

# **Ocean Surface Currents in the northern Nordic Seas from a combination of multi-mission satellite altimetry and numerical modeling**

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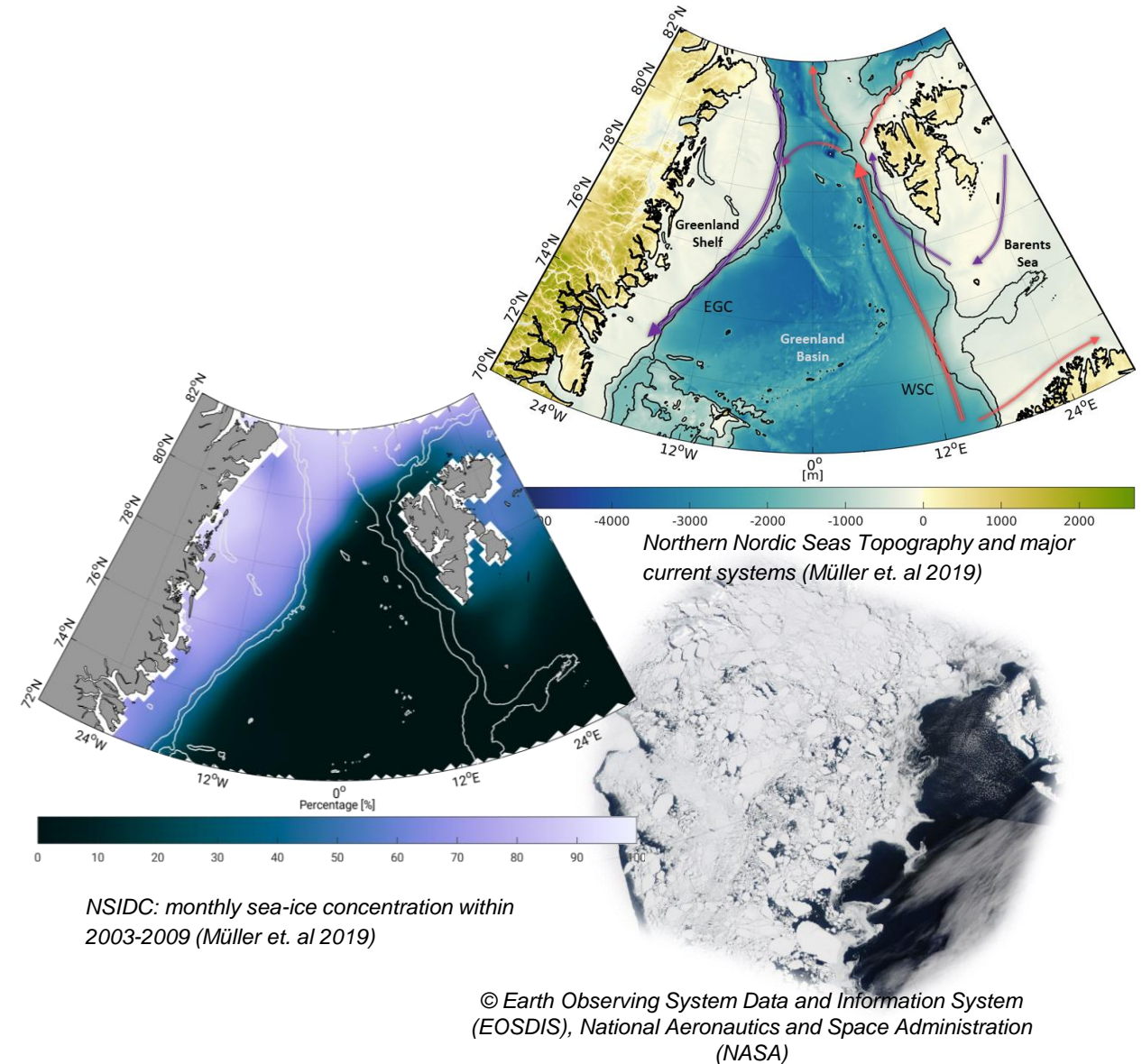
# Motivation

## The current status:

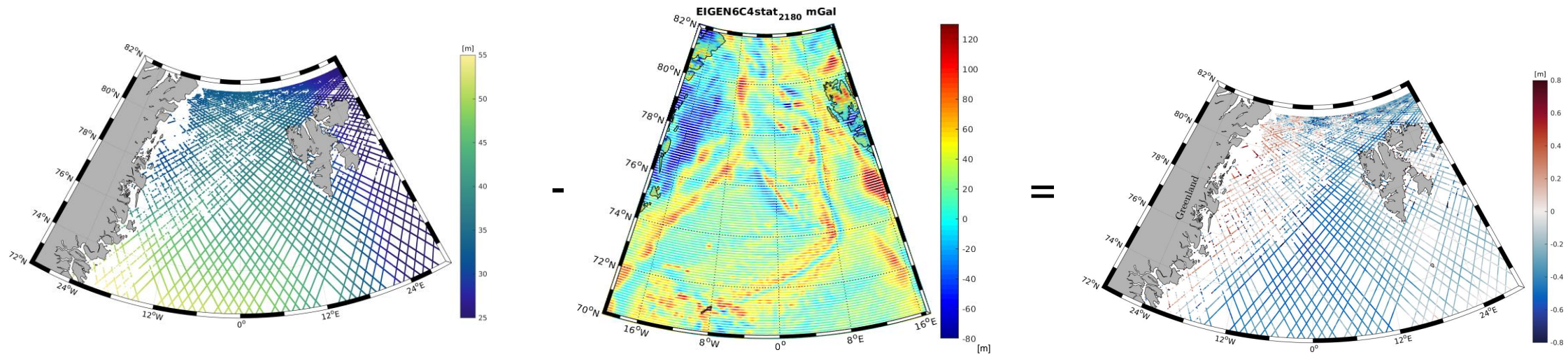
- Temporal variable Dynamic Ocean Topography (DOT) enables detection of surface current variabilities
- Altimetry derived polar DOT is affected by irregular sampling and data gaps (along-track data, sea-ice)
- Models can give spatio-temporal consistent DOT information, but are limited by mathematical assumptions and restrictions

## The idea:

- Exploitation of possible synergy effects of both datasets
  - Altimetry Sea Surface Observations
  - Ocean Model Simulation
- Generation of an innovative homogenous, temporal-variable DOT in polar regions (i.e. combination), with the possibility to derive geostrophic surface currents – Model should support observational data.
- Requires: 1. Comparison of datasets and 2. Combination of datasets from observational point of view - **No data assimilation**



# Short excursion: Sea Surface Heights (SSH), Geoid and DOT



E.g. EIGEN-6C4 (Förste et al. 2014)

## ➤ Sea surface heights

(Reference: Ellipsoid)

- Altimetry provides distance between satellite COM and sea surface (retracked altimetry range)
- $SSH = \text{satellite orbit height} - (\text{range} + \text{corrections})$

## ➤ Geoid

- Equipotential earth surface
- Shape of the earth just considering gravity changes and Earth rotation
- Approximates the mean sea level
- Examples: EIGEN-6C4 (GFZ) or OGMOC (IAPG)

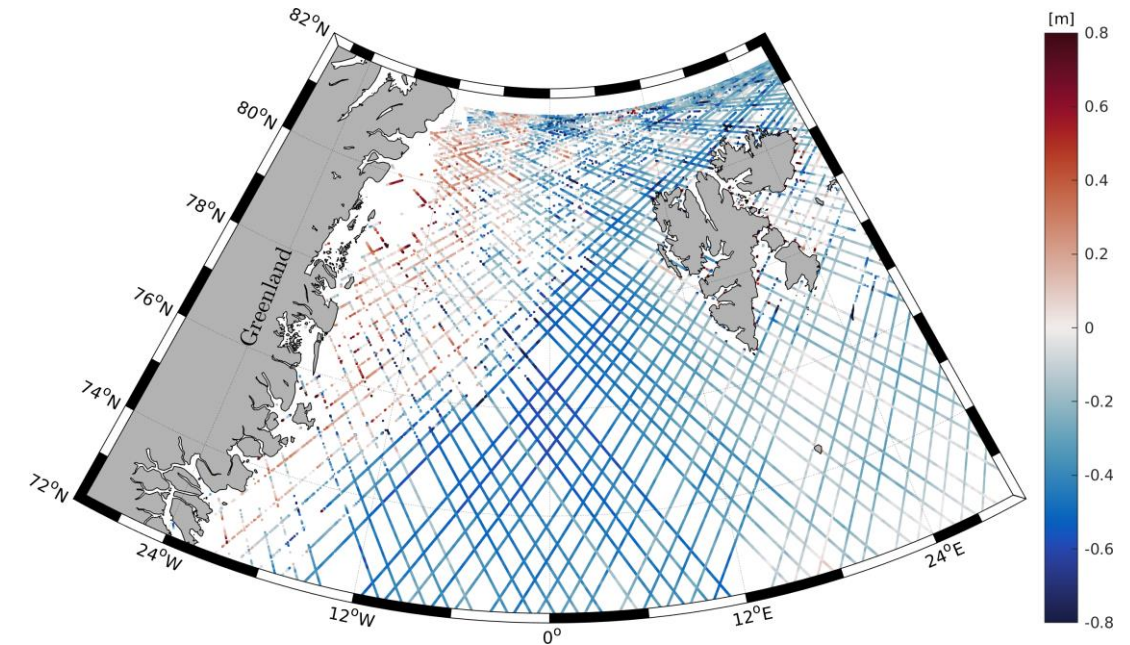
## ➤ DOT

- Sea surface affected by hydrodynamic processes and gravity variations (Reference: Geoid)
- Used to compute geostrophic currents

