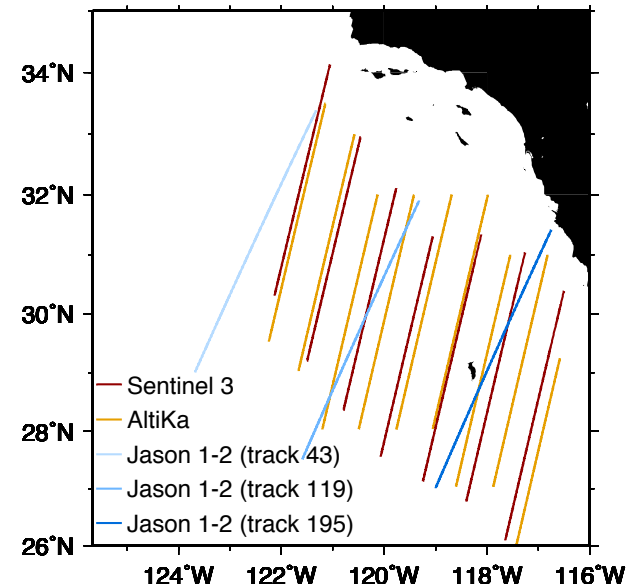


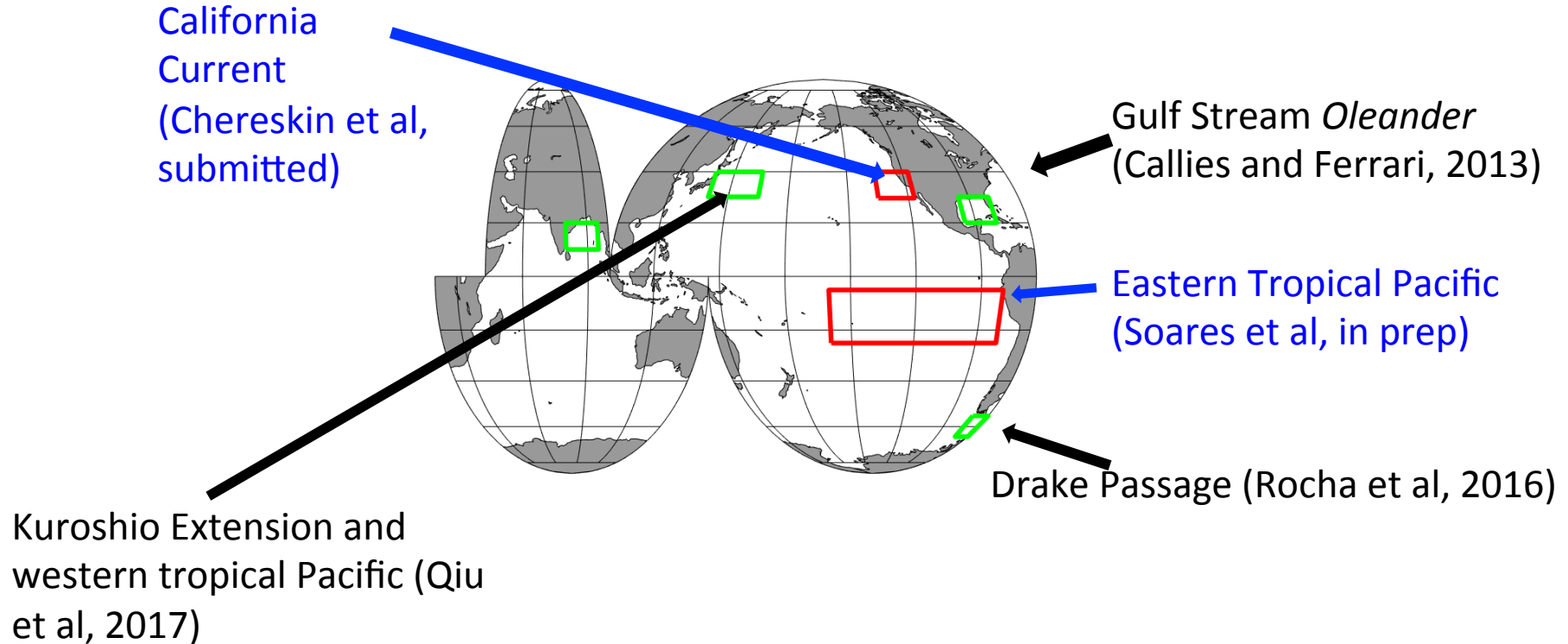
# Assessing high-wavenumber spectral slopes (and effective resolution) in new altimeter products

