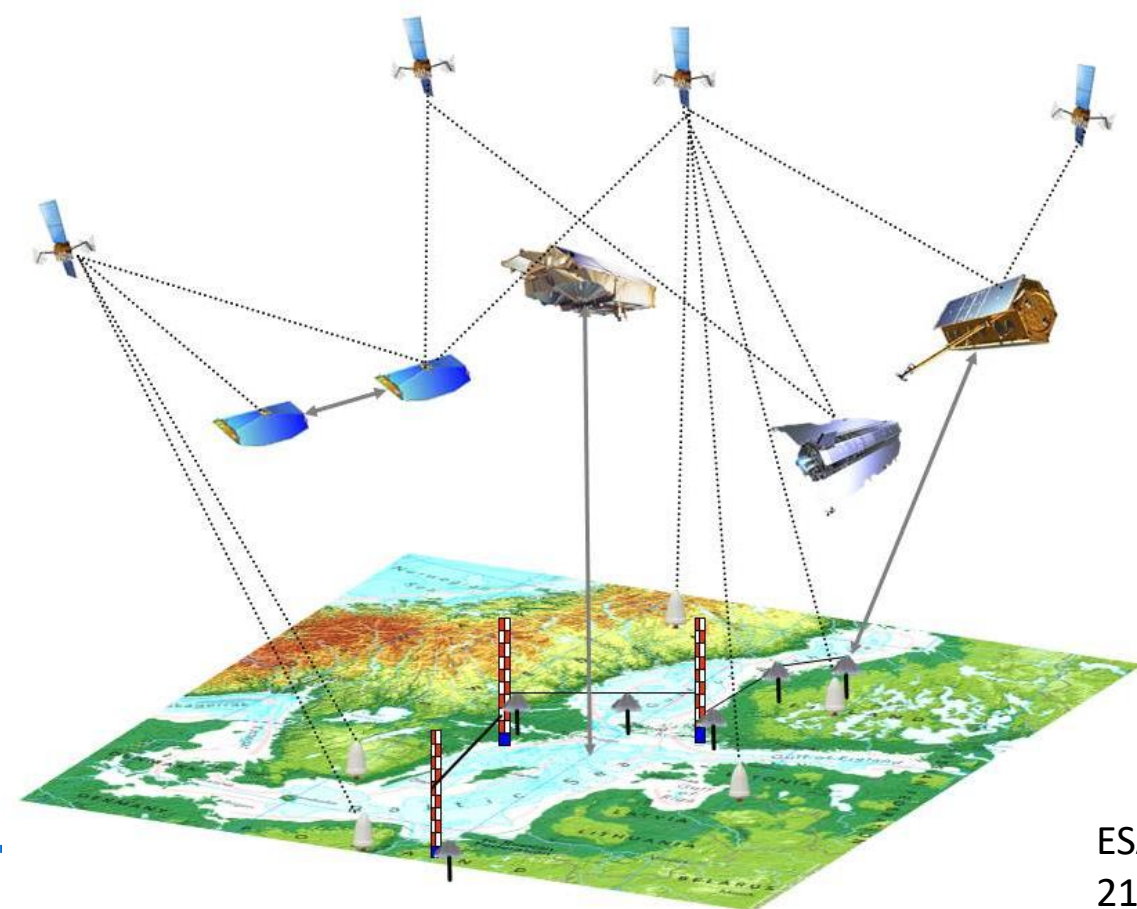


# BALTIC+

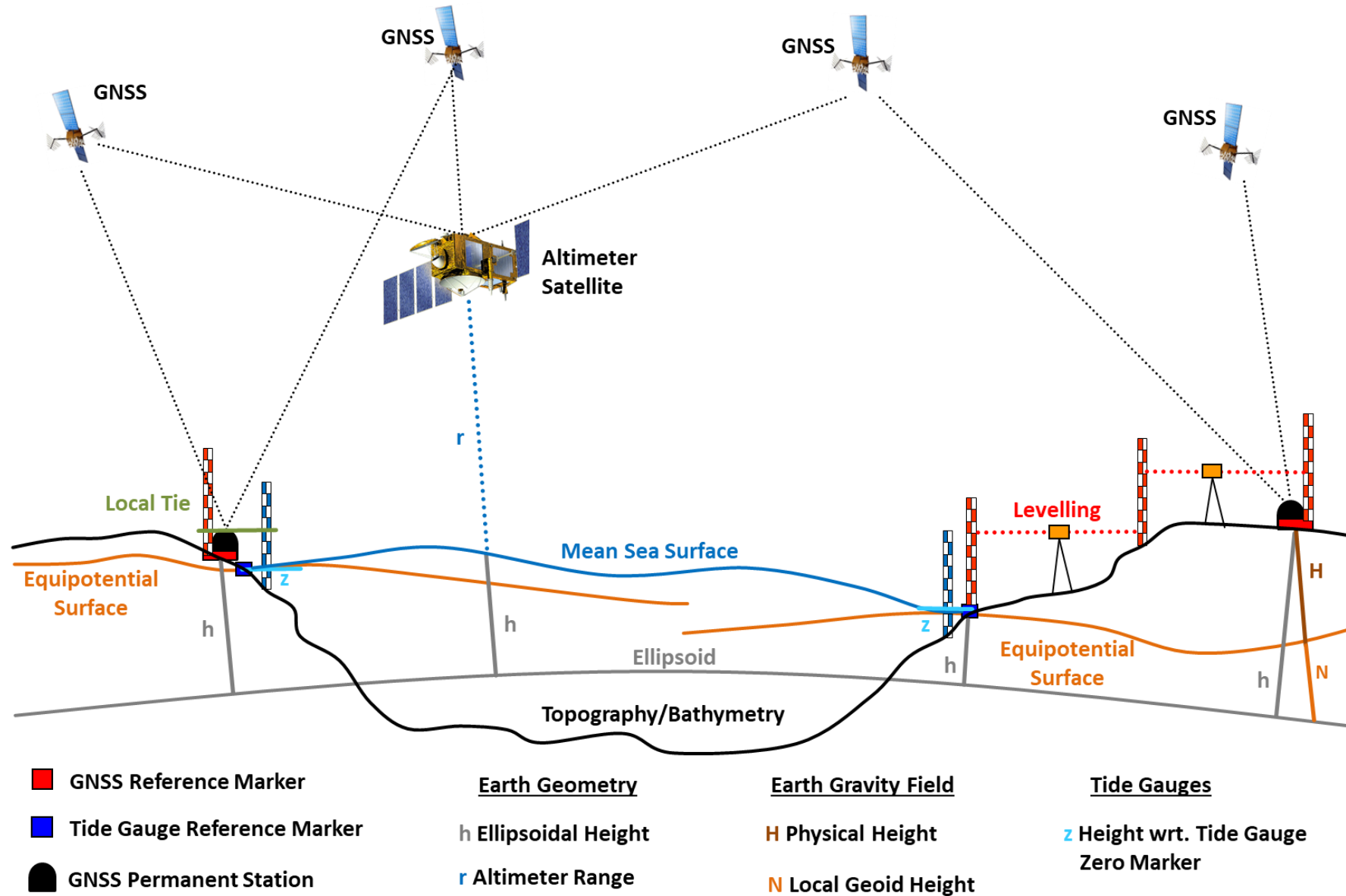
## Geodetic SAR for Baltic Height System Unification and Baltic Sea Level Research

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- (3) Technical University of Munich, German Geodetic Research Institute
- (4) Tallinn University of Technology, School of Engineering
- (5) German Aerospace Center, Remote Sensing Technology Institute
- (6) Space Research Centre, Polish Academy of Sciences
- (7) Finnish Geospatial Research Institute