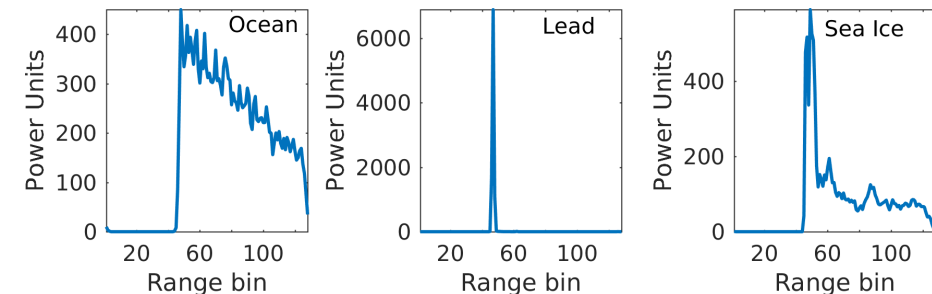


# Observational DOT: Altimetry (ESA: ERS-2, Envisat)

- High-frequency altimetry data (20 Hz)
- Consistent estimated SSHs
  - Retracker, ALES+ (Passaro et al., 2018)
  - No offset between sea-ice and ocean areas
- Elimination of sea-ice contaminated radar echoes
  - Unsupervised classification (no training data)
  - Assignment of sea-ice and open water radar echoes (Müller et al., 2017)
- Transformation to DOT heights by subtracting high resolved geoid (OGMOC, Gruber & Willberg, 2019) → 2190 degrees
- Spatial filtering of profiled data with ~9km moving average filter



Example: Along-track DOT heights

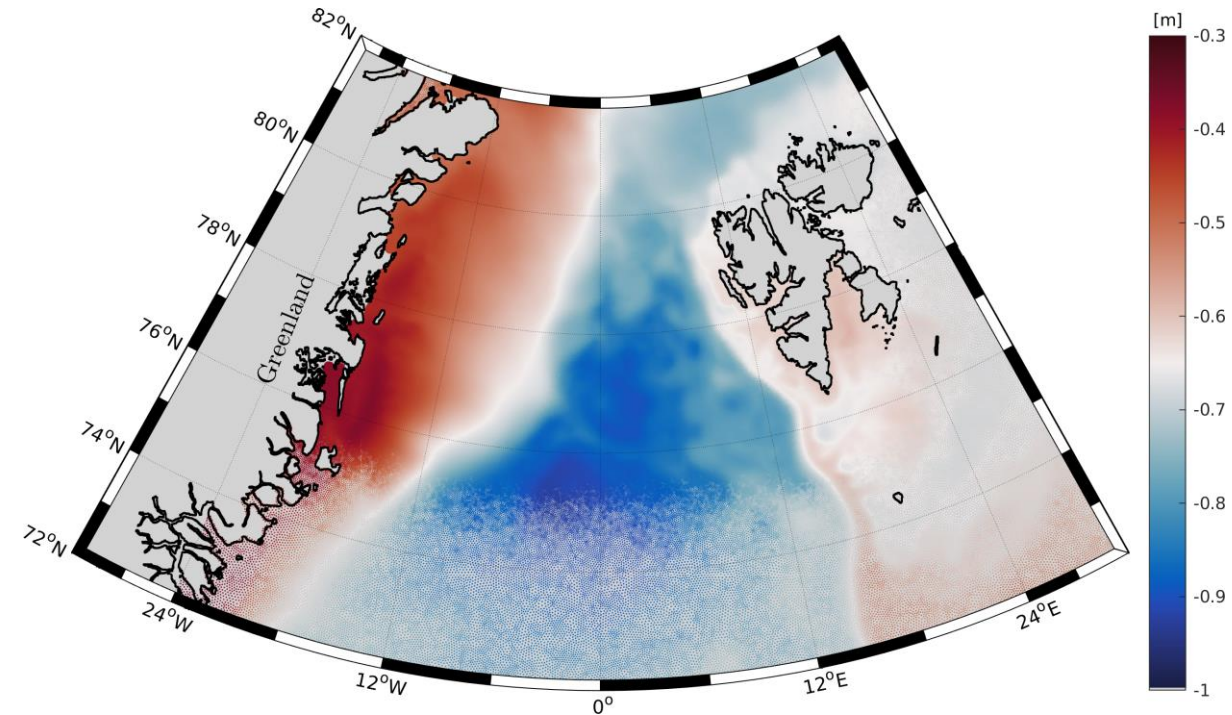


Example: Envisat Waveforms

# Modelled DOT: FESOM (eddy resolving configuration)

## ➤ Finite Element Sea-Ice Ocean Model (FESOM)

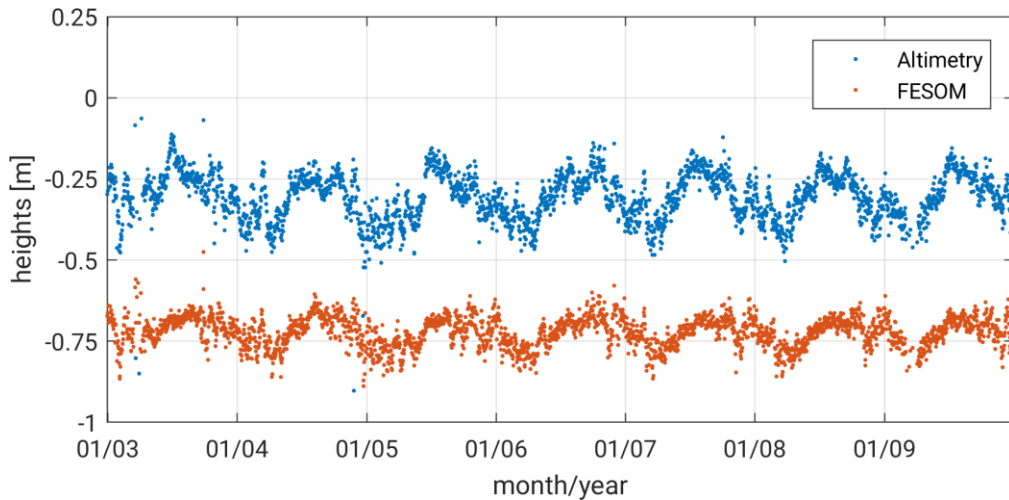
- Irregular, unstructured (<1km sp. resolution) mesh with local refinements
- Daily differential water heights w.r.t bathymetry
- Covers years 2002 – 2009
- Water heights are comparable to DOT heights
- Includes sea-ice component considering major sea-ice drift patterns
- Conserves for volume not for mass
- Does not include: barometric effects and ocean tide signal



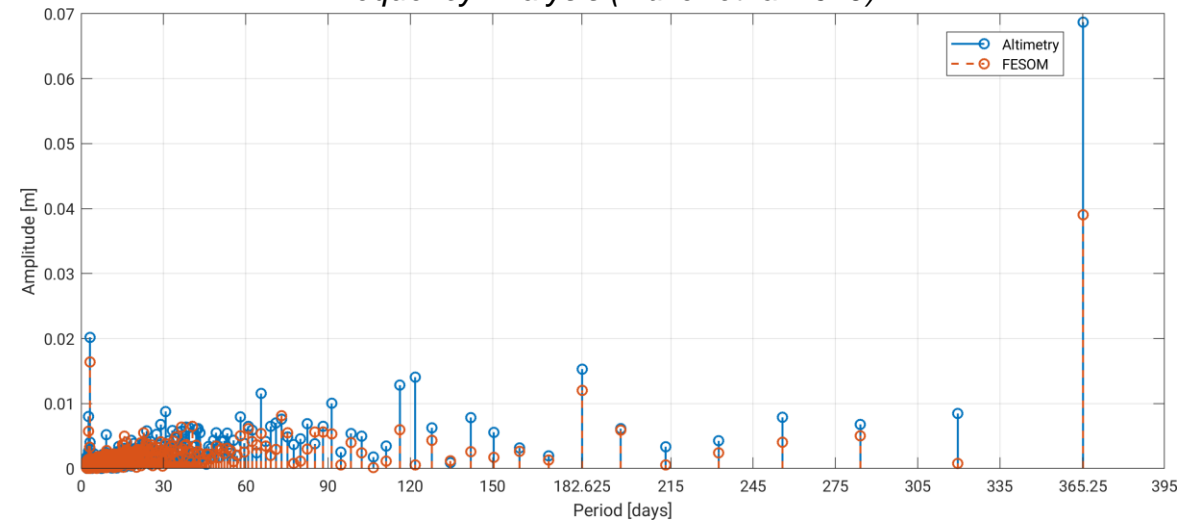
Example: FESOM Differential Water heights

# Temporal Comparison – Frequency analysis

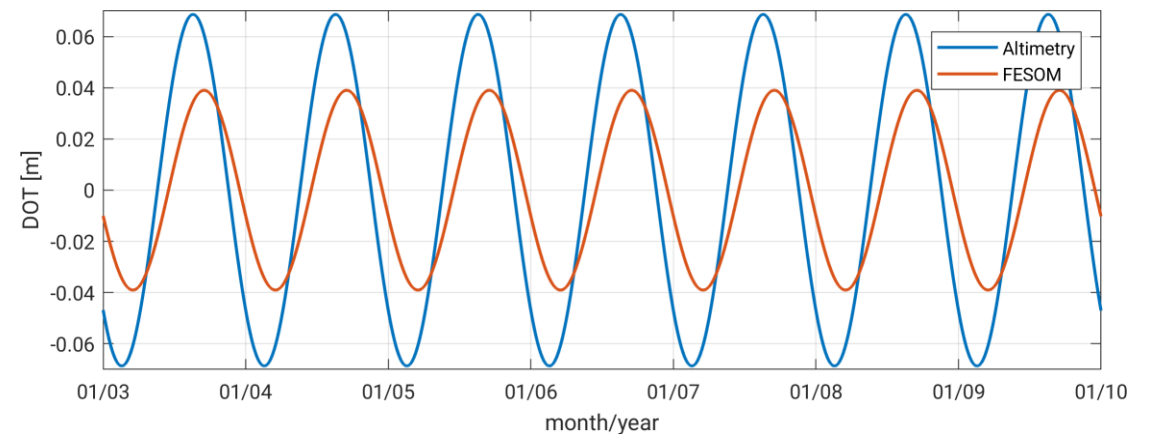
Time Series Daily means (Müller et. al 2019)



Frequency Analysis (Müller et. al 2019)