Sarah Gille<sup>1</sup>, Teresa Chereskin<sup>1</sup>, Jessica Masich<sup>1,2</sup>, Marcello Passaro<sup>3</sup>, Saulo Soares<sup>4</sup>

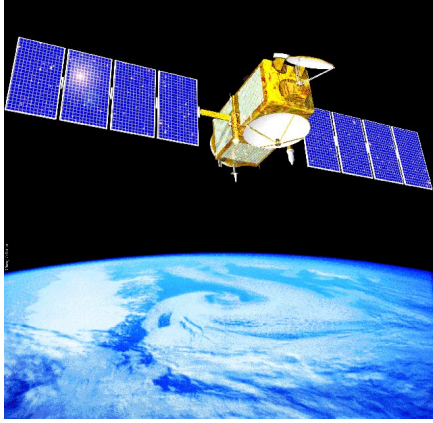
<sup>1</sup>Scripps institution of Oceanography, <sup>2</sup>NOAA/PMEL, <sup>3</sup>Deutsches Geodätisches Forschungsinstitut der Technischen Universität München, <sup>4</sup>University of Hawaii



# Acoustic Doppler Current Profiler data: High-wavenumber currents



# What can we learn from new altimetry?



Jason-1/2 ALES  
processing for  
coastal  
applications



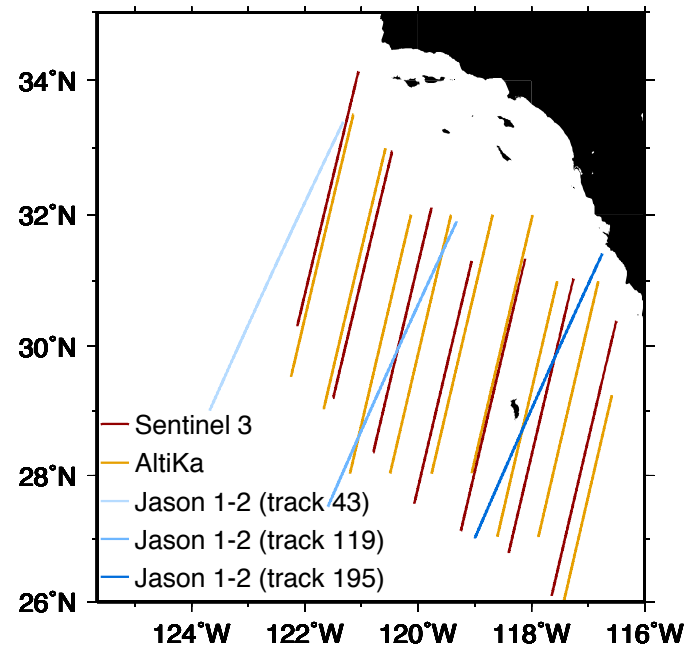
AltiKa 40-Hz  
data release



Sentinel-3 SAR  
mode

# Altimeter products

- **Sentinel 3**: SAR mode altimeter, Jan 2017 to May 2018, 20 cycles, 7 ground tracks
- **AltiKa**: October 2013 to May 2016, 25 cycles 9 ground tracks
- **Jason-1/2 ALES**: January 2002-August 2016, 557 cycles, 3 ground tracks



# Altimeter processing at high wavenumber

To minimize geoid contamination:

- Remove mean sea surface height from each satellite pass:  $\eta'(x)$
- Interpolate each pass to common latitude grid:  $\eta'(x_m)$
- Average over all passes to obtain mean:  $\langle \eta(x_m) \rangle$  (but don't use  $\eta'(x_m)$  for calculations, because interpolation is a smoothing operation)
- Interpolate mean back onto original data points:  $\langle \eta(x) \rangle$
- Subtract mean:  $\eta'(x) - \langle \eta(x) \rangle$

