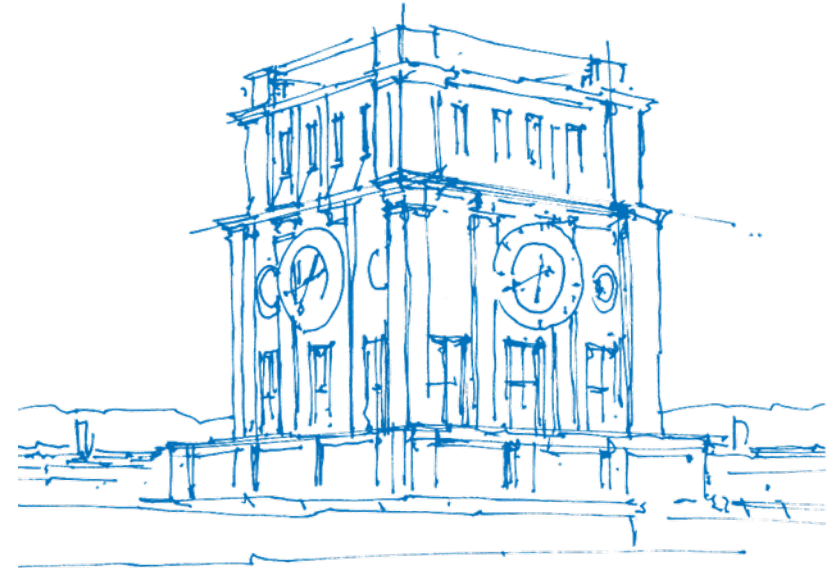


Design and evaluation of a waveform iteration–based approach for coupling heterogeneous time stepping methods via preCICE

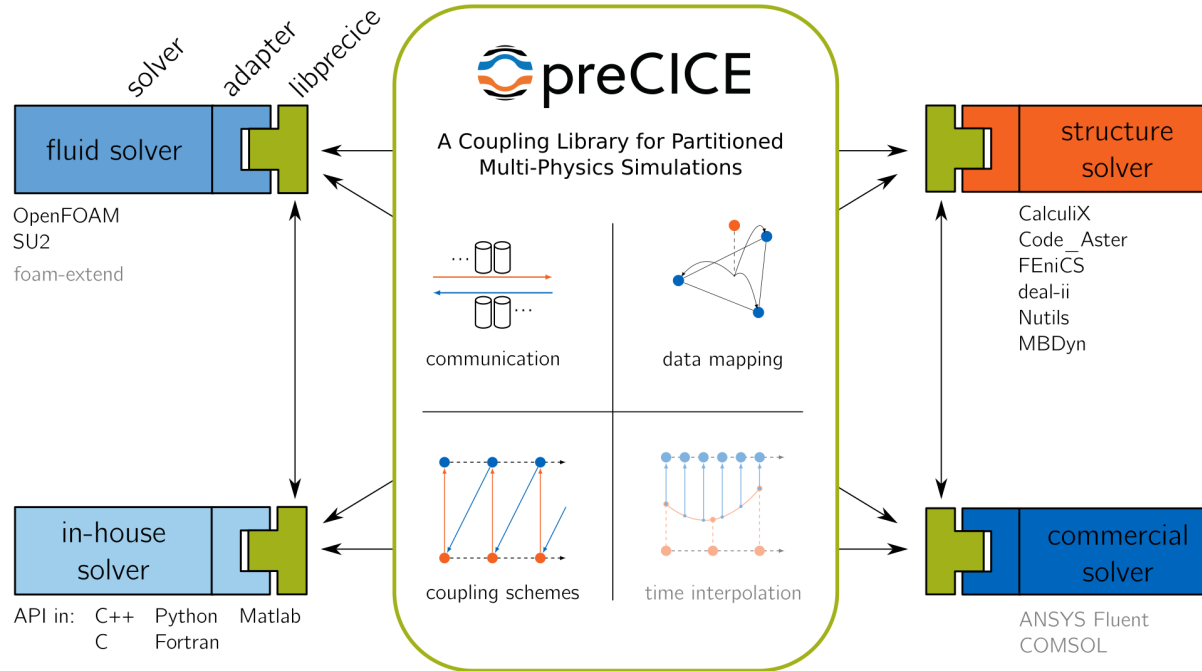
Benjamin Rodenberg¹, Ishaan Desai², Benjamin Uekermann²