Annual signal

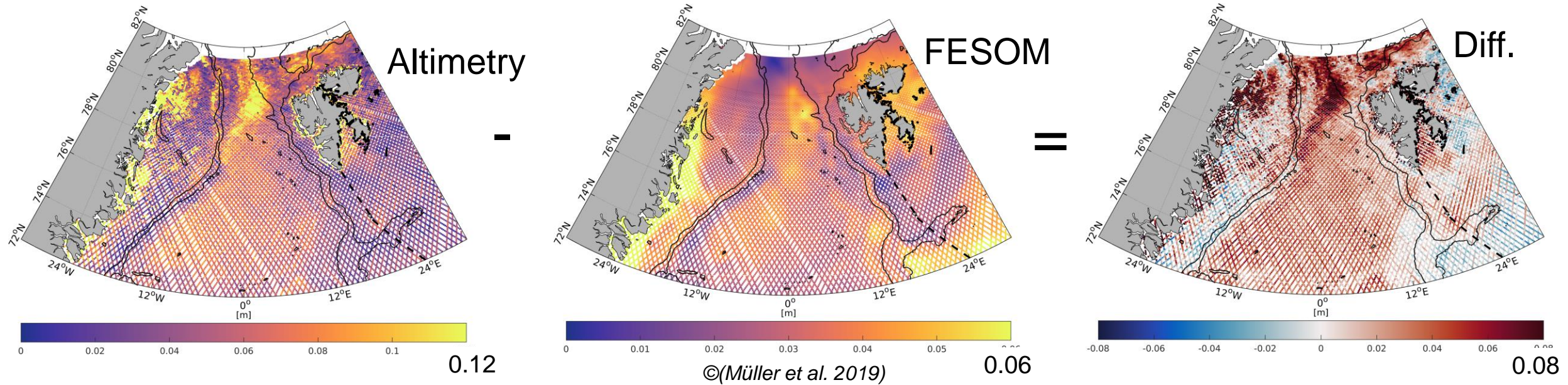


Annual signal (Müller et. al 2019)

- Interpolation of FESOM water heights to altimetry ground track locations (nearest-neighbor)
- Daily means of available observations and interp. model data
- Harmonic freq. analysis of both datasets (2003 – 2009)
- Annual period dominates in both datasets (365.25 days)
- Amplitude: ~7cm (Altimetry) vs. ~4cm (FESOM)
- Minor subordinated periods
- Phase shift: ~ 30 days



# Spatial Comparison - Annual Signal

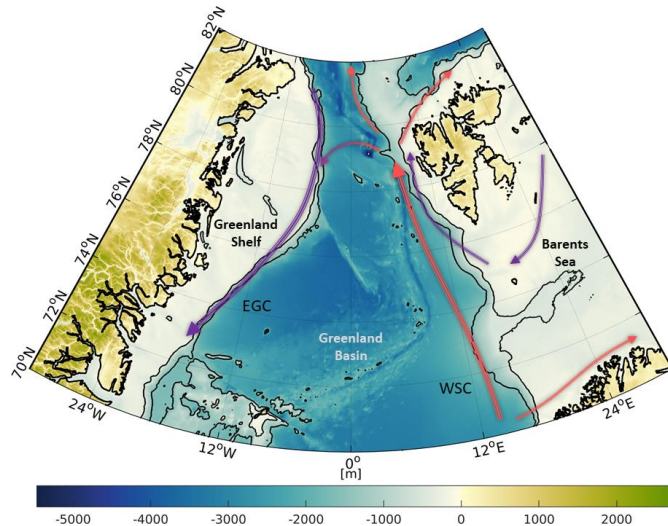


- Comparison of altimetry DOT and FESOM water heights, based on nominal ground track
- Data is equally ordered in bins (7.5km)
- Significant differences in sea-ice regions and at the coast
- Altimetry DOT shows higher seasonal variability and stronger magnitude
- Phase differences in central Greenland Sea

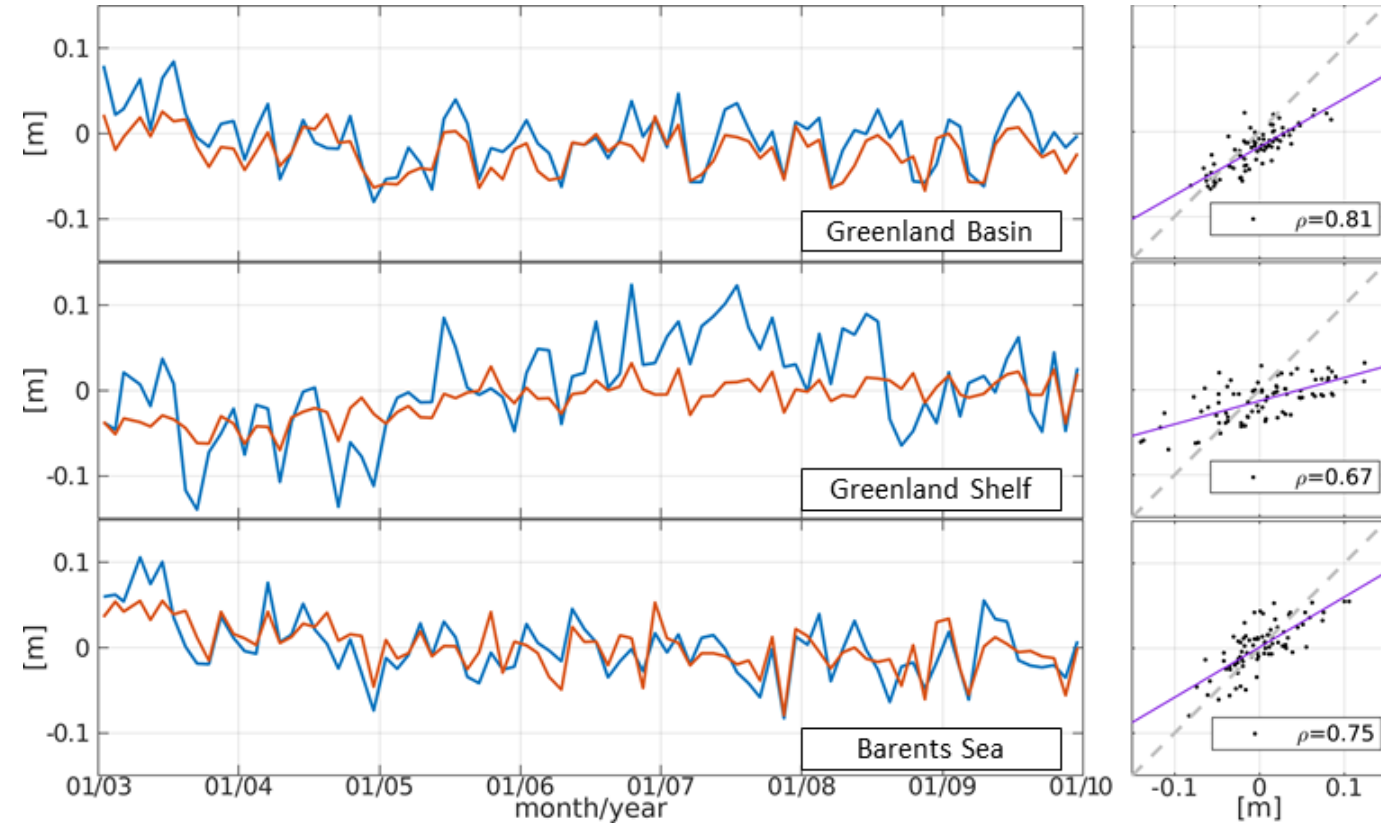
Region	Amplitude [cm]	Day of maximum
Greenland Basin	6.3 (Altimetry) 3.0 (FESOM)	233 (Aug) 267 (Sept)
Greenland Shelf	5.7 3.8	315 (Nov) 312 (Nov)
Barents Sea	4.0 3.8	284 (Oct) 304 (Oct)

# Differential analysis: Temporal evolution

- Reduction of both datasets by constant offsets and annual oscillation
- High correlation in all sub-areas indicate good agreement
- No systematic effects in Greenland Basin and Barents Sea
- Observed trend in Greenland Shelf not significant