# Altimeter processing at high wavenumber

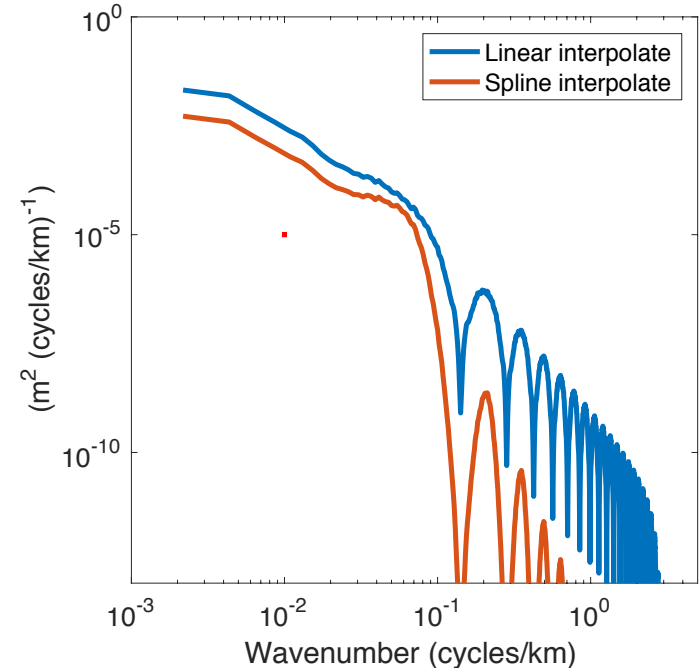
To minimize geoid contamination:

- Remove mean sea surface height from each satellite pass:  $\eta'(x)$
- Interpolate each pass to common latitude grid:  $\eta'(x_m)$
- Average over all passes to obtain mean:  $\langle \eta(x_m) \rangle$  (but don't use  $\eta'(x_m)$  for calculations, because interpolation is a smoothing operation)
- Interpolate mean back onto original data points:  $\langle \eta(x) \rangle$
- Subtract mean:  $\eta'(x) - \langle \eta(x) \rangle$

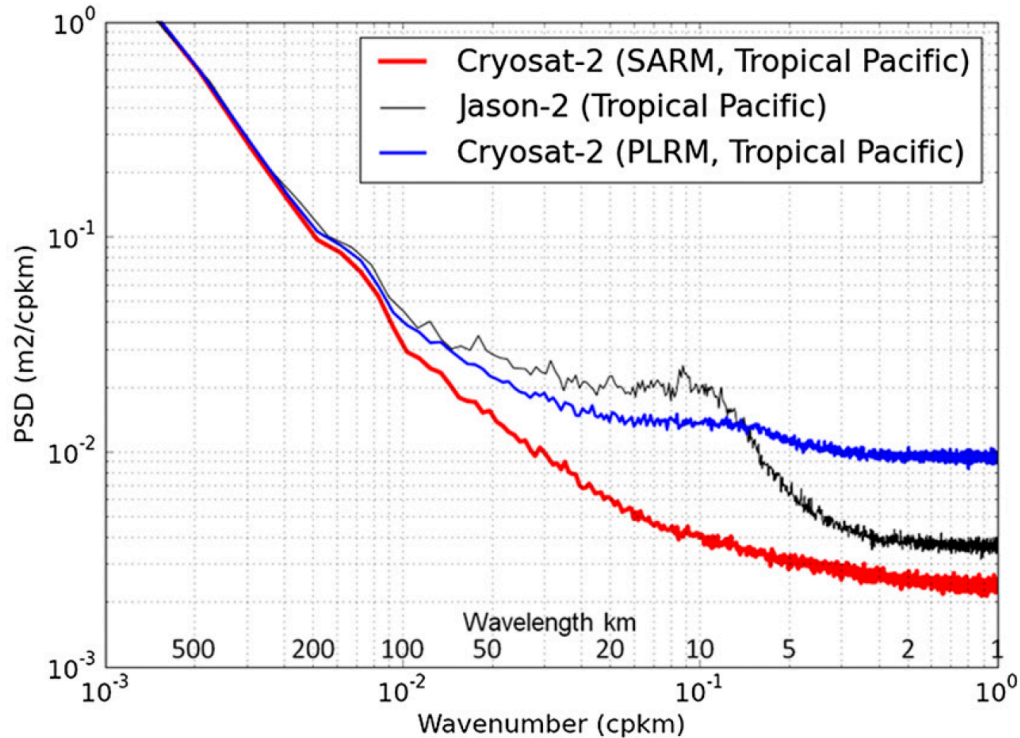
# Altimeter processing at high wavenumber