¹Technical University of Munich, Department of Informatics

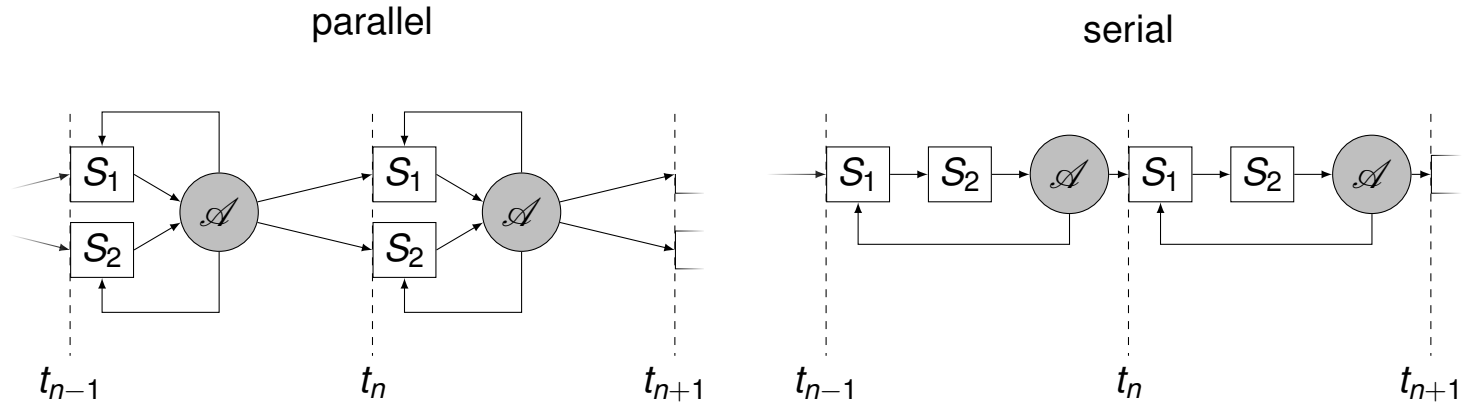
²University of Stuttgart, Usability and Sustainability of Simulation Software
WCCM-XV & APCOM-VIII