# Overview Height System & Sea Level



# Scientific Challenges & Objectives

## Vertical Land Movement (Geometry)

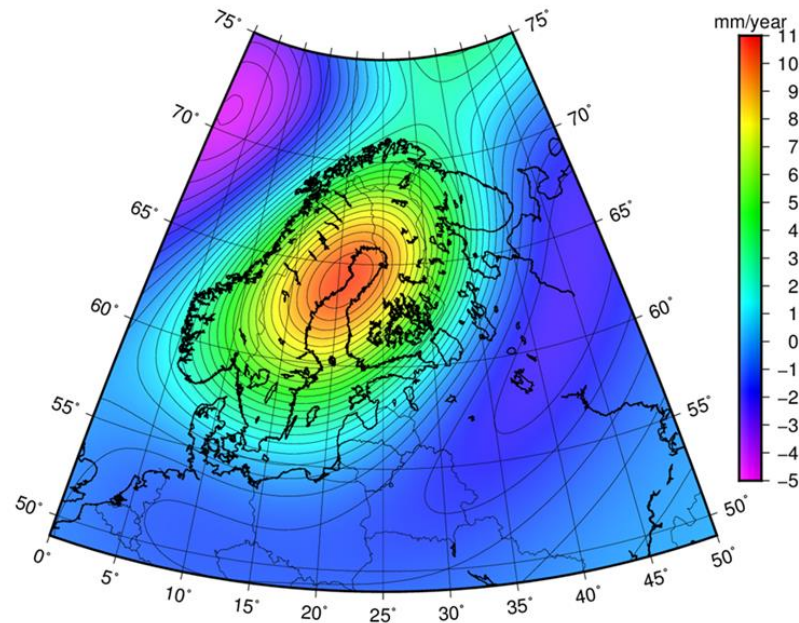
- Post-glacial rebound
- Subsidence
- any other cause ....

## Tide Gauge Vertical Movement

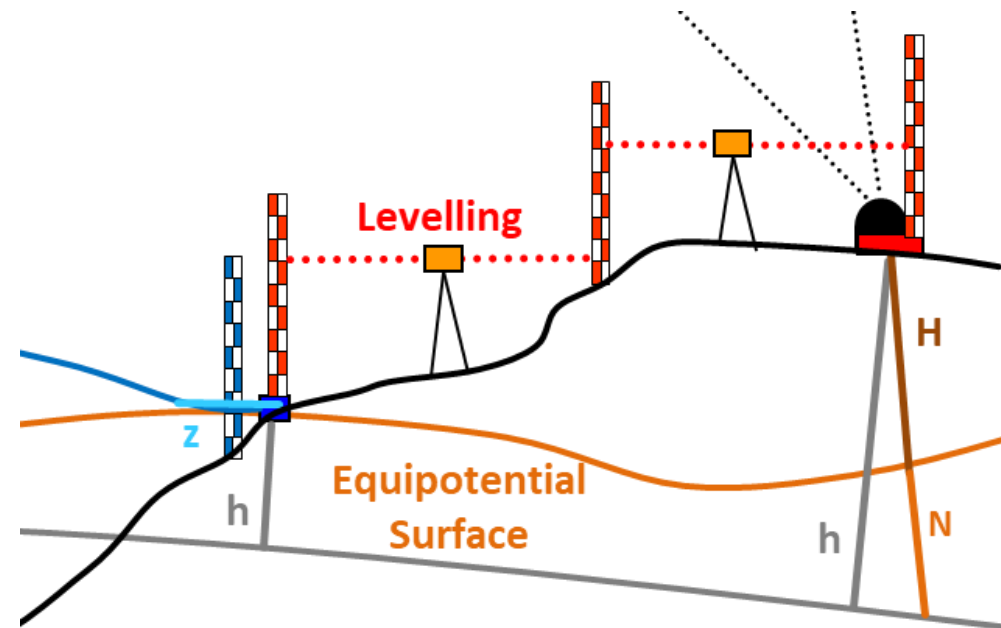
- Only relative sea level observations
- Permanent monitoring needed

## Objective 1

Connect tide gauge markers with GNSS network geometrically to determine vertical motion and to correct tide gauge readings.



Gridded vertical displacement rate  
(Steffen & Ågren, pers. comm.)



# Scientific Challenges & Objectives

## Height Systems (Gravimetry)

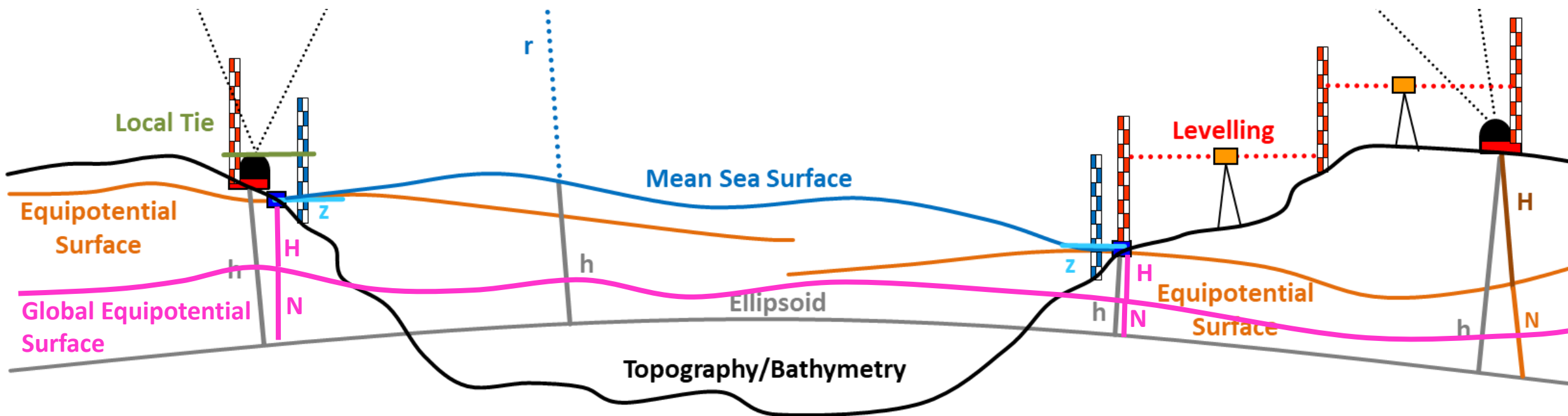
- Different height systems in countries
- Mass Redistribution

## Height System Unification

- Unique height reference surface for all countries
- Local geoid modelling per tide gauge station

## Objective 2

Geoid heights at tide gauges to compute absolute physical heights with respect to a global reference equipotential surface.



# Scientific Challenges & Objectives

## Geometry

- Geometric height tide gauge zero marker per epoch
- Tide gauge readings relative to zero marker per epoch