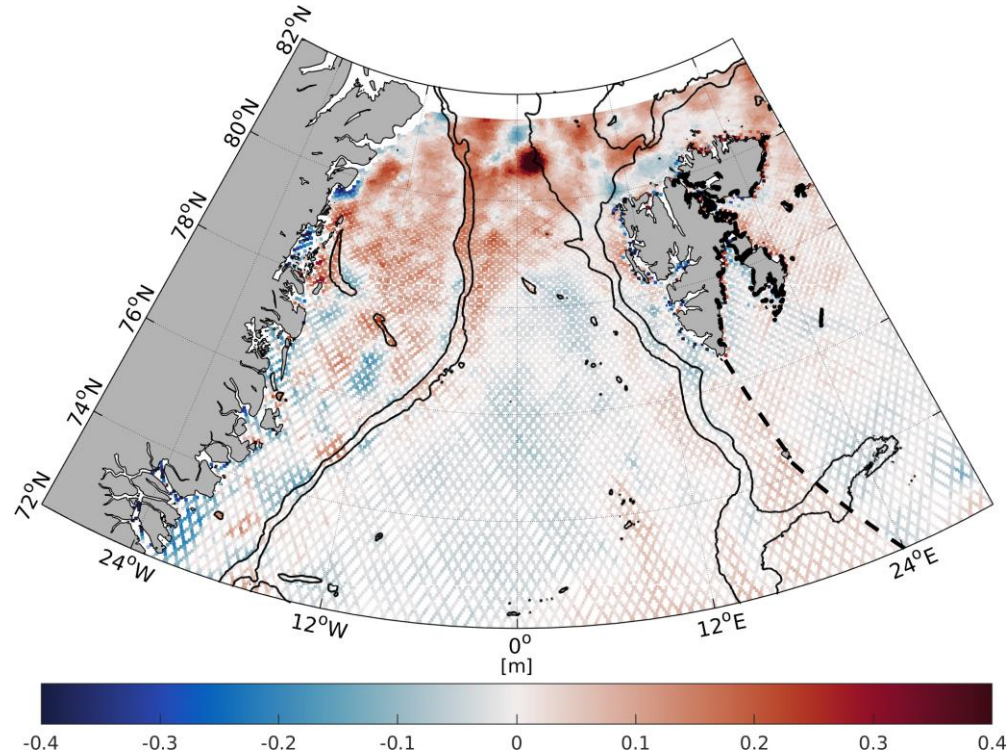
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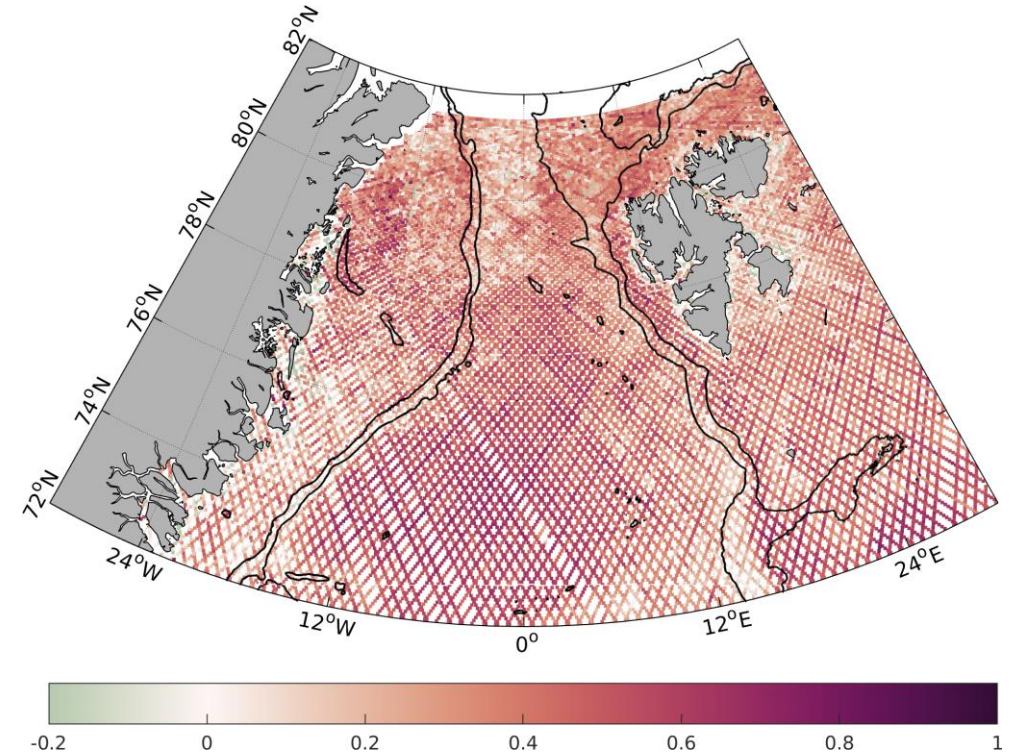


# Differential analysis: Spatial patterns



Mean Differences 2003-2009

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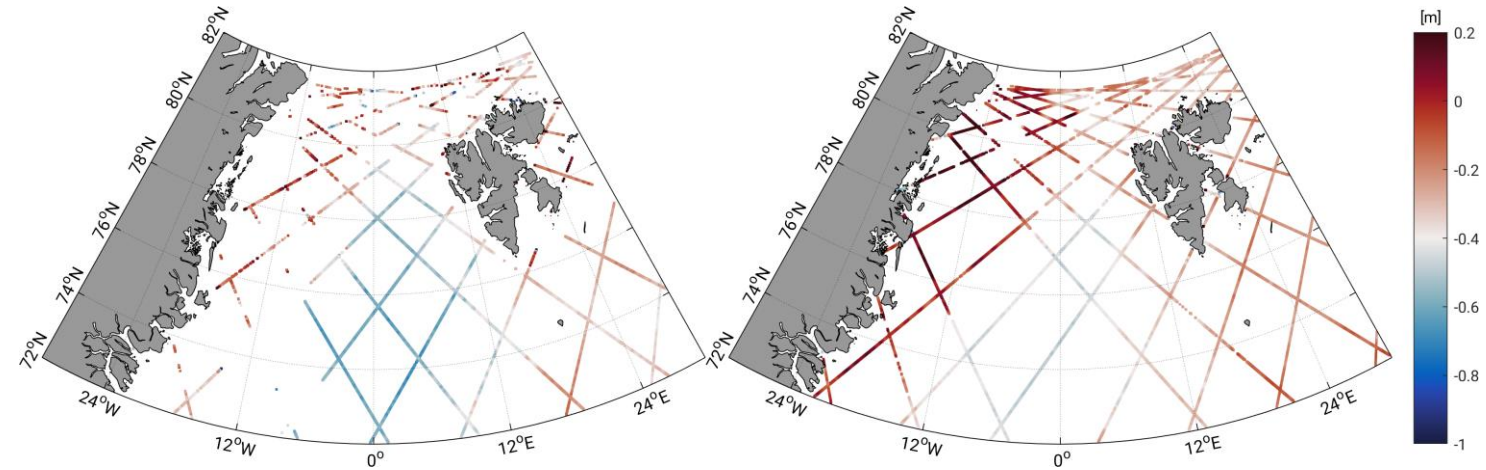


Correlation 2003-2009

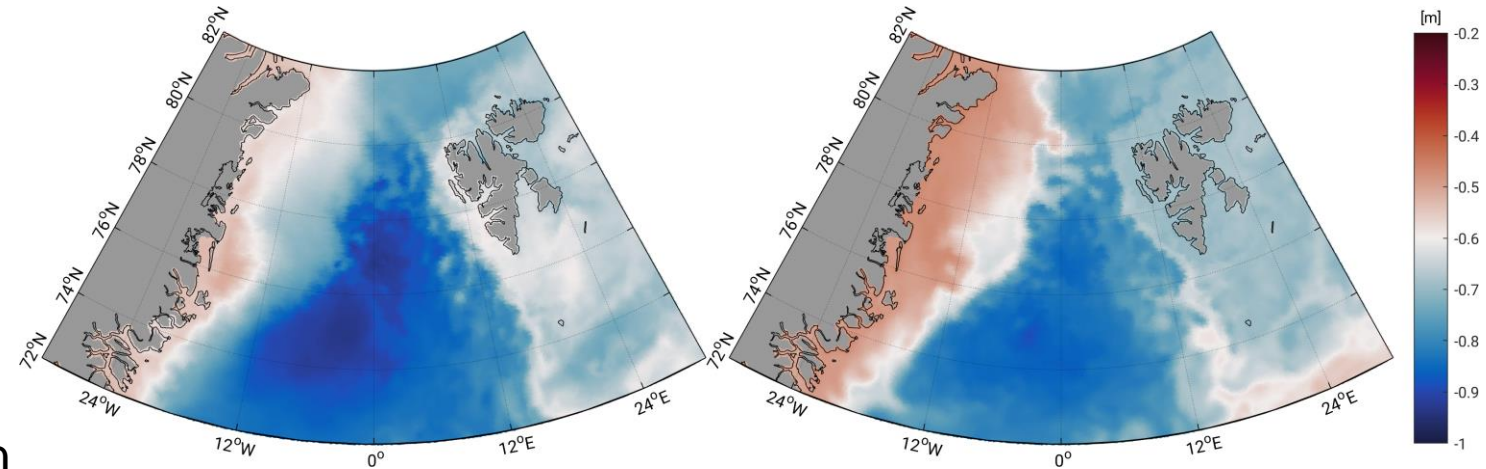
- Small differences in Greenland Basin
- Strong differences in Fram Strait (>40cm), due to geoid uncertainties
- Mostly positive correlation in study area (>0.5, 21%)
- Lower correlations in current areas

# Combination of multi-mission altimetry with ocean modeling

- Combination of ~20 years multi-mission altimetry (Envisat, ERS-2) with simulated DOT heights
- Projection of along-track DOT heights to the modeled DOT heights keeping altimetry height reference
- The temporal variability is given by altimetry, whereas the spatial signal is provided by the model
- Application of Principal Component Analysis
- Enables the generation of a 20 years covering DOT and geostrophic circulation dataset (model mesh)



3-days altimetry (top) and daily FESOM (bottom) DOT in March 2004 (left) and July 2006 (right) © (Müller et al. 2019)





# Short excursion: Principal Component Analysis (PCA)

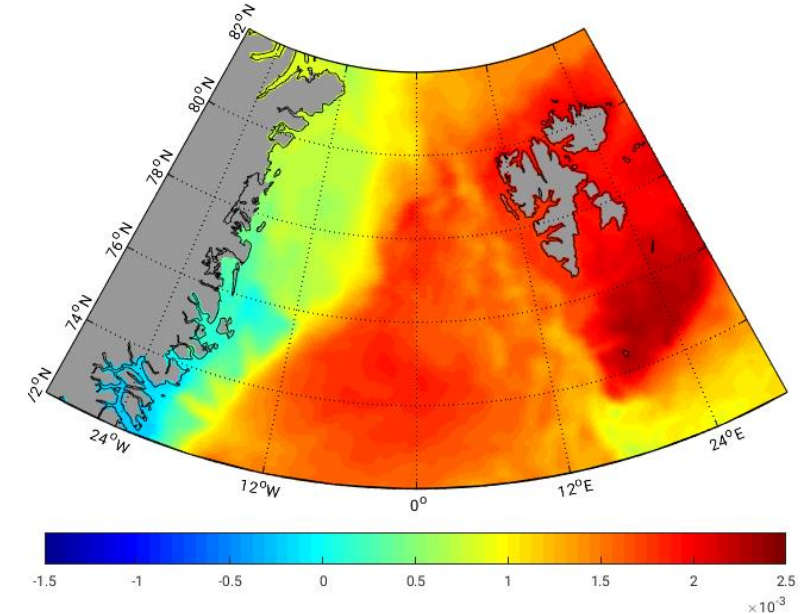
- Other name: Empirical Orthogonal Function Analysis
  - Empirical Orthogonal Functions (EOF) are part of PCA