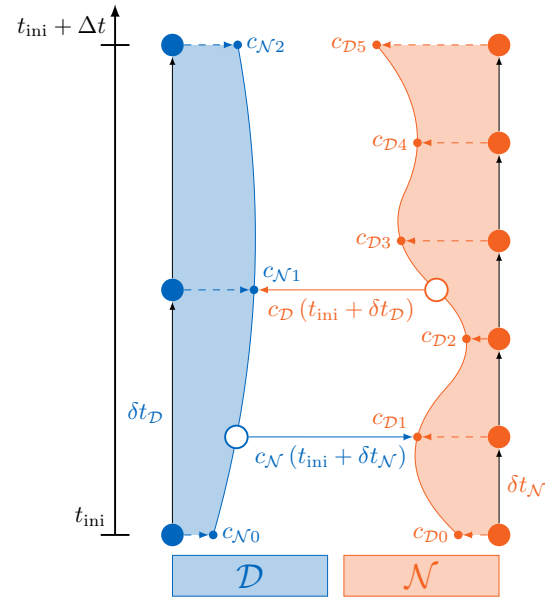
TUM Uhrenturm



Implicit coupling schemes



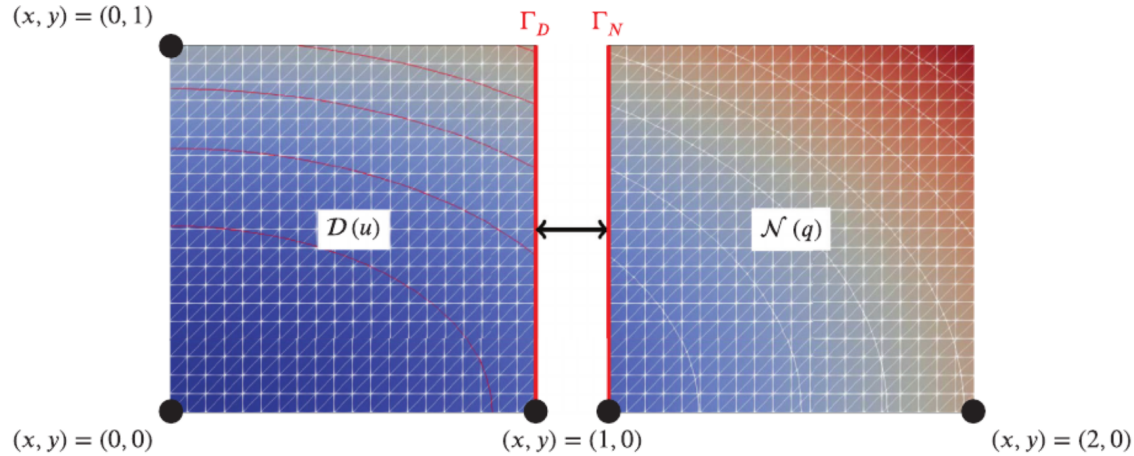
Idea: Use waveforms



For details: See QNWI paper¹

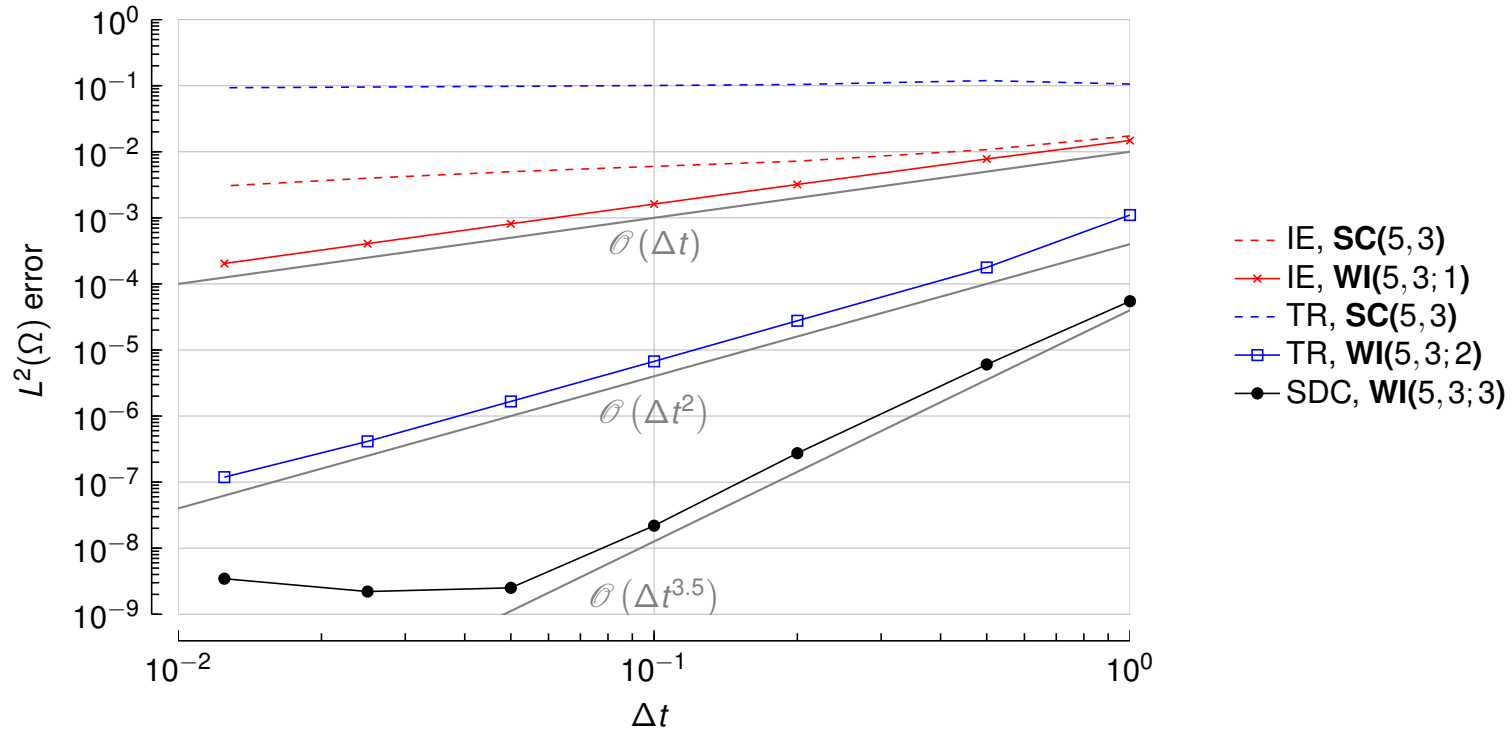
¹Quasi-Newton waveform iteration for partitioned surface-coupled multiphysics applications. *Int J Numer Methods Eng.* 2021. <https://doi.org/10.1002/nme.6443>

QNWI paper: What can we expect?