Environmental corrections available at 1 Hz

- Interpolate to 20 or 40 Hz
- Caution: if energetic relative to signal, then expect spectral ringing



# Anatomy of a wavenumber spectra

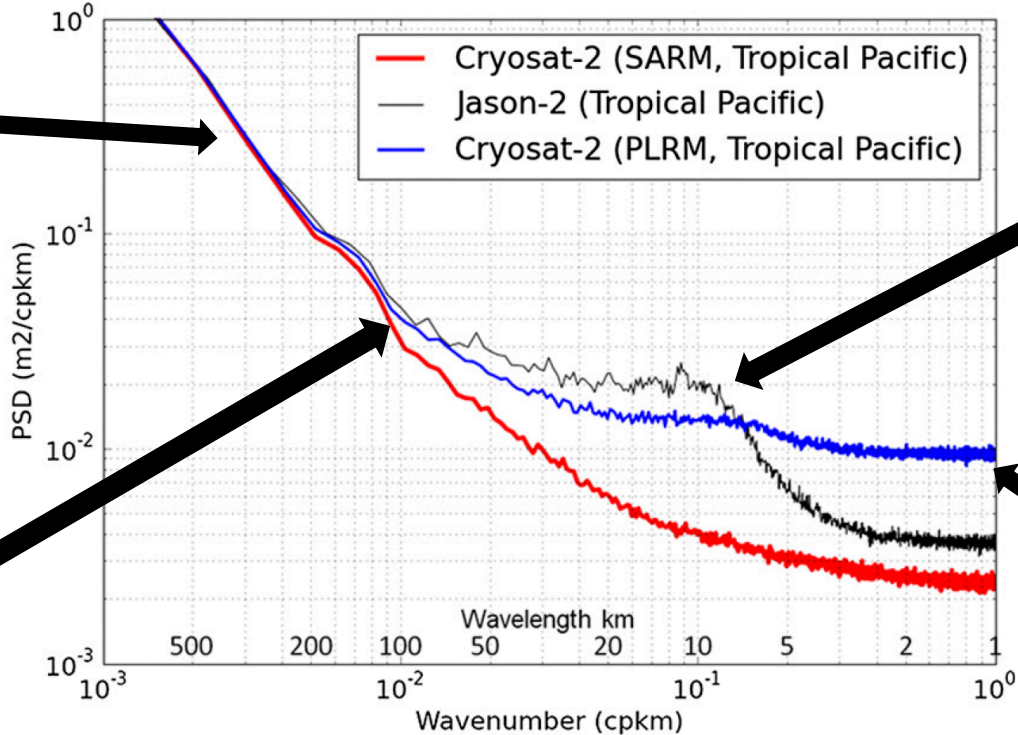




# Anatomy of a wavenumber spectra

Low wavenumbers:  
Geostrophic flow  
implies  $k^{-5}$   
spectrum. Should  
be well resolved by  
most altimeters

Transition from  
geostrophic  
(balanced) to  
ageostrophic.  
Spectral slope  
prediction  
unclear