## Why and what is for?

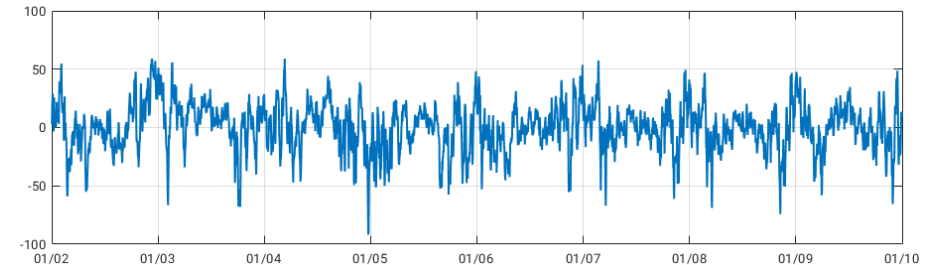
- **PCA identifies spatial structures (eigenvectors, EOF) and the temporal evolution (principal components, pc) of a multi-variate dataset (FESOM meshes, sea level grids etc.)**
- Application: Extraction of dominant ocean phenomena (e.g. El Niño)

## What is a Mode?

- **A single eigenvector (EOF) multiplied with the associated pc**
- The first mode explains the most dominant part of a signal
- Modes are sorted in a decreasing order (significant contribution to the signal variance)
- Summation of i-Modes enables the reconstruction of the total signal or w.r.t. a specific degree of approximation → **PCS**



Example: FESOM EOF1 (48%)



Example: FESOM pc1 (48%)

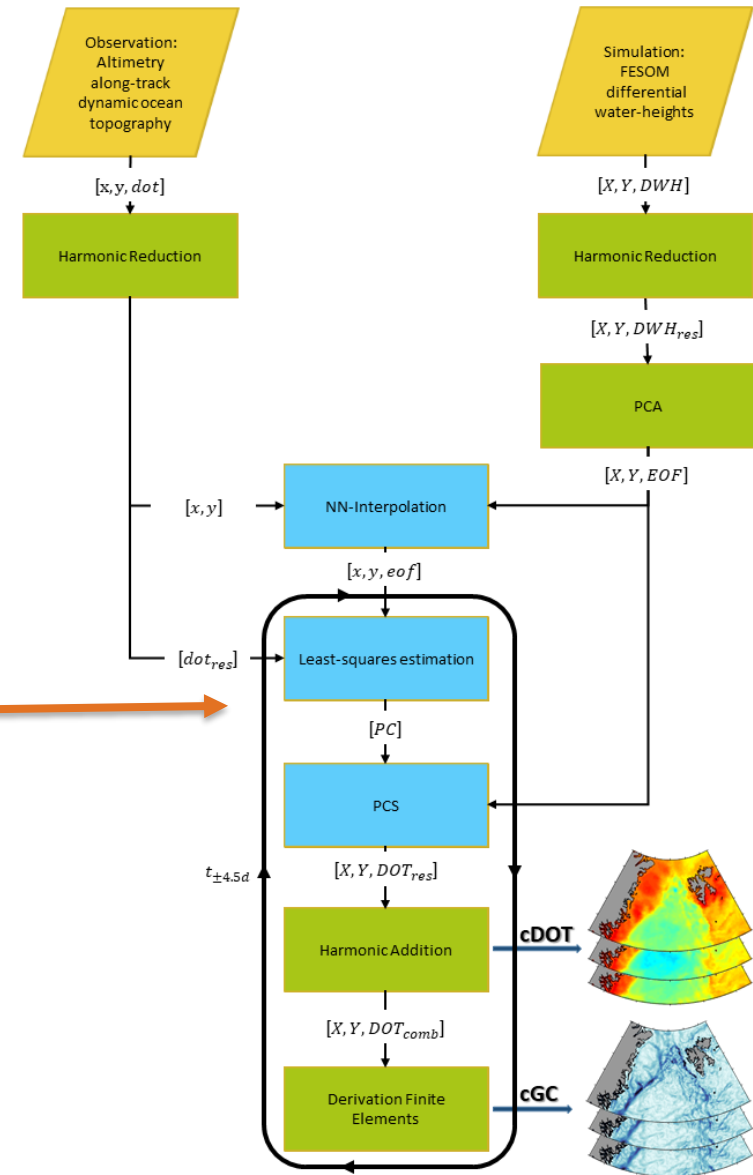


# Combination – Processing Steps

- Combination of by constant offset and annual signal reduced observational and modeled datasets
- Process based on Principal Component analysis (PCA)
  - Dominant spatial patterns are provided by FESOM
  - DOT temporal variability is given by Altimetry
  - Estimation of combined principal components by least-squares solution:

$$dot_{res}(x, y, t) = \sum_{i=1}^n pc_{comb_i}(t) * eof_i(x, y)$$

- Reconstruction DOT by applying Principal Component Synthesis (PCS) based on estimated combined principal components, FESOM EOF and re-adding offset + annual signal → **cDOT**
- Deriving combined geostrophic currents by derivation of cDOT meshes → **cGC**

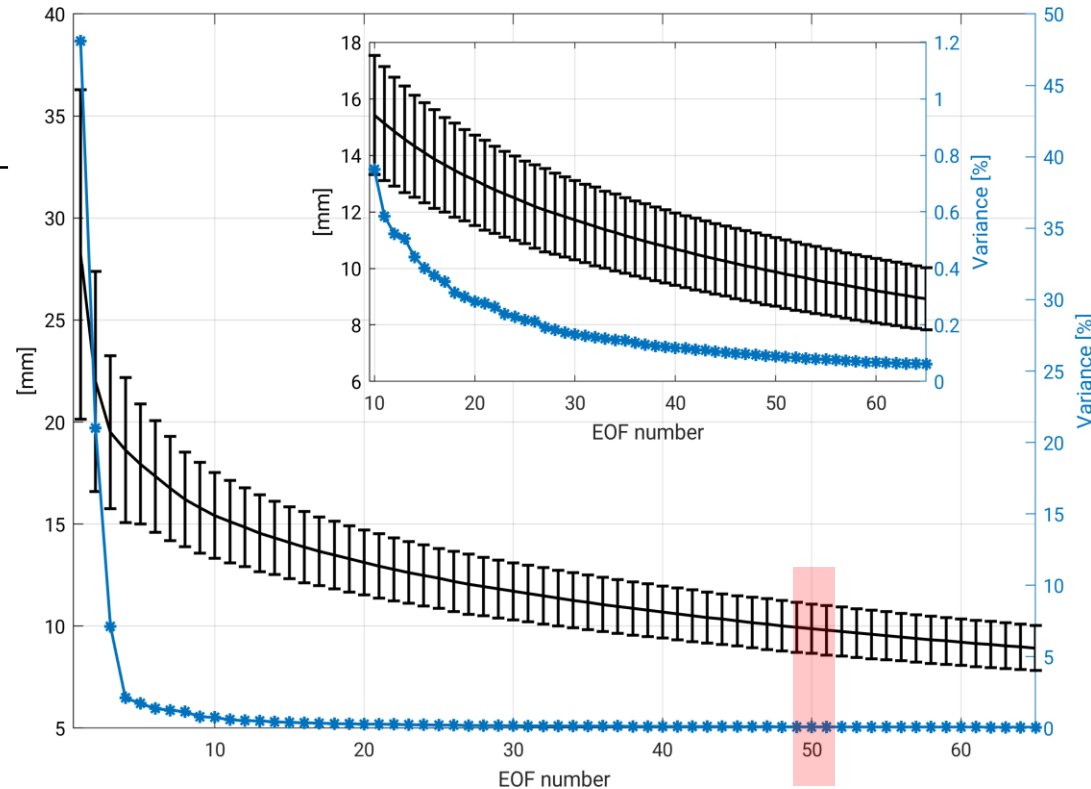


Yellow: Input, Green: auxiliary steps, Blue: Combination Steps (Müller et al. 2019)

# How many Modes do we need for combination?

- Experiment: Reconstruction of the input signal
- Root Mean Square Error of original minus reconstructed signal

$$\text{RMSE} = \sqrt{(\text{FESOM}_{\text{orig}} - \text{FESOM}_{\text{rec}})^2}$$

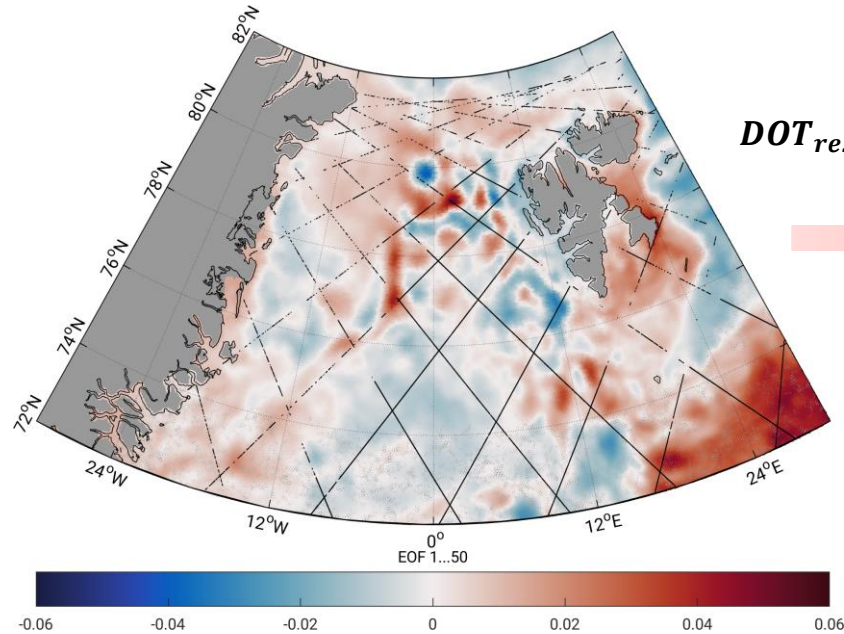


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**Contribution of one eigenvalue to the total variance (%)**