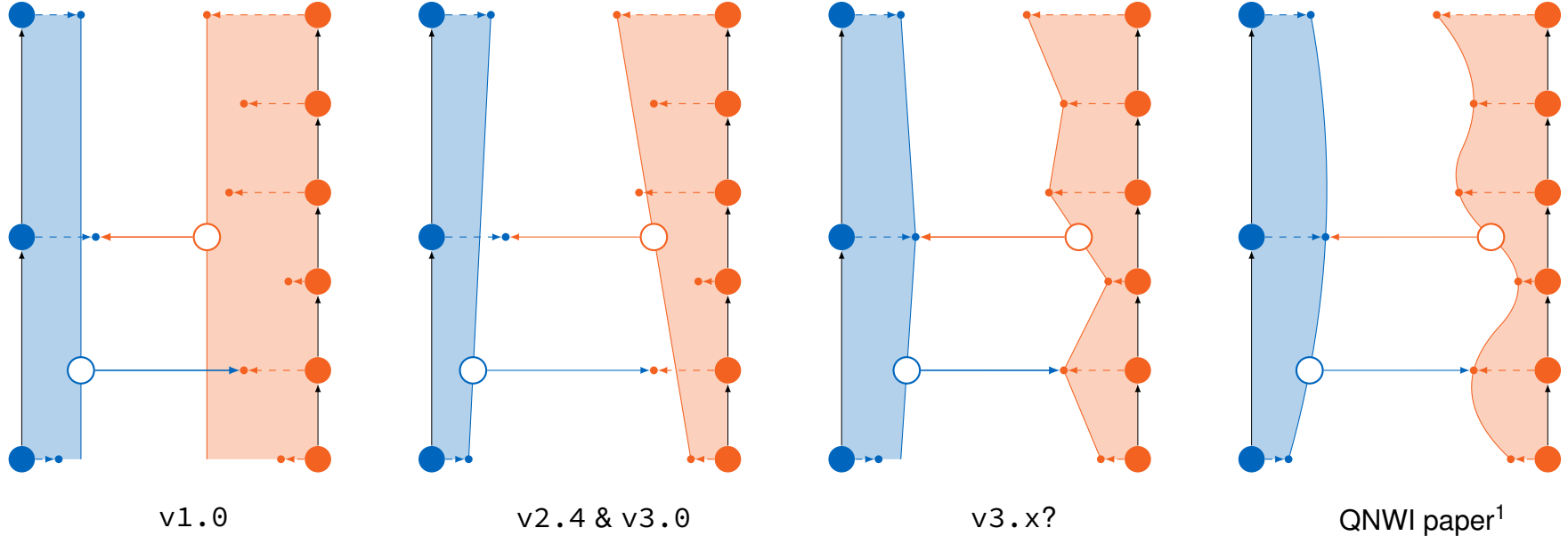


- Manufactured solution allows us to quickly check for errors: $u(x, y, t) = 1 + g(t)x^2 + 3y^2 + 1.2t$
- linear FEM are exact in space. Only error in time, if any.
- $g(t)$ is used to check
 - for high order: $g(t) = (1 + t)^\alpha$
 - for convergence (time & quasi-Newton): $g(t) = \sin(t)$

QNWl paper: What can we expect?



Bringing waveforms to preCICE



¹Quasi-Newton waveform iteration for partitioned surface-coupled multiphysics applications. *Int J Numer Methods Eng.* 2021.

<https://doi.org/10.1002/nme.6443>

Bringing waveforms to preCICE

Define interpolation order:

```
<participant name="SolverOne">  
  ...  
  <write-data name="Force" mesh="MeshOne" />  
  <read-data name="Velocities" mesh="MeshOne" waveform-order="1" />  
</participant>
```

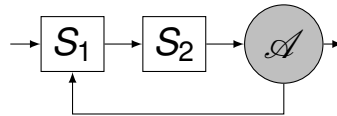
Sample from interpolant:

```
// old API  
precice.readScalarData(readDataID, vertexID, readData);  
  
// new API has optional argument  
precice.readScalarData(readDataID, vertexID, sampleDt, readData);
```