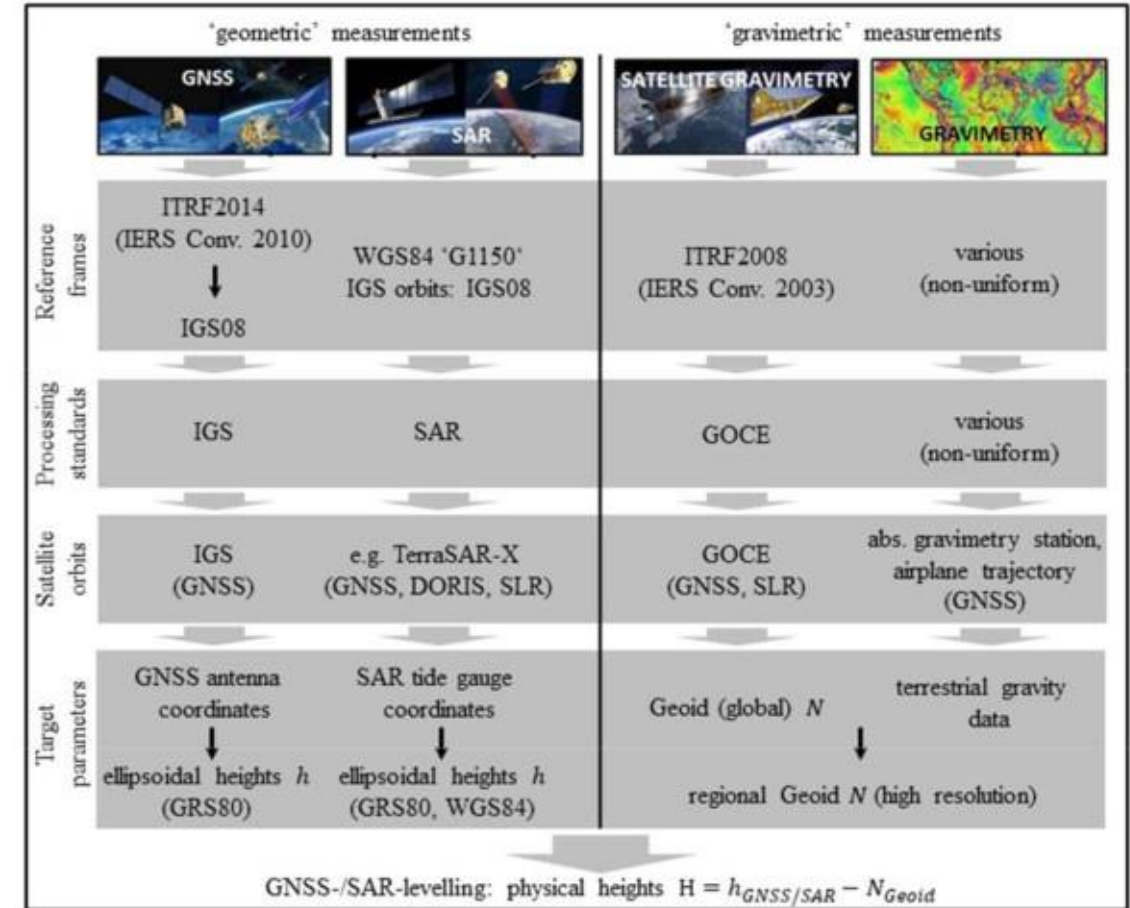
## Gravimetry

- Tide gauge geoid height wrt. a global equipotential surface per epoch
- Physical height per epoch

## Objective 3

Combination of geometric and physical heights in a common reference frame to determine absolute sea level heights.

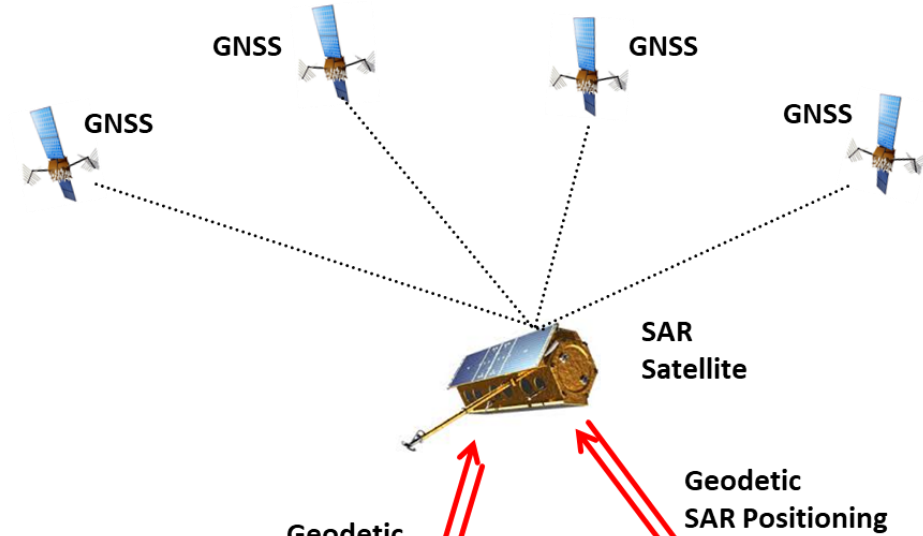
$$S^{TG}(t) = h^{TG}(t) - N^{TG}(t) + z^{TG}(t) = H^{TG}(t) - N^{TG}(t)$$



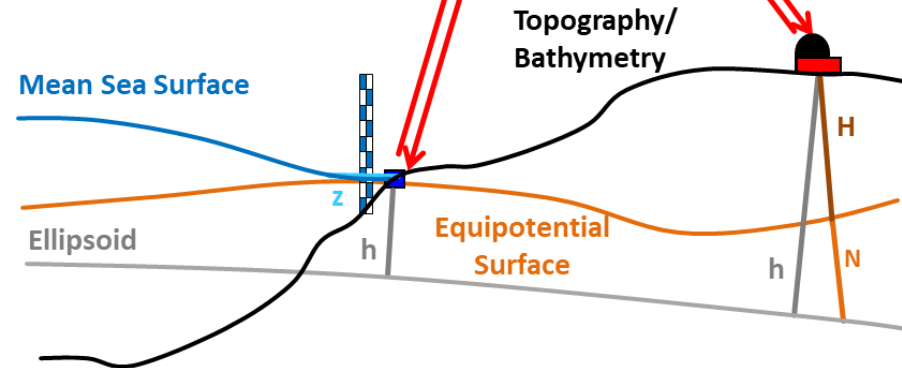


# Geodetic SAR for Ellipsoidal Height Determination

## Passive SAR Targets (Corner Reflectors)



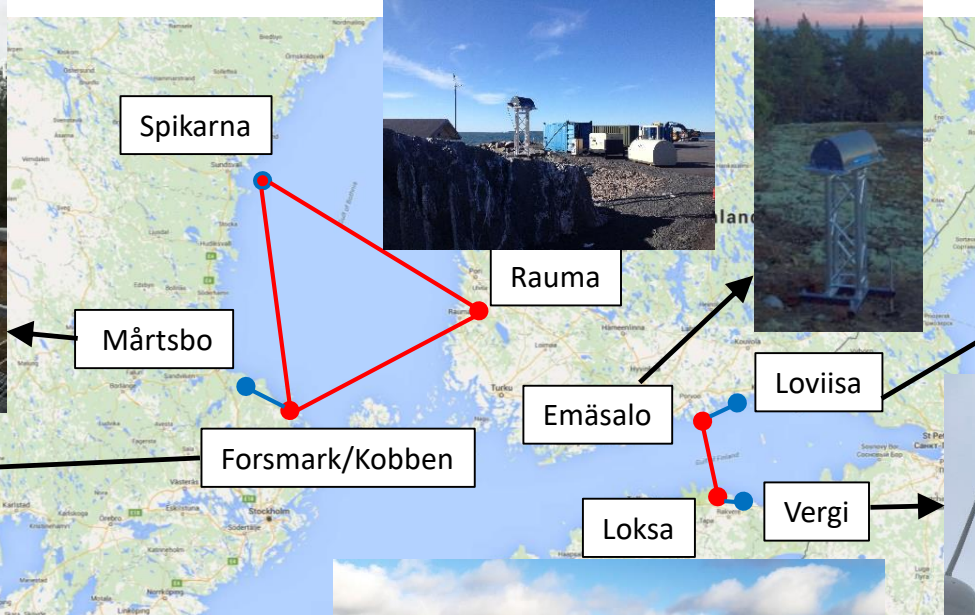
## Active SAR Targets (Electronic Corner Reflectors - ECR)



- |   |                        |                            |  |
|---|------------------------|----------------------------|--|
| <span style="color: red;">■</span> GNSS Reference Marker        | <u>Earth Geometry</u>  | <u>Earth Gravity Field</u> | <u>Tide Gauges</u>                     |
| <span style="color: blue;">■</span> Tide Gauge Reference Marker | $h$ Ellipsoidal Height | $H$ Physical Height        | $z$ Height wrt. Tide Gauge Zero Marker |
| <span style="color: black;">●</span> GNSS Permanent Station     |                        | $N$ Local Geoid Height     |  |