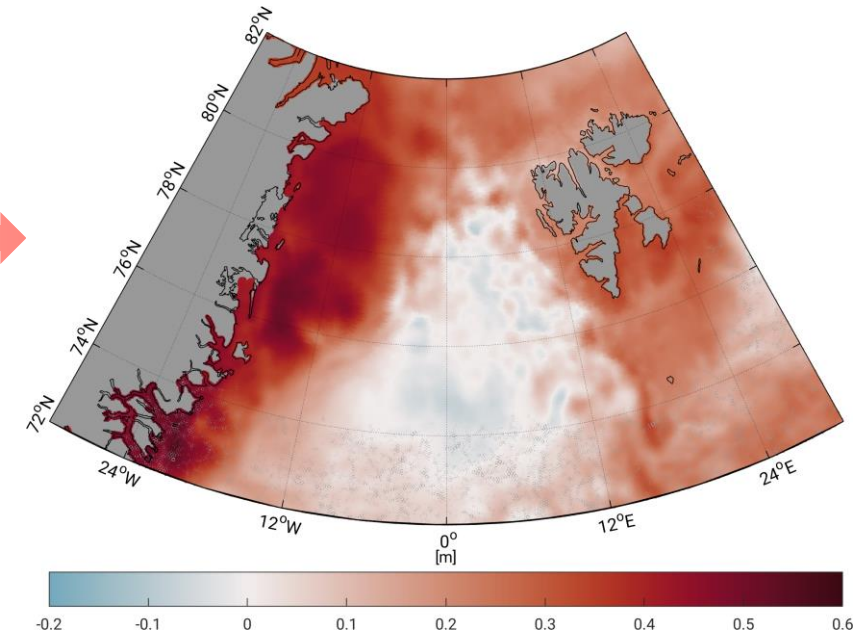
- Using 50 Modes → Mean Error <1cm (94% of total signal)

# Combination of estimated pc with FESOM EOF



$$DOT_{res}(x, y, t) = \sum_{i=1 \dots 50} pc_{comb_i}(t) * EOF_i(x, y)$$

- FESOM EOF
- Spatial resolution of FESOM



*FESOM  $\sum_1^{50} EOF$  and altimetry ground track pattern (3-days are shown) in 2003-01-12*

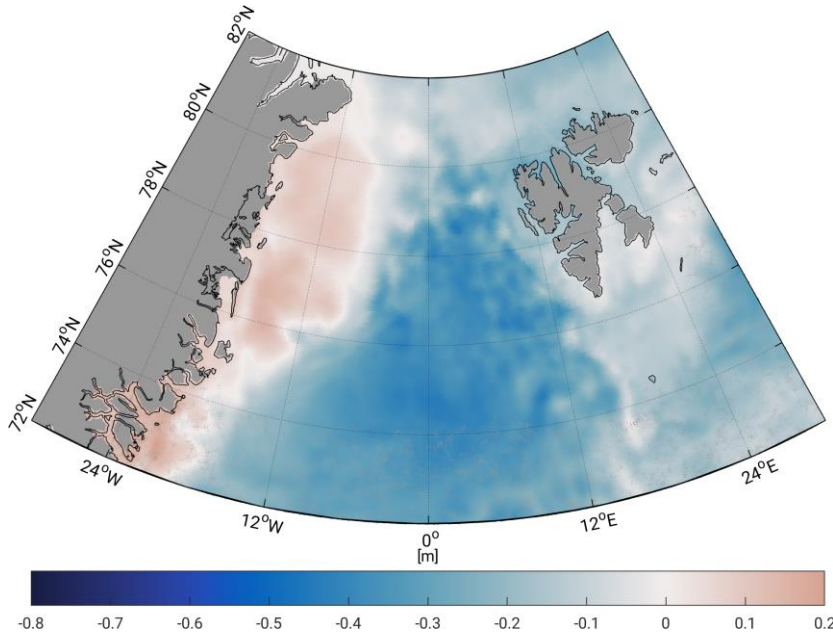
*Residual DOT heights 2003-01-12*

- Estimation of 50 combined principal components  $pc_{1 \dots 50}$  based on 50 eof and 9-day altimetry residual DOT along-track heights

- Residual DOT heights show spatial resolution of model → no data gaps
- Time stamp  $t_j \pm t_{4.5d}$
- Next step: Re-addition of annual signal and constant offset



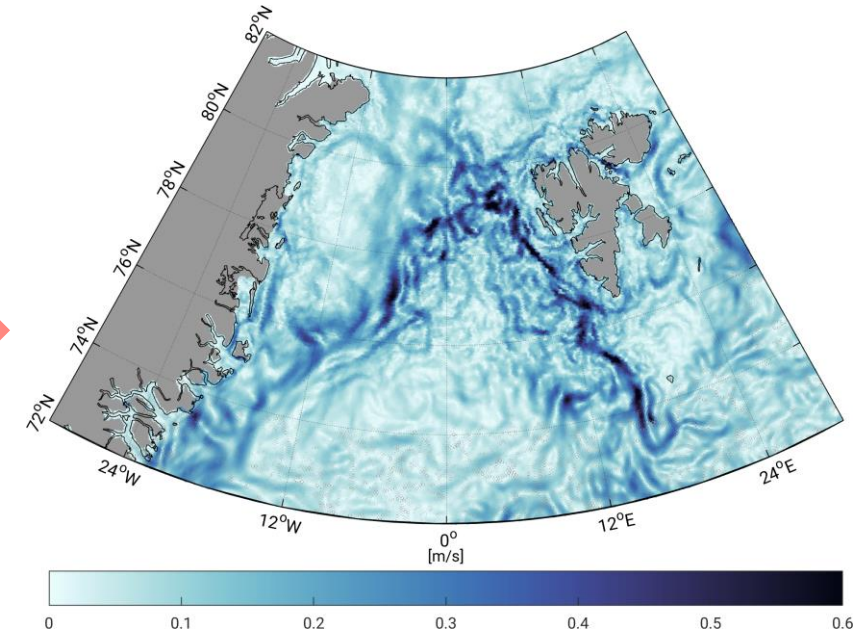
# Combined DOT and Geostrophic Currents



Combined DOT 2003-01-12

Adding:

- Coriolis force
- Gravity force
- Horizontal pressure gradient



Combined absolute geostrophic velocity 2003-01-12

- Combined DOT with altimetry height reference and altimetry-derived annual oscillation
  - Spatial resolution: up to <1km
  - Temporal resolution: daily

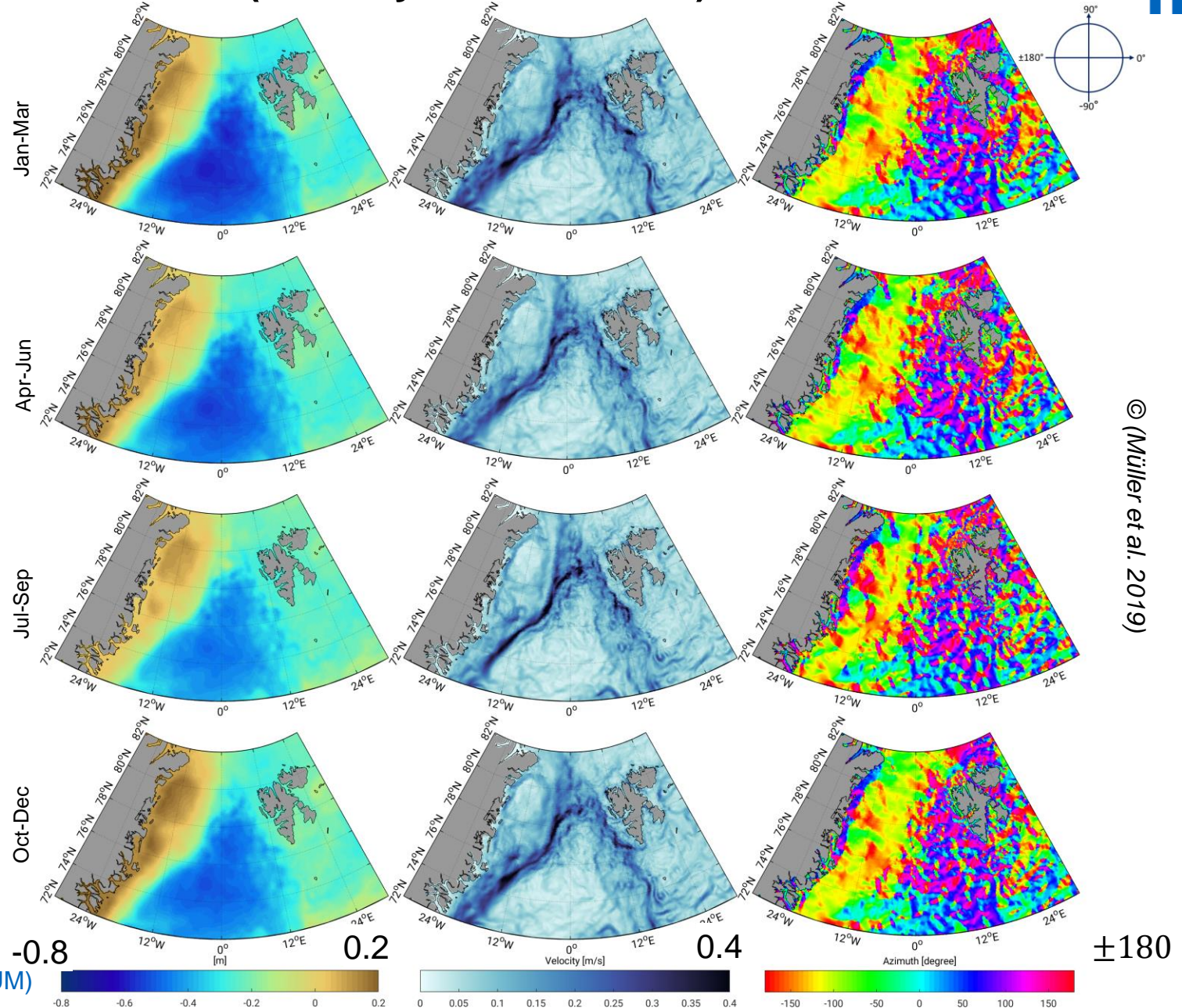
$$u = -\frac{g}{f} * \frac{\partial DOT}{\partial y}$$

$$v = \frac{g}{f} * \frac{\partial DOT}{\partial x}$$

- Derivation of DOT to compute geostrophic components u (zonal) and v (meridional) via Finite-Element-Method
- Computation of flow direction, abs. velocity and eddy-kinetic-energy