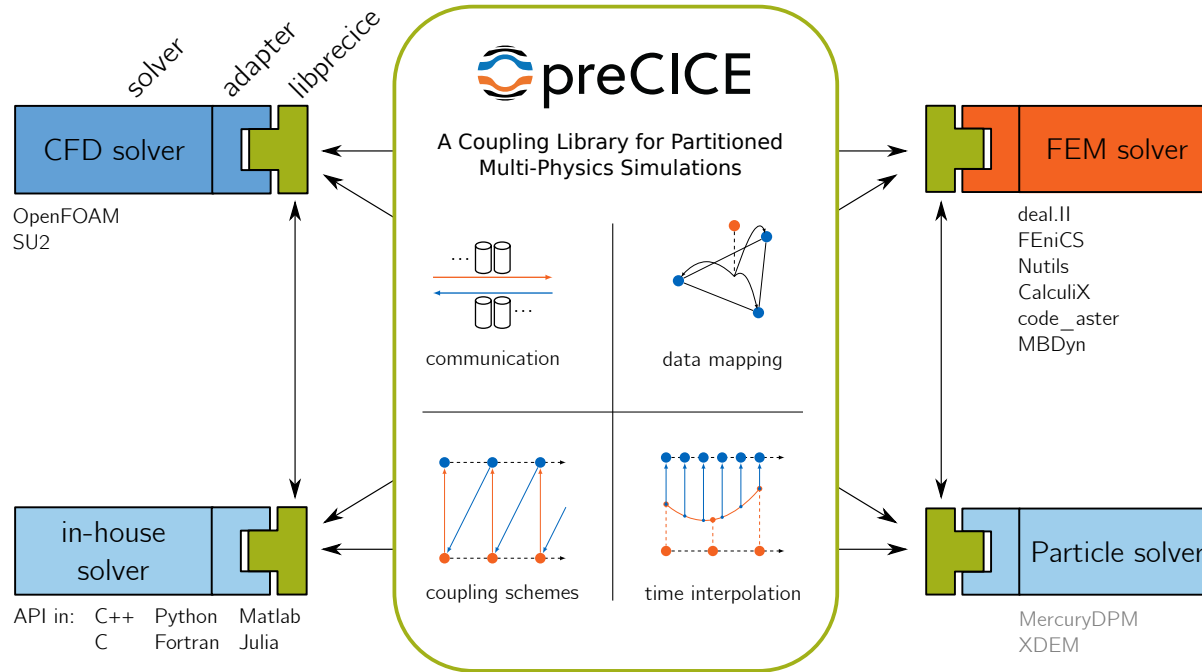

Bringing waveforms to preCICE

```
<coupling-scheme:serial-implicit>  
  <participants first="SolverOne" second="SolverTwo" />  
  <max-time-windows value="10" />  
  <time-window-size value="1.0" />  
  ...  
  <exchange data="Forces" from="SolverOne" to="SolverTwo" initialize="true"/>  
  <exchange data="Velocities" from="SolverTwo" to="SolverOne" initialize="true"/>  
</coupling-scheme:serial-implicit>
```

Data initialization for data sent from first to second participant in serial coupling is now possible.



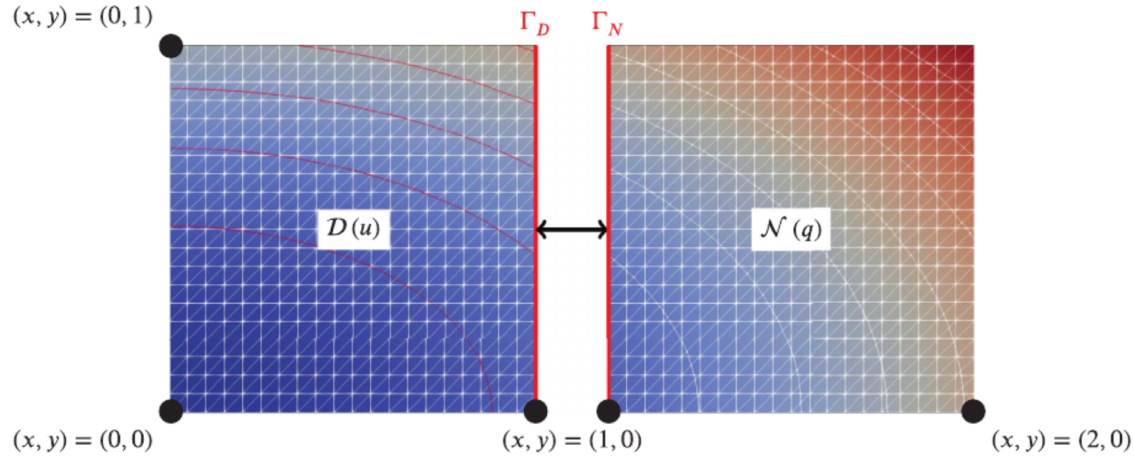
Remaining components: bindings, adapter, tutorials