# Test Case Baltic Sea



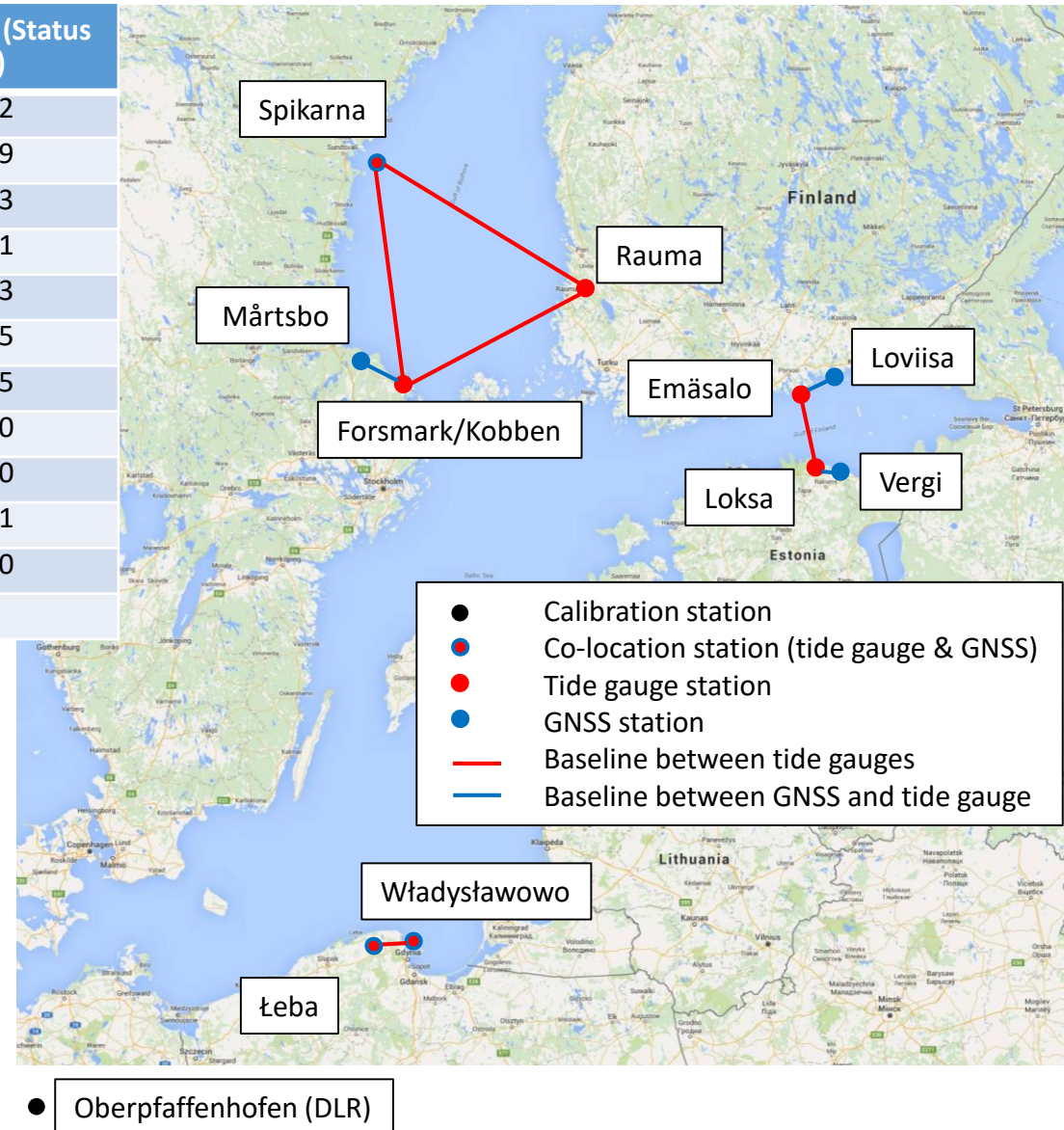
● Oberpfaffenhofen (DLR)

- Calibration station
- Co-location station (tide gauge & GNSS)
- Tide gauge station
- GNSS station
- Baseline between tide gauges
- Baseline between GNSS and tide gauge



# Test Case Baltic Sea

Location	Local Tie	Operational Since	No. SAR Scenes (Status 7.8.2020)
Loksa, Estonia	Tide Gauge	16.02.2020	A: 66 D: 62
Vergi, Estonia	GNSS	06.03.2020	A: 40 D: 39
Emäsalo, Finland	Tide Gauge	25.01.2020	A: 48 D: 33
Loviisa, Finland	GNSS	06.02.2020	A: 30 D: 31
Rauma, Finland	Tide Gauge	21.04.2020	A: 28 D: 13
Oberpfaffenhofen 112, Germany	GNSS	10.01.2020	A: 68 D: 35
Oberpfaffenhofen 113, Germany	GNSS	10.01.2020	A: 68 D: 35
Władysławowo, Poland	Tide Gauge, GNSS	26.03.2020	A: 29 D: 30
Łeba, Poland	Tide Gauge, GNSS	15.05.2020	A: 20 D: 20
Mårtsbo, Sweden	GNSS	07.01.2020	A: 47 D: 61
Forsmark/Kobben, Sweden	Tide Gauge	01.06.2020	A: 30 D: 20
Spikarna, Sweden	Tide Gauge, GNSS	Not yet installed	-