# Combined DOT and Geostrophic Currents (Velocity and Direction) 1995 - 2012

- Plot shows combination products (From left to right: DOT heights, abs. geostrophic surface velocity and direction)
- Major current systems (West-Spitsbergen and East-Greenland Current) and East-Greenland Coastal Current are visible
- Seasonal variations are observable
  - Velocity maximum in Winter months
  - Anti-Phase of DOT heights in Greenland Shelf vs. Greenland Deep-Basin
- Data freely available on PANGAEA: <https://doi.pangaea.de/10.1594/PANGAEA.900691>

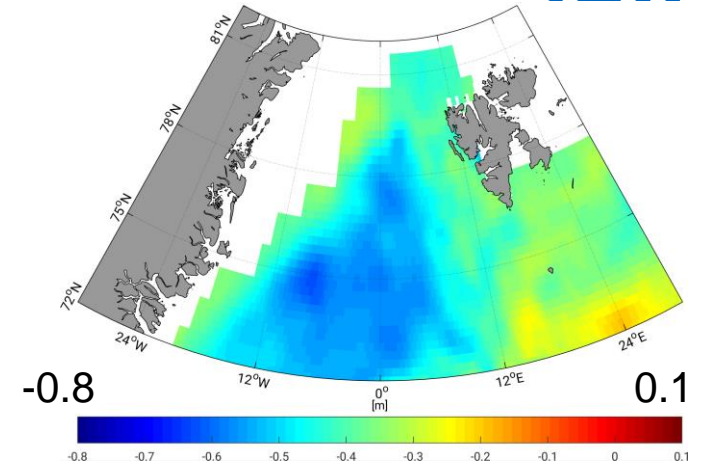


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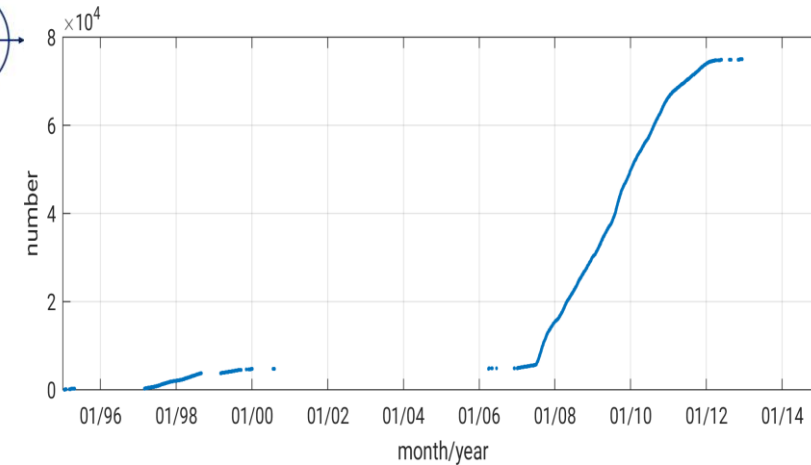
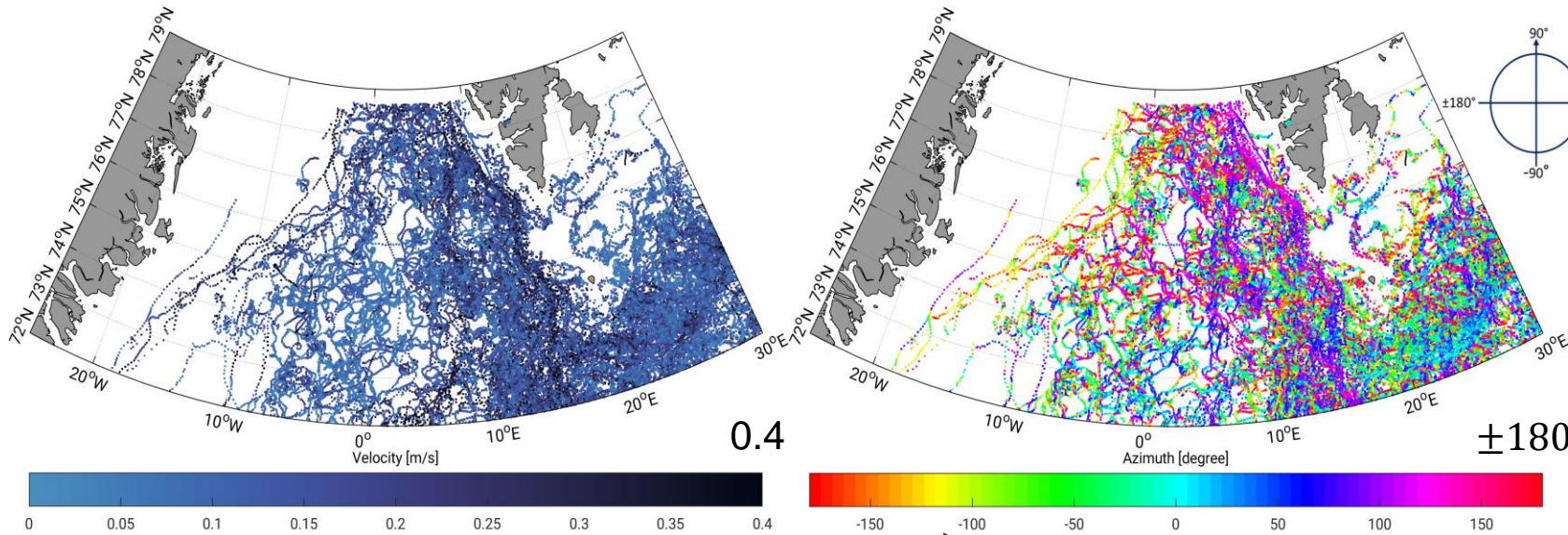


# Validation of combination products

- Point-wise and bin-wise comparison with to geostrophic surface velocities reduced surface drifter observations (Drifter Dataset: CMEMS, Rio and Etienne (2018))
- Requires: A-geostrophic velocity fields (i.e. Stokes Drift, Ekman-Drift, local wind slippage)
- Reduced availability of in-situ data – no velocity data in sea-ice regions (no validation possibilities for East-Greenland Current, East-Greenland Coastal Current)
- Comparison with altimetry only derived geostrophic velocity fields for Absolute Dynamic Topography grids (ADT, provided by CMEMS)



Absolute Dynamic Topography (CMEMS, Pujol & Mertz, 2019)

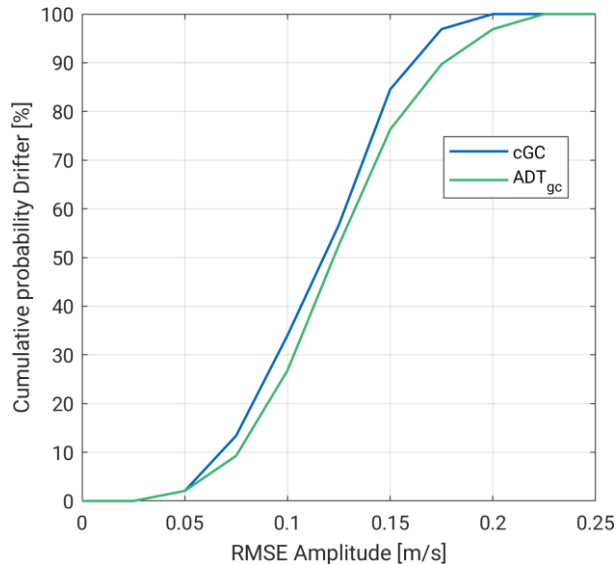
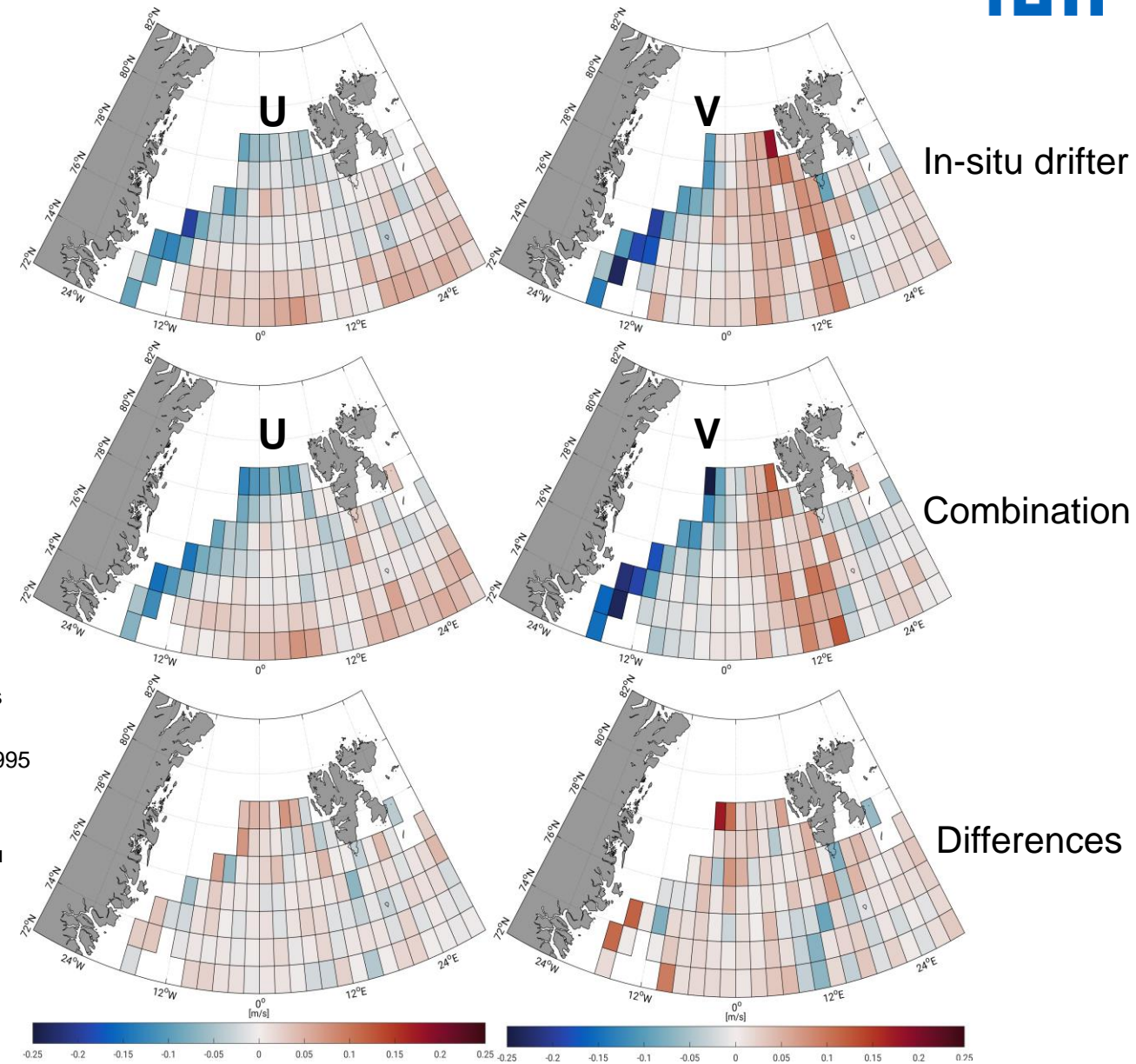