Remaining components: bindings, adapter, tutorials

- python bindings (<https://github.com/precice/python-bindings/pull/147>)
- FEniCS adapter (<https://github.com/precice/fenics-adapter/pull/153>)
- update tutorial (<https://github.com/precice/tutorials/pull/281>)
- All these updates were just a few hours of work.
- Conjugate heat transfer with multirate works as expected!

Evaluation: Conjugate heat transfer



- Manufactured solution allows us to quickly check for errors: $u(x, y, t) = 1 + g(t)x^2 + 3y^2 + 1.2t$
- linear FEM are exact in space. Only error in time, if any.
- $g(t)$ is used to check
 - for high order: $g(t) = (1 + t)^\alpha$
 - for convergence (time & quasi-Newton): $g(t) = \sin(t)$

tutorials/partitioned-heat-conduction

```
partitioned-heat-conduction/precice-config.xml
```

7	enabled="true" />	7	enabled="true" />
8	</log>	8	</log>
9		9	
10	- <solver-interface dimensions="2">	10	+ <solver-interface dimensions="2" experimental="true">
11	<data:scalar name="Temperature" />	11	<data:scalar name="Temperature" />
12	<data:scalar name="Heat-Flux" />	12	<data:scalar name="Heat-Flux" />
13		13	
25	<use-mesh name="Dirichlet-Mesh" provide="yes" />	25	<use-mesh name="Dirichlet-Mesh" provide="yes" />
26	<use-mesh name="Neumann-Mesh" from="Neumann" />	26	<use-mesh name="Neumann-Mesh" from="Neumann" />
27	<write-data name="Heat-Flux" mesh="Dirichlet-Mesh" />	27	<write-data name="Heat-Flux" mesh="Dirichlet-Mesh" />
28	- <read-data name="Temperature" mesh="Dirichlet-Mesh" />	28	+ <read-data name="Temperature" mesh="Dirichlet-Mesh" waveform-order="1"/>
29	<mapping:rbf-thin-plate-splines	29	<mapping:rbf-thin-plate-splines
30	direction="read"	30	direction="read"
31	from="Neumann-Mesh"	31	from="Neumann-Mesh"
38	<use-mesh name="Neumann-Mesh" provide="yes" />	38	<use-mesh name="Neumann-Mesh" provide="yes" />
39	<use-mesh name="Dirichlet-Mesh" from="Dirichlet" />	39	<use-mesh name="Dirichlet-Mesh" from="Dirichlet" />
40	<write-data name="Temperature" mesh="Neumann-Mesh" />	40	<write-data name="Temperature" mesh="Neumann-Mesh" />
41	- <read-data name="Heat-Flux" mesh="Neumann-Mesh" />	41	+ <read-data name="Heat-Flux" mesh="Neumann-Mesh" waveform-order="0"/>
42	<mapping:rbf-thin-plate-splines	42	<mapping:rbf-thin-plate-splines
43	direction="read"	43	direction="read"
44	from="Dirichlet-Mesh"	44	from="Dirichlet-Mesh"

tutorials/partitioned-heat-conduction



```
partitioned-heat-conduction/fenics/heat.py
```

62	62
63	63
64	64
65 - fenics_dt = .0 # time step size	65 + fenics_dt = .001 # time step size
66 # Error is bounded by coupling accuracy. In theory we would obtain the analytical solution.	66 # Error is bounded by coupling accuracy. In theory we would obtain the analytical solution.
67 error_tol = args.error_tol	67 error_tol = args.error_tol
68	68
@@ -178,7 +178,7 @@ def determine_gradient(V_g, u, flux):	
178 if precice.is_action_required(precice.action_write_iteration_checkpoint()):	178 if precice.is_action_required(precice.action_write_iteration_checkpoint()):
179 precice.store_checkpoint(u_n, t, n)	179 precice.store_checkpoint(u_n, t, n)
180	180
181 - read_data = precice.read_data()	181 + read_data = precice.read_data(dt(0))
182	182
183 # Update the coupling expression with the new read data	183 # Update the coupling expression with the new read data
184 precice.update_coupling_expression(coupling_expression, read_data)	184 precice.update_coupling_expression(coupling_expression, read_data)

Are we there?