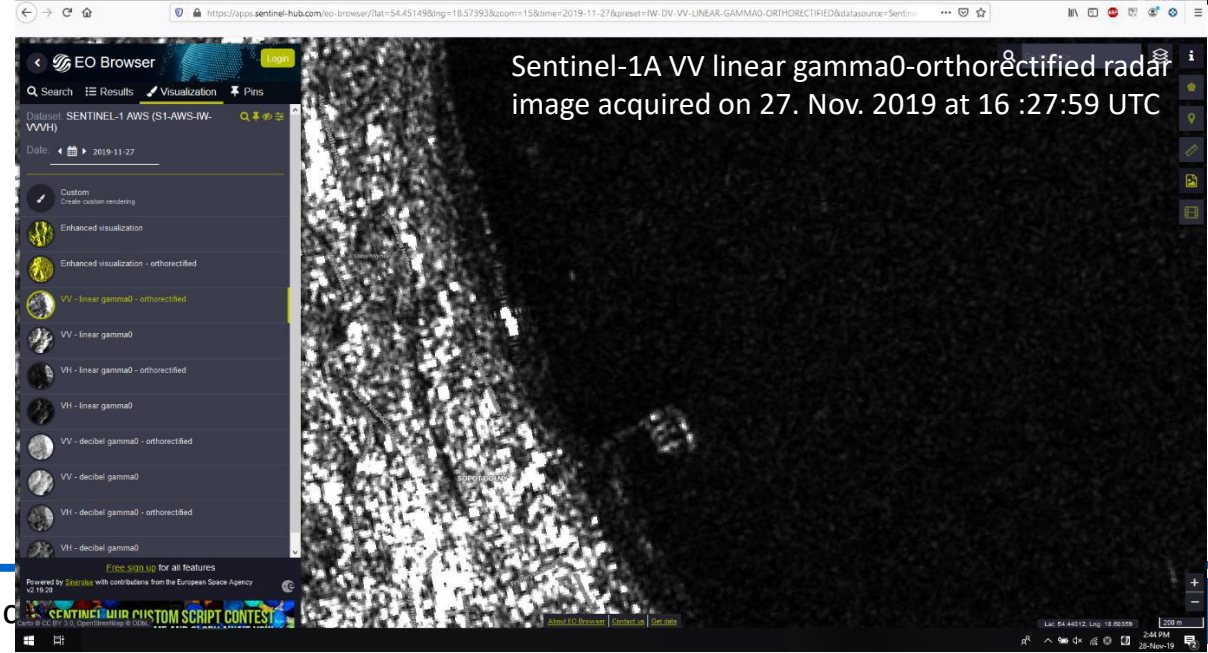
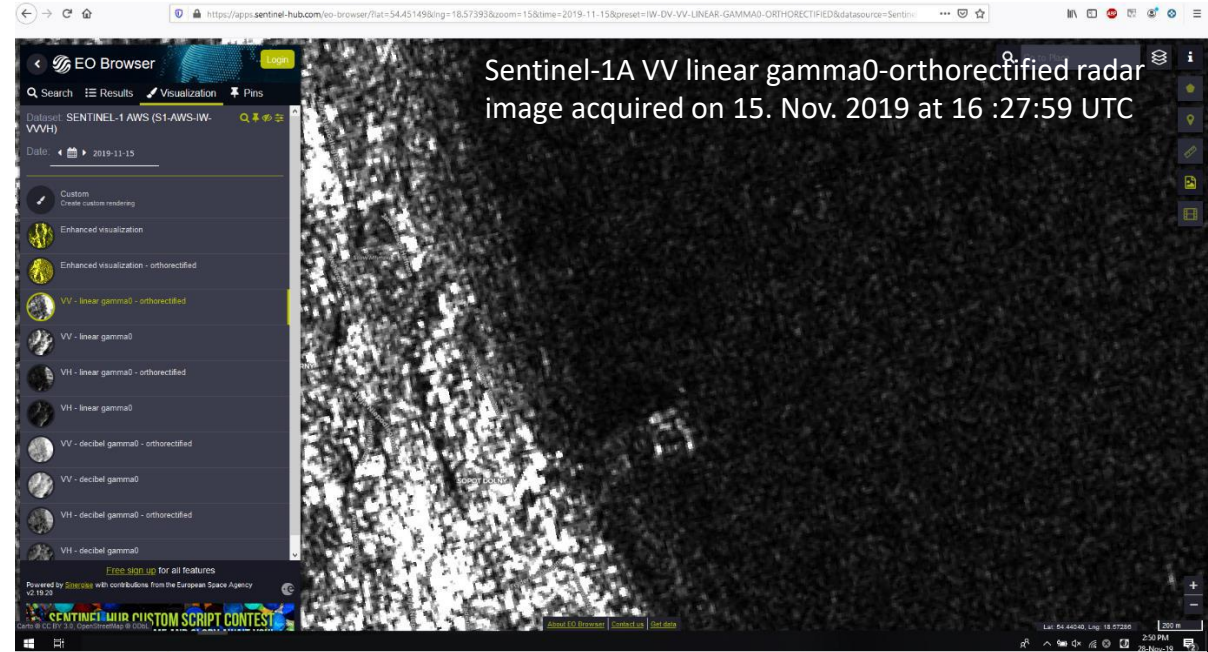
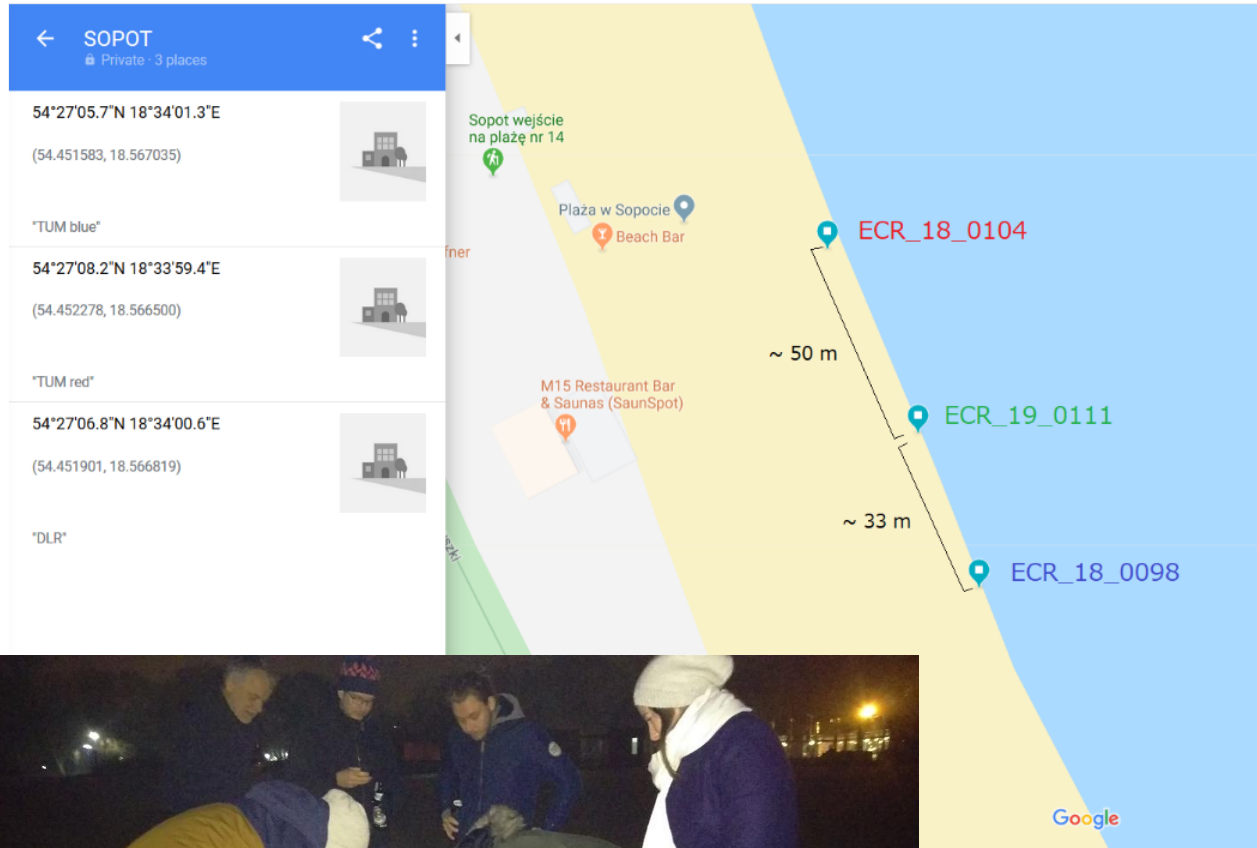
## Experiments Plan:

1. ECR Calibration at DLR Oberpfaffenhofen
2. Collocation Sites: Tide Gauges and permanent GNSS
3. Tide Gauge Sites
4. Permanent GNSS Sites – Short Baselines
5. Long Baselines (Finland to Estonia, Sweden to Finland)
6. Tide Gauge Linking (Polish Stations)
7. Absolute vs. Relative SAR for short Baselines