Comparison with to geostrophic velocities reduced Surface Drifter Measurements (from left: abs. velocity, direction, cumulative number of available drifter observations (Müller et al. 2019))



# Validation of combination products

- Bin-wise comparison shows small differences in the investigation area
- Differences agree well with spatial patterns of the velocity components
- Drifter and the cGC describe same amplitude and flow direction in most of the bins
- Meridional component shows bigger differences than the zonal component.
- The combination shows smaller RMSE residuals.
  - 35% of the combined residuals are smaller than 0.1 m/s vs. 27% of altimetry only geostrophic abs.velocity

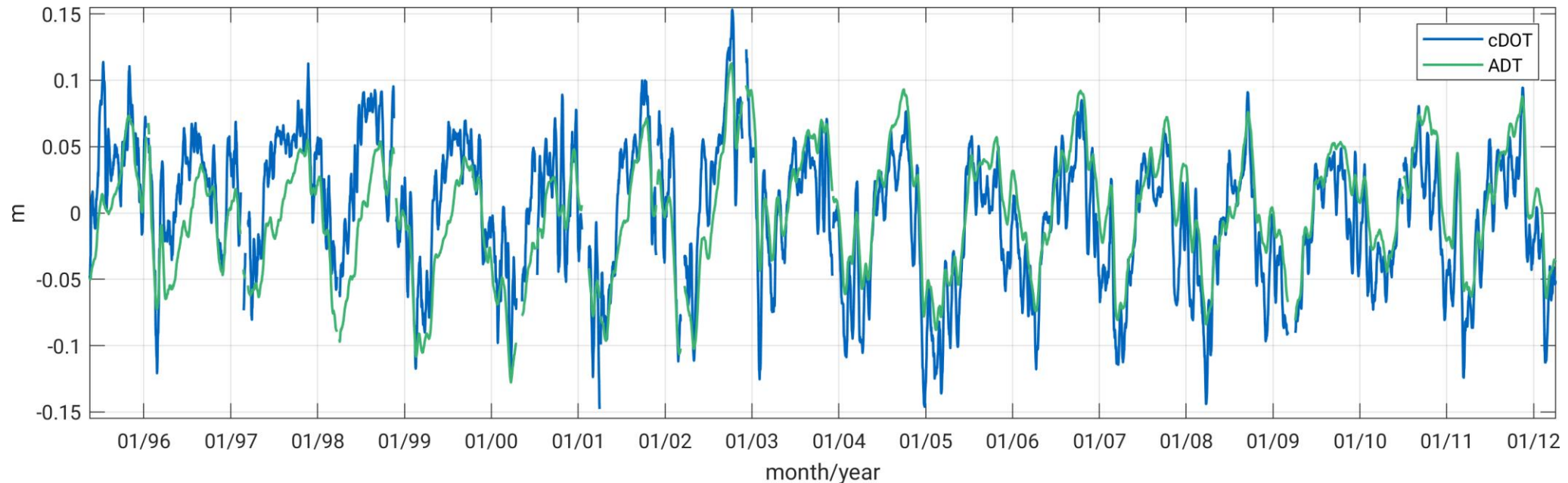


←RMSE of geostrophic absolute velocity between drifter observations and to the trajectories interpolated combined and ADT datasets from 1995 to 2012. (Müller et al. 2019)

→ Temporal averaged geostrophic u and v components of drifter observations, combined dataset and differences respectively, binned in 2°x1°(lon,lat) boxes (1995-2012). See Müller et al. 2019

# Validation of combination products

- Comparison of mean reduced time series of ADT and Combination in the northern Nordic Seas
- Both signals display high-frequent patterns
- Comparison with ADT time series shows the same seasonal signal, but higher variabilities in combined DOT
- Positive correlation between both signals >80%



Mean-reduced time series of daily and spatial averaged altimetry-only ADT grids and to the ADT grid nodes interpolated combined DOT (cDOT) limited to ice-free regions in the northern Nordis seas (Müller et al. 2019)

The work has been published in Copernicus journals, *The Cryosphere* and *Earth System Science Data*

### 1. Comparison of datasets:

*Müller F. L., Wekerle C., Dettmering D., Passaro M., Bosch W., Seitz F.*: **Dynamic ocean topography of the northern Nordic seas: a comparison between satellite altimetry and ocean modeling.** *The Cryosphere*, 13, 611–626, [10.5194/tc-13-611-2019](https://doi.org/10.5194/tc-13-611-2019), 2019 ([Open Access](#))

### 2. Combination of datasets:

*Müller F. L., Dettmering D., Wekerle C., Schwatke C., Passaro M., Bosch W., Seitz F.*: **Geostrophic currents in the northern Nordic Seas from a combination of multi-mission satellite altimetry and ocean modeling.** *Earth System Science Data*, 11(4), 1765-1781, [10.5194/essd-11-1765-2019](https://doi.org/10.5194/essd-11-1765-2019), 2019 ([Open Access](#))

### 3. PANGAEA link datasets:

*Müller F. L., Dettmering D., Wekerle C., Schwatke C., Bosch W., Seitz F.*: **Geostrophic Currents in the northern Nordic Seas - A Combined Dataset of Multi-Mission Satellite Altimetry and Ocean Modeling (data).** Deutsches Geodätisches Forschungsinstitut, München , [10.1594/PANGAEA.900691](https://doi.org/10.1594/PANGAEA.900691), 2019 ([Open Access](#))



### Comparison: DOT from altimetry vs. simulated differential water heights of FESOM

- Both datasets show good agreement in dominating oscillation periods
- A combination of both quantities is useful because of a general good agreement and to benefit from both datasets enabling the computation of a homogeneous DOT and geostrophic ocean surface circulation.

### Combination: high-frequent along-track altimetry observation and ocean model output

- Development of an innovative dataset based on a combination of height observations from satellite altimetry with spatial information provided by an ocean model (FESOM)
- Comprehensive variability analyses of geostrophic surface currents not only in open ocean regions, but also in the sea-ice area is possible

## Further References:

### FESOM Model:

- Wang, Q., Danilov, S., Sidorenko, D., Timmermann, R., Wekerle, C., Wang, X., Jung, T., and Schröter, J.: **The Finite Element Sea Ice-Ocean Model (FESOM) v.1.4: formulation of an ocean general circulation model**, Geosci. Model Dev., 7, 663–693, <https://doi.org/10.5194/gmd-7-663-2014> , 2014.
- Wekerle, C., Wang, Q., von Appen, W.-J., Danilov, S., Schourup-Kristensen, V., and Jung, T.: **Eddy-Resolving Simulation of the Atlantic Water Circulation in the Fram Strait With Focus on the Seasonal Cycle**, J. Geophys. Res. Oceans, <https://doi.org/10.1002/2017JC012974> ,25 2017.

### Comparison dataset:

- Rio, M.-H. and Etienne, H.: **Copernicus in situ TAC, Global ocean delayed mode currents from drifting buoys**, Product User Manual - PUM, Report (technical document (specification, manual)), <https://doi.org/10.13155/41257> , CMEMS Product ID:INSITU\_GLO\_UV\_REP\_OBSERVATIONS\_013\_044, 2018
- Pujol, M. I. and Mertz, F.: **PRODUCT USER MANUAL For Sea Level SLA products, GLOBAL OCEAN GRIDDED L4 SEA SURFACE HEIGHTS AND DERIVED VARIABLES REPROCESSED (1993-ONGOING), 1.0**, [http://resources.marine.copernicus.35eu/?option=com\\_csw&view=details&product\\_id=SEALEVEL\\_GLO\\_PHY\\_L4\\_REP\\_OBSERVATIONS\\_008\\_047](http://resources.marine.copernicus.35eu/?option=com_csw&view=details&product_id=SEALEVEL_GLO_PHY_L4_REP_OBSERVATIONS_008_047) , CMEMS Product ID:SEALEVEL\_GLO\_PHY\_L4\_REP\_OBSERVATIONS\_008\_047, 2019

### Altimetry dataset:

- Envisat (SGDR) and ERS-2 (REAPER-SGDR) altimetry data access is available from ESA (Envisat, <https://doi.org/10.5270/EN1-85m0a7b> , ESA (2018); ERS-2, <https://earth.esa.int/web/guest/-/radar-altimeter-reaper-sensor-geophysical-data-record-sgdr> , Brockley et al. (2017)).

## Further References:

*Förste C., Bruinsma S.L., Abrikosov O., Lemoine J.-M., Marty J. C., Flechtner F., Balmino F., Barthelmes F., and Biancale R.* **Eigen-6c4 the latest combined global gravity field model including goce data up to degree and order 2190 of gfz Potsdam and grgs toulouse.** GFZ Data Services, 2014

*Gruber T. and Willberg M.* **Signal and error assessment of GOCE-based high resolution gravity field models.** *Journal of Geodetic Science*, 9(1):71-86, January 2019. doi:10.1515/jogs-2019-0008. URL <https://doi.org/10.1515/jogs-2019-0008>

*Müller, F. L., Dettmering, D., Bosch, W., and Seitz, F.* **Monitoring the Arctic Seas: How Satellite Altimetry Can Be Used to Detect Open Water in Sea-Ice Regions,** *Remote Sensing*, 9, <https://doi.org/10.3390/rs9060551> , 2017.