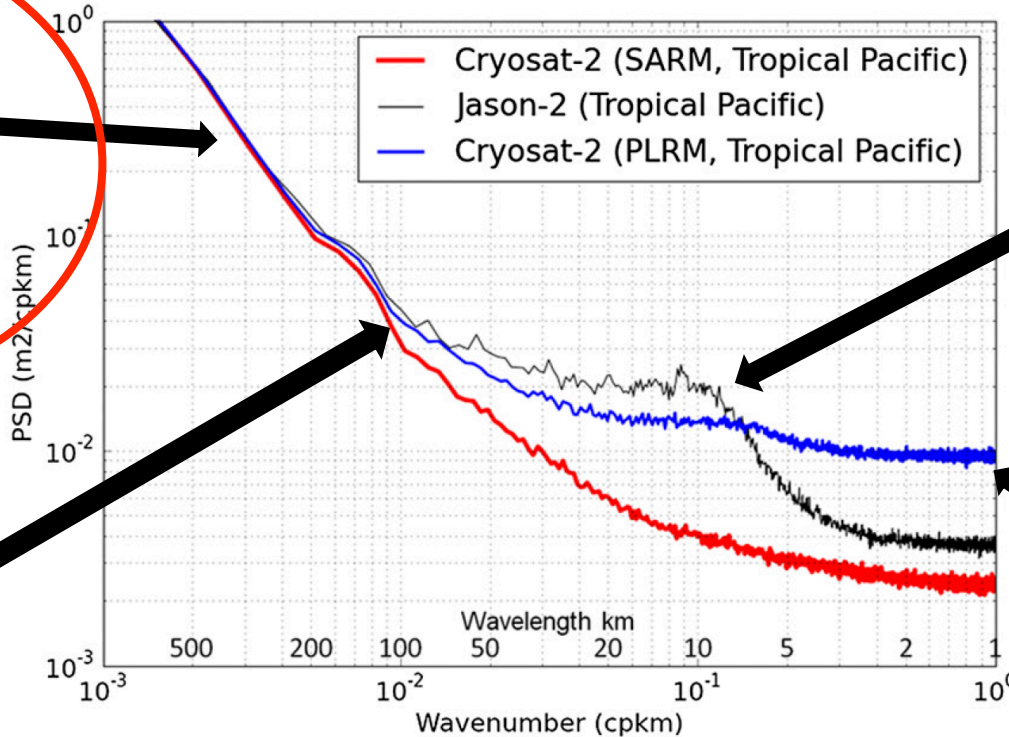
Spectral “bump”  
attributed to large  
satellite footprints

High wavenumbers:  
Noise floor  
determined by  
instrument

# Anatomy of a wavenumber spectra

Low wavenumbers:  
Geostrophic flow  
implies  $k^{-5}$   
spectrum. Should  
be well resolved by  
most altimeters

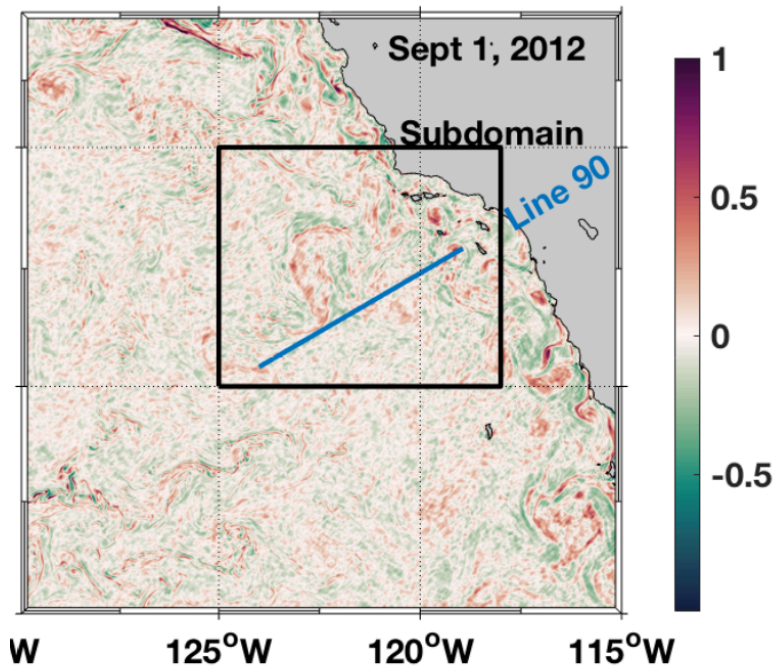
Transition from  
geostrophic  
(balanced) to  
ageostrophic.  
Spectral slope  
prediction  
unclear