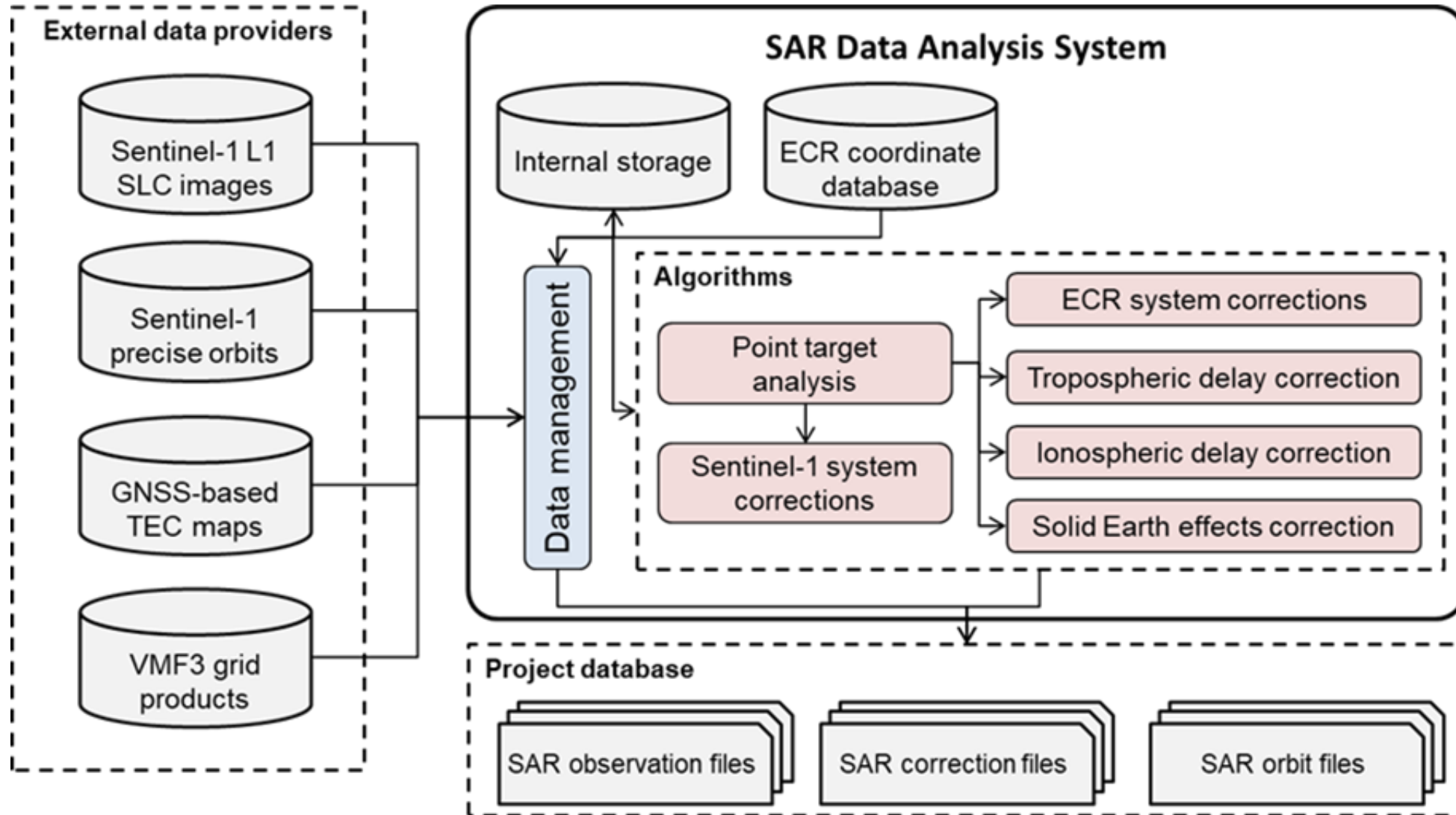


# Test Case Baltic Sea

## ECR Testing at Sopot/Gdansk, Poland (27. Nov. 2019)



# SAR Data Analysis

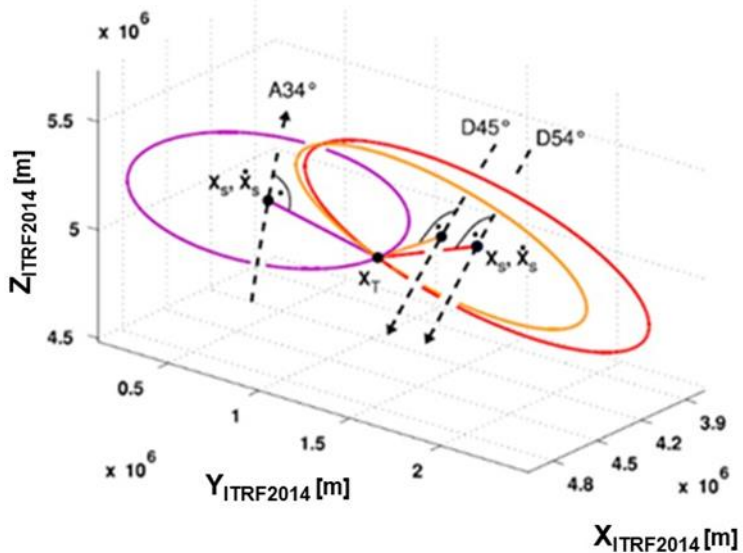


# SAR Positioning

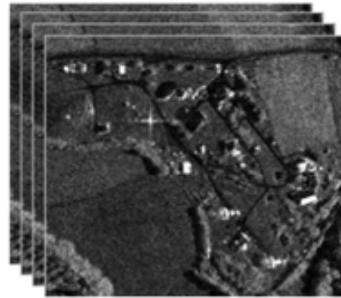
## Range-Doppler Equation System

$$|\mathbf{X}_S(t) - \mathbf{X}| - \frac{c}{2} \cdot \tau$$

$$\frac{\dot{\mathbf{X}}_S(t)(\mathbf{X} - \mathbf{X}_S(t))}{|\dot{\mathbf{X}}_S(t)| |\mathbf{X} - \mathbf{X}_S(t)|} = \sin \alpha$$



## L1b images



## L1b metafiles

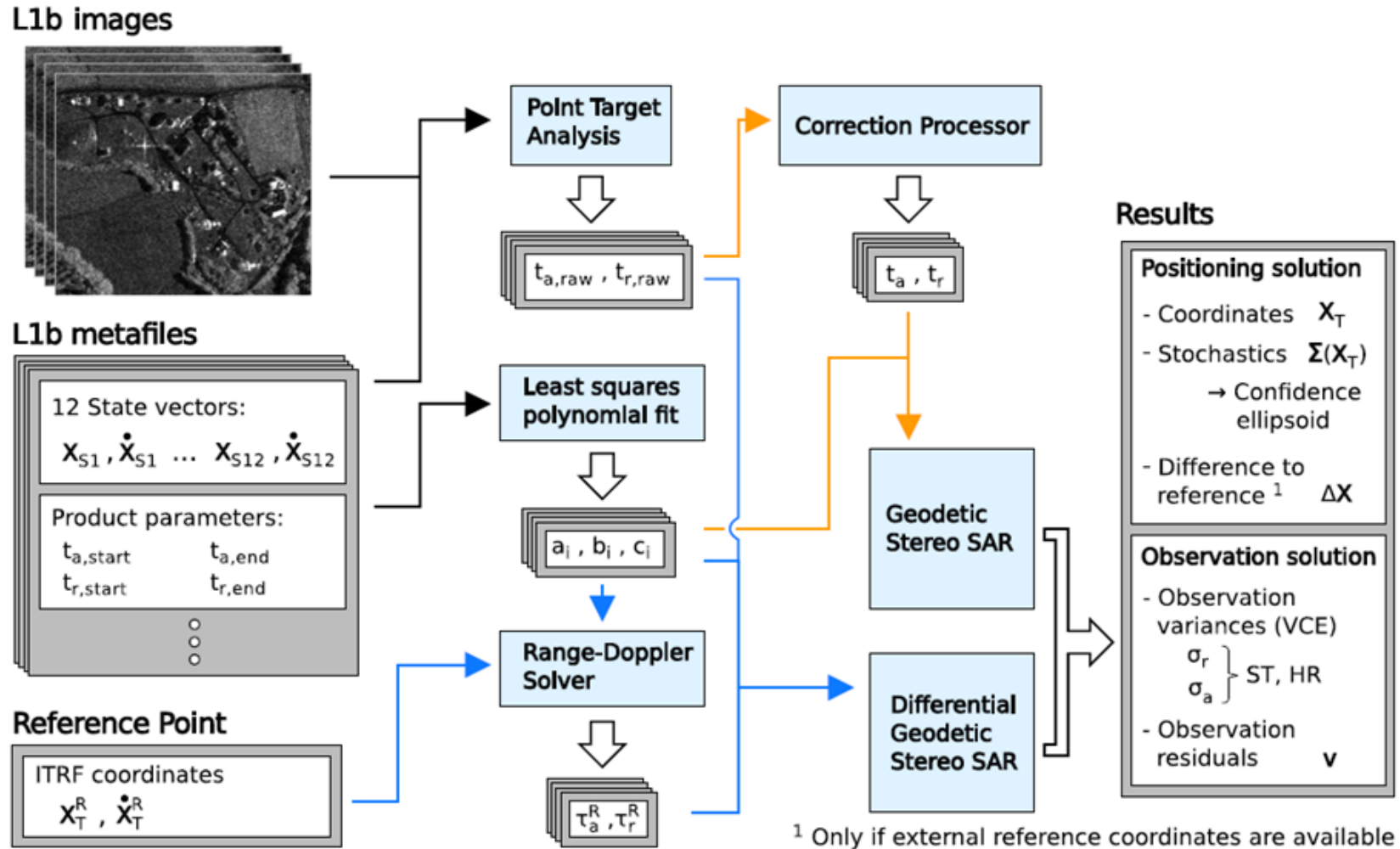
12 State vectors:  
 $\mathbf{X}_{S1}, \dot{\mathbf{X}}_{S1} \dots \mathbf{X}_{S12}, \dot{\mathbf{X}}_{S12}$