Parallel implicit

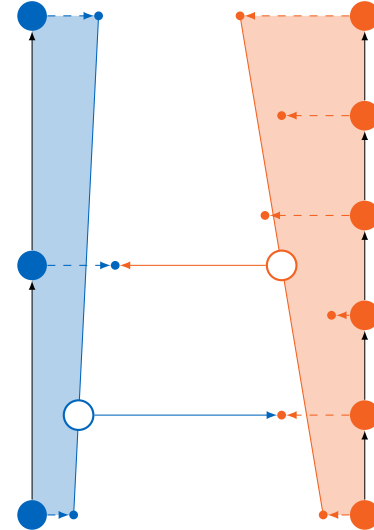
Released in preCICE v2.4.0 (<https://github.com/precice/precice/releases/tag/v2.4.0>)

Serial implicit

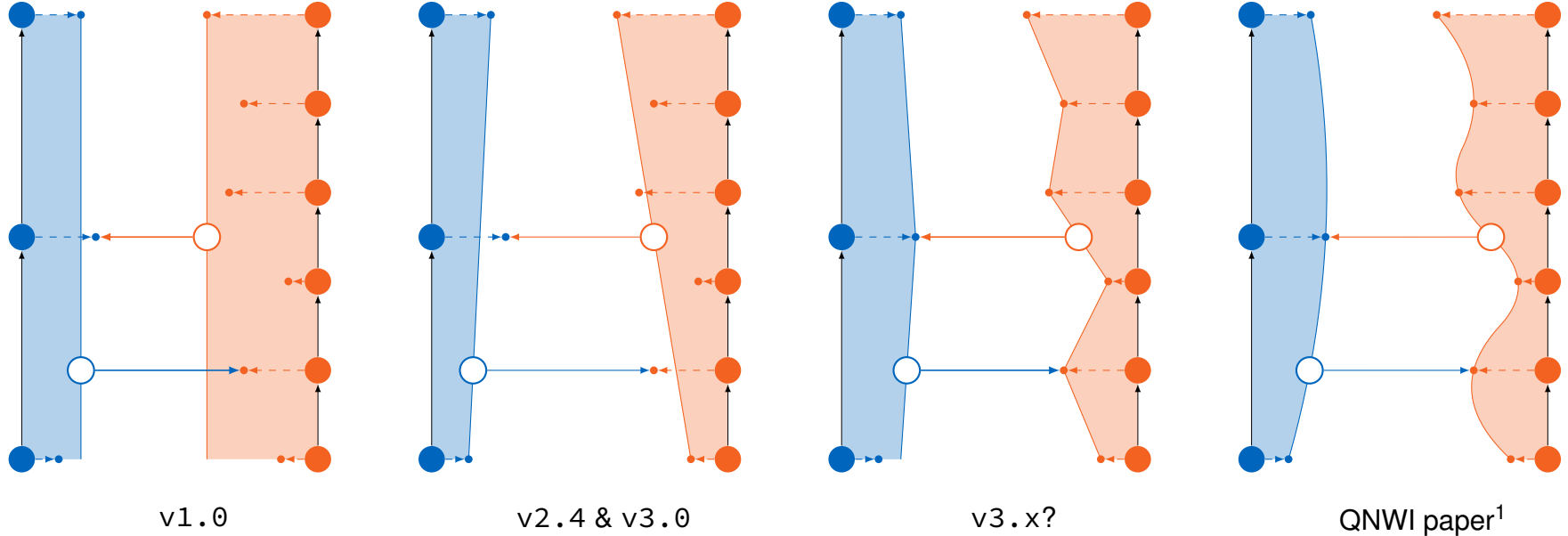
Ready for preCICE v3.0.0

Restrictions

First order, no real multirate support.



Outlook: Multirate, Higher order, Quasi-Newton



¹Quasi-Newton waveform iteration for partitioned surface-coupled multiphysics applications. *Int J Numer Methods Eng.* 2021.

<https://doi.org/10.1002/nme.6443>