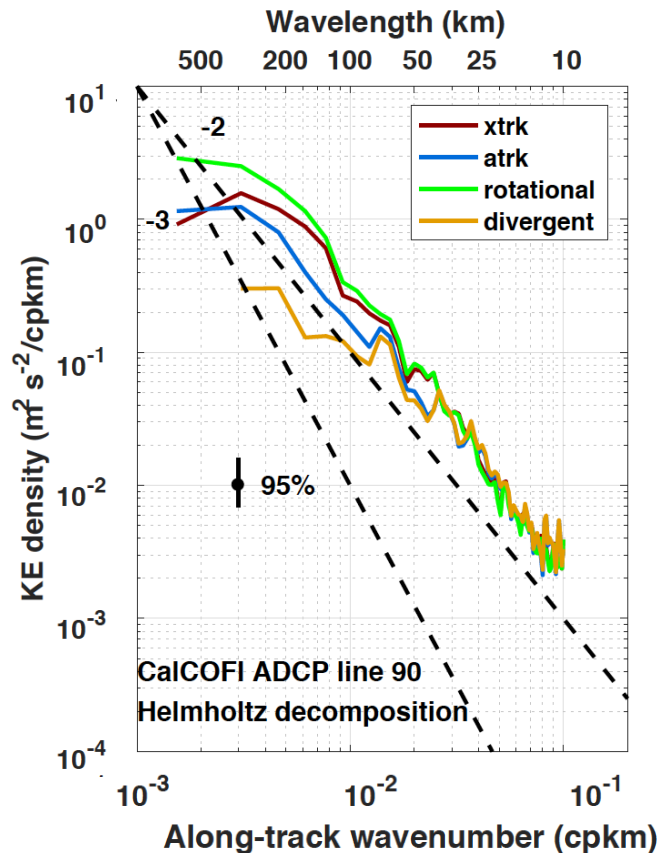
Spectral “bump”  
attributed to large  
satellite footprints

High wavenumbers:  
Noise floor  
determined by  
instrument

# Low wavenumbers: geostrophic balance



- Hanning window
- Fourier transform both components
- Helmholtz decomposition to separate rotational and divergent components

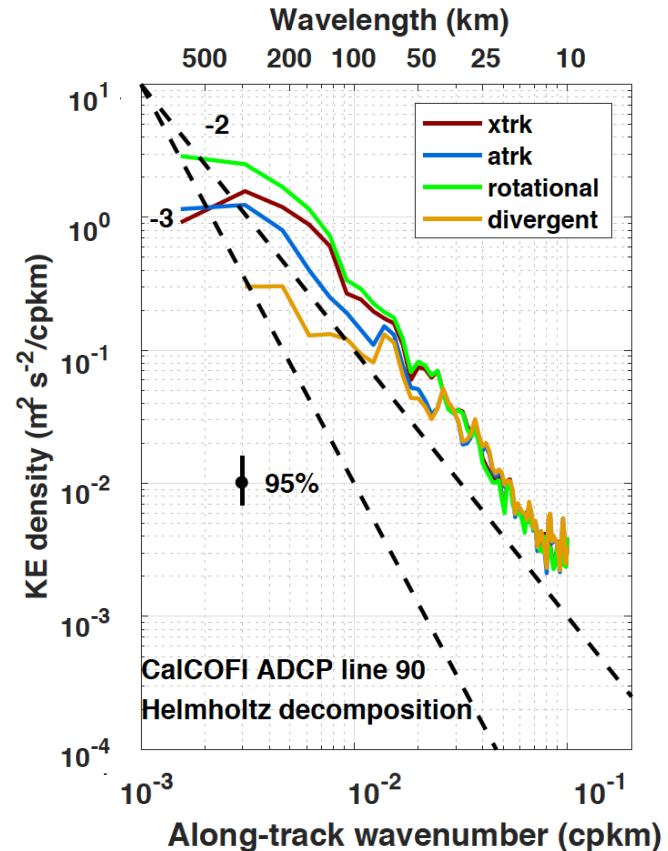


Acoustic Doppler Current Profiler data:  
1993-2004, 39 cruises

# Low wavenumbers: geostrophic balance

- **Rotational** (balanced, geostrophic) and **divergent** (ageostrophic) converge at 70 km.
- Scales larger than 70 expected to be in geostrophic balance.
- Slope  $k^{-2}$  for scales larger than 70 km.
- Geostrophy ( $u = -g/f \, d\eta/dy$ ) implies  $k^{-2}$  slope difference between velocity and ssh spectra