Product parameters:  
 $t_{a,start} \quad t_{a,end}$   
 $t_{r,start} \quad t_{r,end}$

○  
○  
○

## Reference Point

ITRF coordinates  
 $\mathbf{X}_T^R, \dot{\mathbf{X}}_T^R$



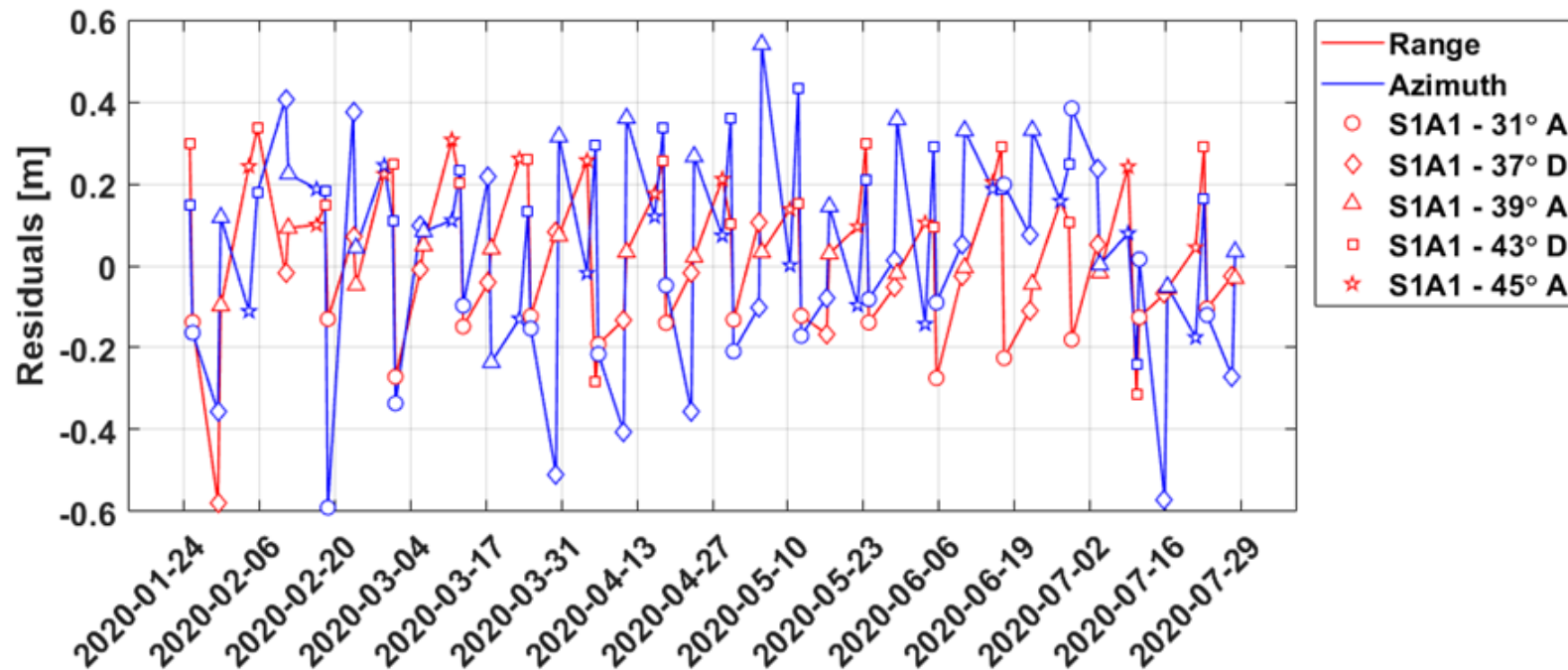
<sup>1</sup> Only if external reference coordinates are available



# SAR Positioning – First Results

Absolute positioning: without compensation for outliers and biases per incidence (original approach)

Station	X [m]	Y [m]	Z [m]	$\sigma_x$ [m]	$\sigma_y$ [m]	$\sigma_z$ [m]
Emäsalo (original)	2864911.2403	1374214.0007	5511816.3914	0.0182	0.0304	0.0252



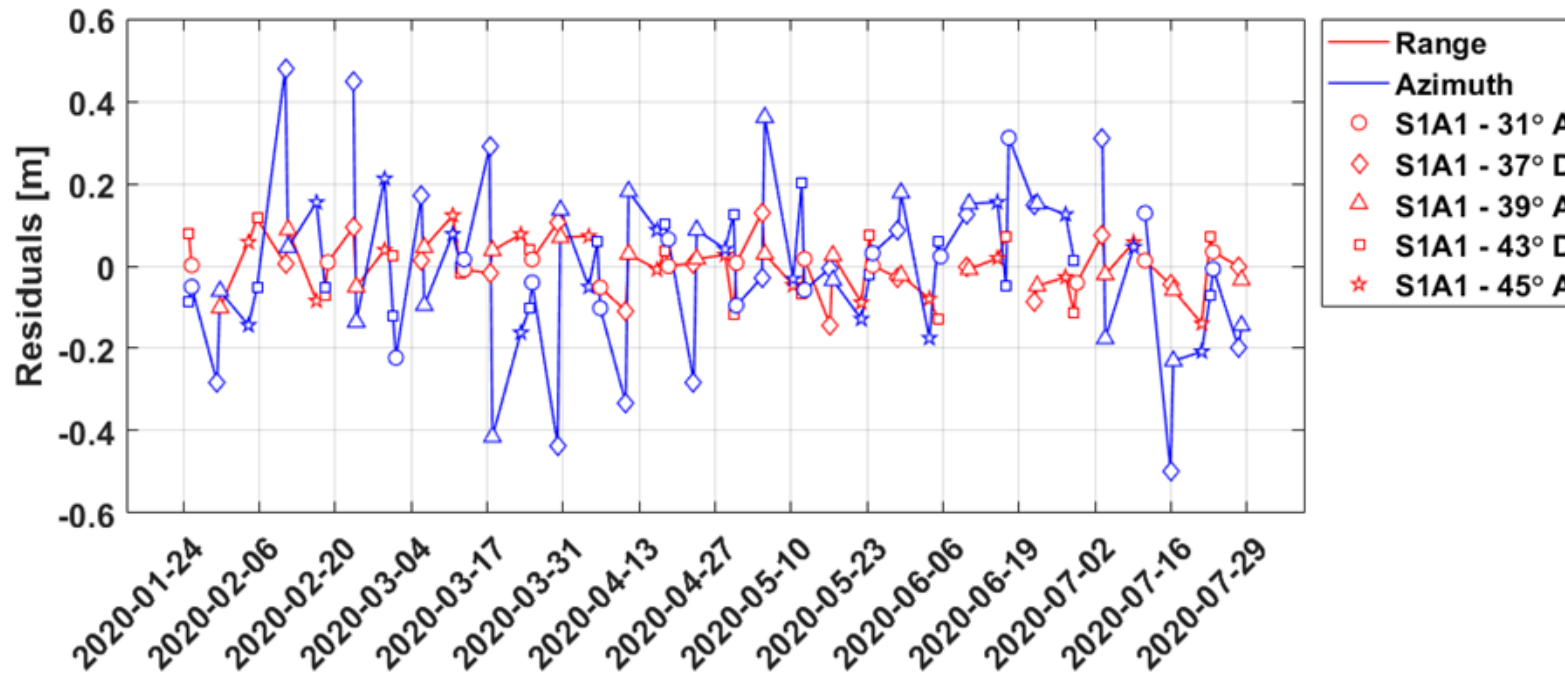
Least squares minimized residuals of the range and azimuth observations per incidence angle. The azimuth timings are expressed in meters by multiplication with the flight velocity of Sentinel-1.

Legend: S1A1: Sentinel-1A image, Incidence angle in degrees, A/D: Ascending/Descending arc.

