Northings [km] 0 Ô 0 0 -4 0 4 Λ **Epicentral Epicentral Epicentral Epicentral** Eastings [km] Eastings [km] Eastings [km] Eastings [km] 0.0 0.05 0.1 0.02 0.045 0.0 0.01 0.02 0.0 0.02 0.045 0.0 peak horizontal peak SPL [Pa] P-wave S-wave peak SPL [Pa] peak SPL [Pa] velocity [mm/s]

PGV: Horizontal Peak Ground Velocity

SPL: Sound pressure level, reconstructed from peak vertical velocity



#### Part III: Local Time Stepping



## Timestep restrictions of ADER-DG

 $\Delta t < \frac{1}{2N+1} \frac{l_{min}}{a_{max}}$ 

With:

N order

 $l_{min}$  diameter of the insphere of tetrahedron  $a_{max}$  largest signal speed inside tetrahedron

Huge variances in both values



## **Clustered Local Time Stepping**

Idea:

Group elements into clusters with time step sizes

 $[\lambda \Delta t^{min}, \lambda 2 \Delta t^{min}], [\lambda 2 \Delta t^{min}, \lambda 4 \Delta t^{min}], \dots$ 

All elements from one cluster are updated at the same time

"Wiggle Factor"  $\lambda$  can be optimized for better clustering

Breuer, Alexander, and Alexander Heinecke. "Next-Generation Local Time Stepping for the ADER-DG Finite Element Method." 2022 IEEE International Parallel and Distributed Processing Symposium (IPDPS). IEEE, 2022.



#### A Clustering Straight from HEL



## ПП





#### Old implementation

Algorithm 2 Generation of work items 1: procedure generateLocal( $C_{l,p}$ ,  $t^{\text{sync}}$ ,  $t^{\text{dofs}}_{l-1,p}$ ,  $t^{\text{pred}}_{l+1,p}$ ,  $t^{\text{dofs}}_{l+1,p}$ )  $e \leftarrow (C_{l,p} \notin \mathcal{L}_p^{int}) \land (C_{l,p} \notin \mathcal{L}_p^{cop})$  $\begin{array}{l} e \leftarrow (\ C_{l,p}.t^{\mathrm{dofs}} < t^{\mathrm{sync}}) \land e \\ e \leftarrow (\ C_{l,p}.t^{\mathrm{pred}} \leq t_{l-1,p}^{\mathrm{dofs}}) \land e \end{array}$ 3:  $e \leftarrow (C_{l,p}t^{\text{pred}} = C_{l,p}t^{\text{dofs}}) \land e$ 53  $e \leftarrow ((C_{l,p}, t^{\text{pred}} < t^{\text{pred}}_{l+1,p}) \lor (C_{l,p}, t^{\text{pred}} \le t^{\text{dofs}}_{l+1,p})) \land e$ if *e* then  $\triangleright$  Add local items if all conditions are met. 7:  $\mathcal{L}_p^{\text{int}} \leftarrow C_{l,p} \cup \mathcal{L}_p^{\text{int}}$ 8:  $\mathcal{L}_{p}^{cop} \leftarrow C_{l,p} \cup \mathcal{L}_{p}^{cop}$ 93 end if 10: 11: end procedure 12: 13: procedure generateNeighboring( $C_{l,p}$ ,  $t^{\text{sync}}$ ,  $t^{\text{pred}}_{l-1,p}$ ,  $t^{\text{pred}}_{l+1,p}$ )  $e \leftarrow (C_{l,p} \notin N_p^{int}) \land (C_{l,p} \notin N_p^{cop})$ 14:  $e \leftarrow (C_{l,v}.t^{dofs} < t^{sync}) \land e$ 15:  $e \leftarrow (C_{l,p}, t^{\text{pred}} \leq t_{l-1,p}^{\text{pred}}) \land e$ 16:  $e \leftarrow (C_{l,n}, t^{\text{pred}} > C_{l,n}, t^{\text{dofs}}) \land e$ 17:  $e \leftarrow (C_{l,p}.t^{\text{pred}} \leq t_{l+1,p}^{\text{pred}}) \land e$ 18: if e then > Add neighboring items if all conditions are met. 19:  $\begin{array}{l} \mathcal{N}_p^{\mathrm{int}} \leftarrow C_{l,p} \cup \mathcal{N}_p^{\mathrm{int}} \\ \mathcal{N}_p^{\mathrm{cop}} \leftarrow C_{l,p} \cup \mathcal{N}_p^{\mathrm{cop}} \end{array}$ 20: 21: end if 22: 23: end procedure

25: procedure generateWorkItems(C<sub>I,p</sub>, t<sup>sync</sup>)  $t_{l-1,p}^{\text{pred}} \leftarrow t_{l-1,p}^{\text{dofs}} \leftarrow \text{limits::max()}$ 26:  $t_{l+1,p}^{\text{pred}} \leftarrow t_{l+1,p}^{\text{dofs}} \leftarrow \text{limits::max()}$ 27: 28: if  $\exists C_{l-1}$ , p then  $\triangleright$  Get times of previous cluster if existent 29:  $t_{l-1,p}^{\text{pred}} \leftarrow C_{l-1,p}.t^{\text{pred}}$ 30:  $t_{l-1,p}^{\text{dofs}} \leftarrow C_{l-1,p}.t^{\text{dofs}}$ 31: end if 32: if  $\exists C_{l+1}, p$  then Get times of next cluster if existent 33:  $t_{l+1,p}^{\text{pred}} \leftarrow C_{l+1,p}.t^{\text{pred}}$ 34:  $t_{l+1,p}^{\text{dofs}} \leftarrow C_{l+1,p}.t^{\text{dofs}}$ 35: end if 36: 37: generateLocal( $C_{l,p}$ ,  $t^{sync}$ ,  $t^{dofs}_{l-1,p}$ ,  $t^{pred}_{l+1,p}$ ,  $t^{dofs}_{l+1,p}$ ) 38: generateNeighboring( $C_{l,p}$ ,  $t^{sync}$ ,  $t^{pred}_{l-1,p}$ ,  $t^{pred}_{l+1,p}$ ) 39: 40: end procedure

Image taken from:

Breuer, Alexander. "High Performance Earthquake Simulations." (2015).



**Cluster connectivity** 

State machine for one time cluster



## Clustering Palu (M)





#### Strong Scaling on Frontera (Palu L)



### Strong Scaling on Frontera (Palu L): Time-to-solution



#### Conclusion

- Fully coupled elastic-acoustic simulations capture more effects than typical one-way linking strategies
- Linearization of free surface boundary conditions efficient way of tracking sea surface height
- Pronounced differences in Palu scenario: "smoother" tsunami
- Differences will be important when connecting to tsunami observations
- Further application: Modeling **sound** generated by **induced earthquakes** (due to geothermal energy)
- Local Time-Stepping useful for elastic-acoustic coupling
- New **state-machine** based model elegant & contains fewer (or different?) bugs
- Outlook: Fully-coupled models for Mediterranean tsunami (Hellenic arc); Húsavík-Flatey Fault Zone, North Iceland