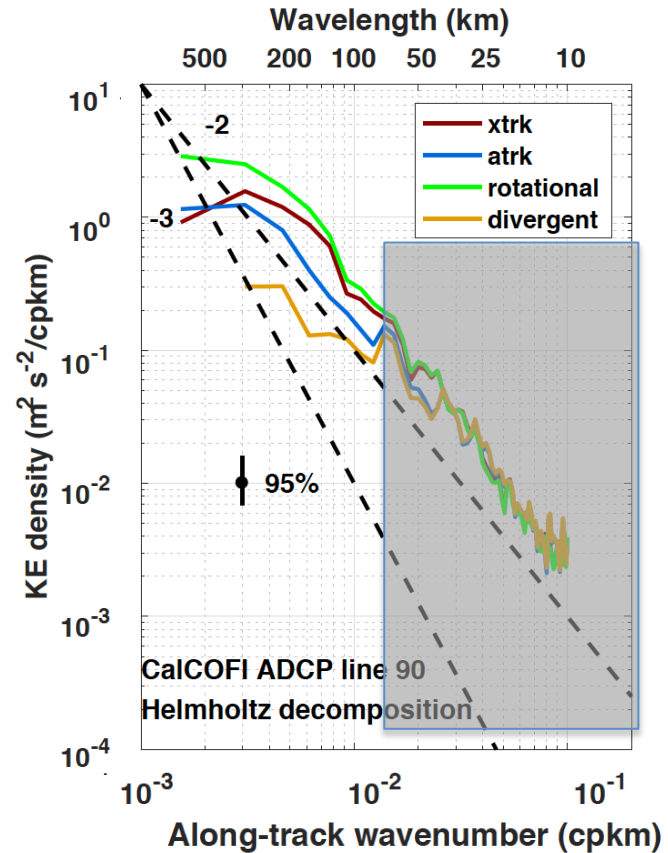
Chereskin et al, submitted, 2018



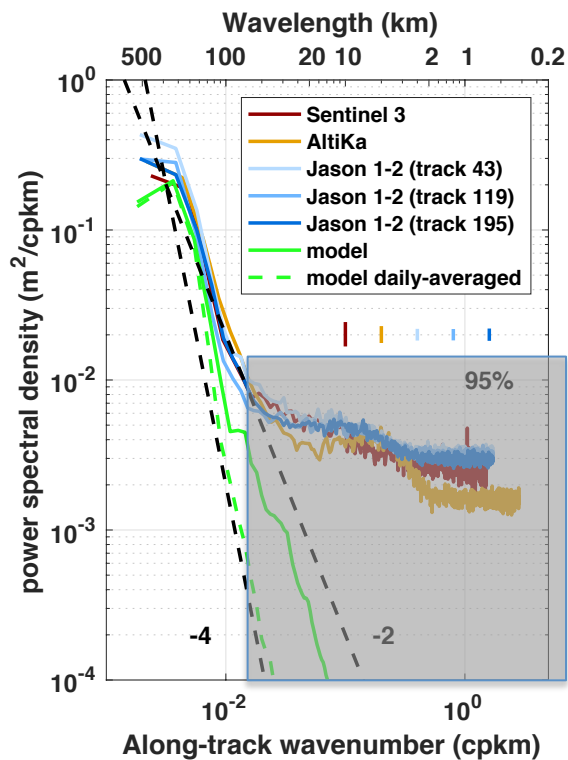
# Low wavenumbers: geostrophic balance

- **Rotational** (balanced, geostrophic) and **divergent** (ageostrophic) converge at 70 km.
- Scales larger than 70 expected to be in geostrophic balance.
- Slope  $k^{-2}$  for scales larger than 70 km.
- Geostrophy ( $u = -g/f \, d\eta/dy$ ) implies  $k^{-2}$  slope difference between velocity and ssh spectra