# SAR Positioning – First Results

Absolute positioning: without (original) and with (refined) compensation for outliers and biases per incidence angle

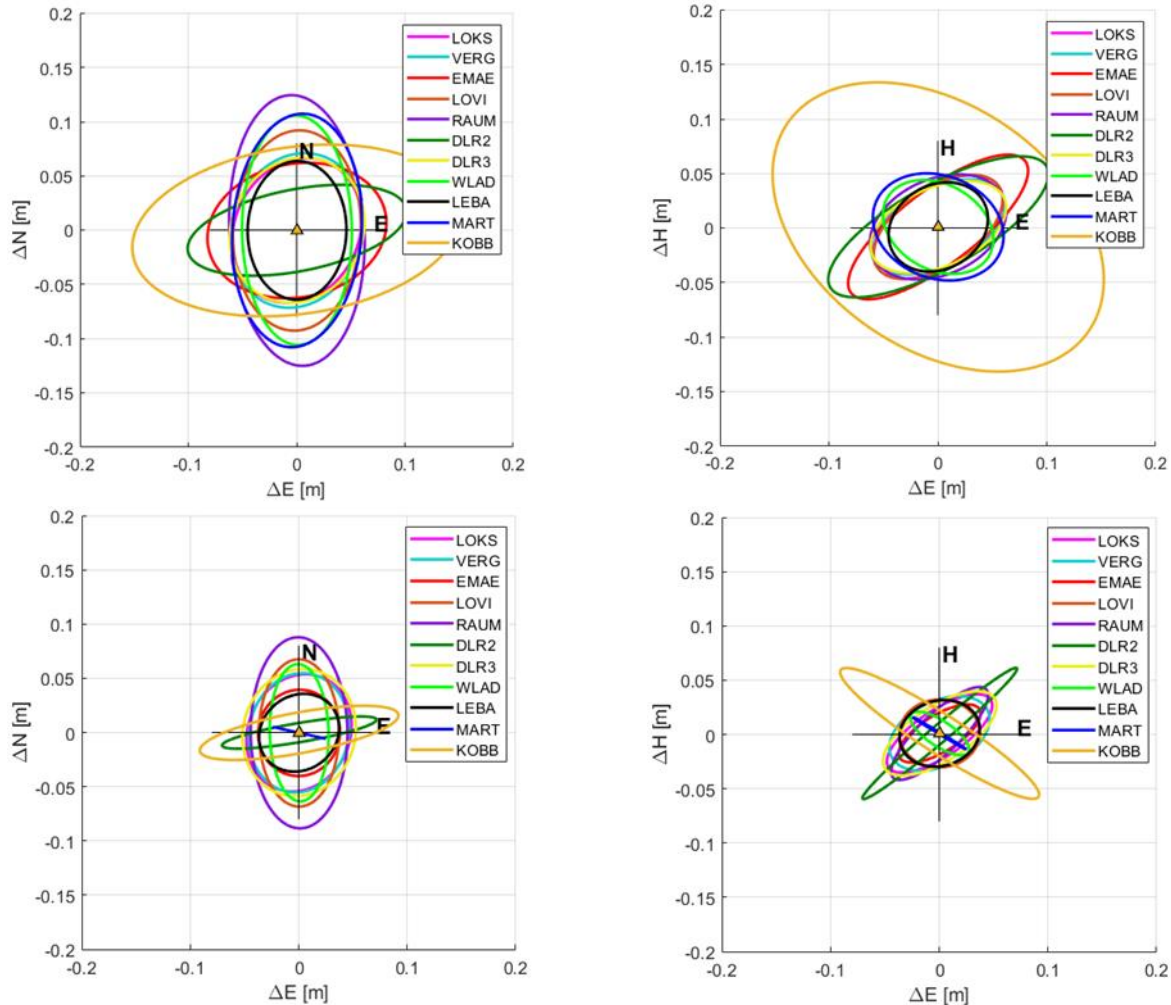
Station	X [m]	Y [m]	Z [m]	$\sigma_x$ [m]	$\sigma_y$ [m]	$\sigma_z$ [m]
Emäsalo (original)	2864911.2403	1374214.0007	5511816.3914	0.0182	0.0304	0.0252
Emäsalo (refined)	2864911.2403	1374214.0007	5511816.3914	0.0110	0.0142	0.0119



Least squares minimized residuals of the range and azimuth observations per incidence angle. The azimuth timings are expressed in meters by multiplication with the flight velocity of Sentinel-1.

Legend: S1A1: Sentinel-1A image, Incidence angle in degrees, A/D: Ascending/Descending arc.

# SAR Positioning – First Results



95% confidence ellipsoids in the horizontal North-East (left column) and vertical height-East view (right column) using the original (upper row) and refined (bottom row) absolute positioning technique.

Estimated coordinate standard deviations for all stations of the Baltic ECR stations applying the refined positioning technique.

Station	$\sigma_x$ [m]	$\sigma_y$ [m]	$\sigma_z$ [m]	# Images
Loksa	0.0150	0.0180	0.0167	122
Vergi	0.0159	0.0167	0.0161	75
Emäsalo	0.0110	0.0142	0.0119	77
Loviisa	0.0186	0.0146	0.0174	72
Rauma	0.0230	0.0190	0.0224	28
DLR2	0.0064	0.0259	0.0182	21
DLR3	0.0149	0.0194	0.0192	99
Władysławowo	0.0166	0.0099	0.0162	55
Łeba	0.0113	0.0126	0.0123	36
Mårtsbo	0.0034	0.0080	0.0055	102
Forsmark/Kobben	0.0248	0.0260	0.0163	43



# Summary, Conclusions & Future Work (1)

- For absolute Sea Level and Height System Unification **tide gauges need to be connected with global geometric and physical height reference networks.**
- Very crucial for such an observing system is the **monitoring of the tide gauge stations for vertical movements** and the determination of **physical heights referring to a global physical reference surface.**
- Only a few tide gauge stations nowadays are permanently equipped with GNSS receivers. Therefore, as a **new technique, the 3D geodetic SAR positioning with active transponders (ECRs)** for densifying existing permanent GNSS networks is introduced.
- The **effort and costs** for installing, maintaining and operating active SAR transponders is **much less** than for a permanent GNSS receiver. **Data are collected via the SAR satellites** and there is no need to store and transmit data.
- Three **different heights need to be combined** (tide gauge records, ellipsoidal heights, geoid heights). To avoid systematic errors in the resulting absolute sea level heights it is needed to use **same standards and reference systems.**
- For a feasibility study an **observing system** has been installed by the project team **in the Baltic Sea area.** All in all, 12 ECRs are installed.
- A number of **experiments** has been identified. This includes among others ECR calibration, absolute and relative positioning, short baseline and long baseline coordinate transfer across the sea.
- Absolute **positioning experiments for 11 stations** have been performed in order to identify the performance of the active transponders in the sense of achievable internal accuracies.

## Summary, Conclusions & Future Work (2)

- The **internal accuracy of 3D absolute positions** applying a simple outlier detection procedure is at a level of **about 4.3 cm** for the station in Emäsalo.
- Post-fit **range residuals depend on the incidence angle** of radar image. Refined procedure estimates biases per incident angle class. **3D position accuracy improved to about 2.1 cm** for Emäsalo (similar for other stations).
- Error **ellipses in a local horizontal coordinate system** (North-East-Height) are computed. Ellipses with larger eccentricities indicate correlations between coordinate axes.
- Absolute **positions are very stable** disregarding the applied approach. This is an indicator that the **absolute coordinate estimation is robust** and that it delivers meaningful results.
- **ECR locations need to be selected very carefully** such that possible other artificial reflectors are avoided.
- Analyses to be performed: (1) **Refinement of SAR positioning** for phase center variations and electronic antenna behavior; (2) Application of **relative SAR positioning**; (3) **Calibration** of ECR and identification of possible systematic delays; (4) **Local geoid** refinement at the tide gauge stations; (5) **Processing tide gauge** observations; (6) Transformation of coordinates into a **unique reference frame**; (7) Computation of absolute sea level heights at tide gauge stations and identification of **height system offsets**; (8) **Validation** of height system differences by comparison to levelled heights.
- There is still a lot to be done to **meet the 1 cm requirement in height**. ECRs can help to systematically **observe vertical movement of tide gauge stations**. Then tide gauges can also be used for determining the absolute sea level.