Chereskin et al, submitted, 2018



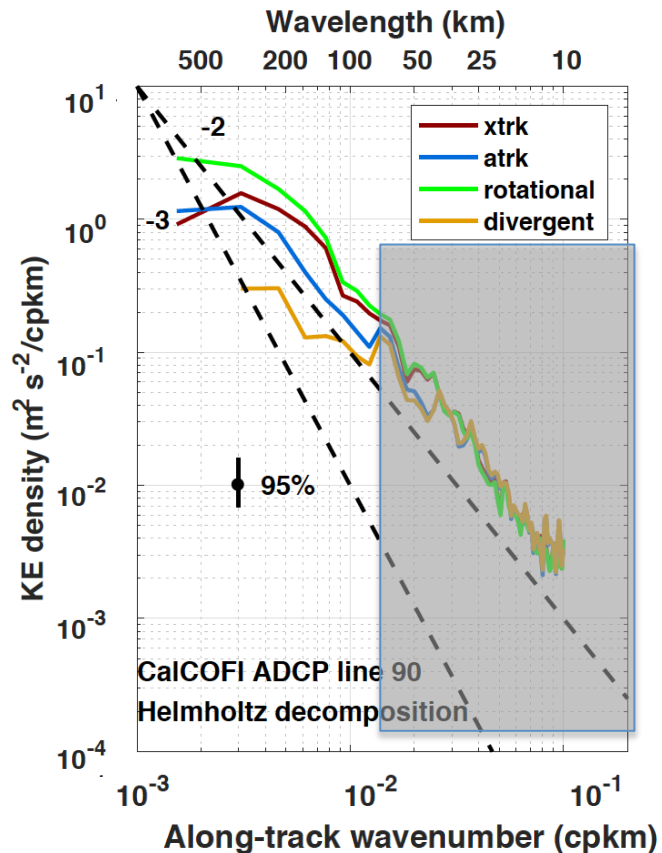
# Low wavenumbers: geostrophic balance



Geostrophic regime  
(scales  $> 70$  km):

Velocity spectra:  $k^{-2}$

Sea surface height:  $k^{-4}$

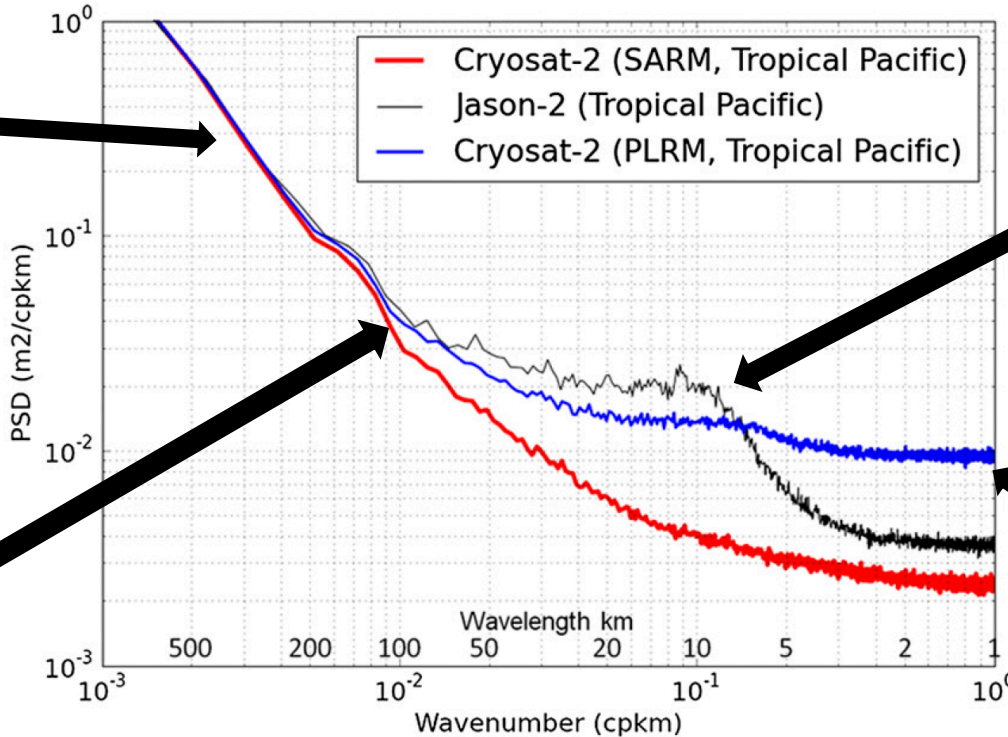




# Anatomy of a wavenumber spectra

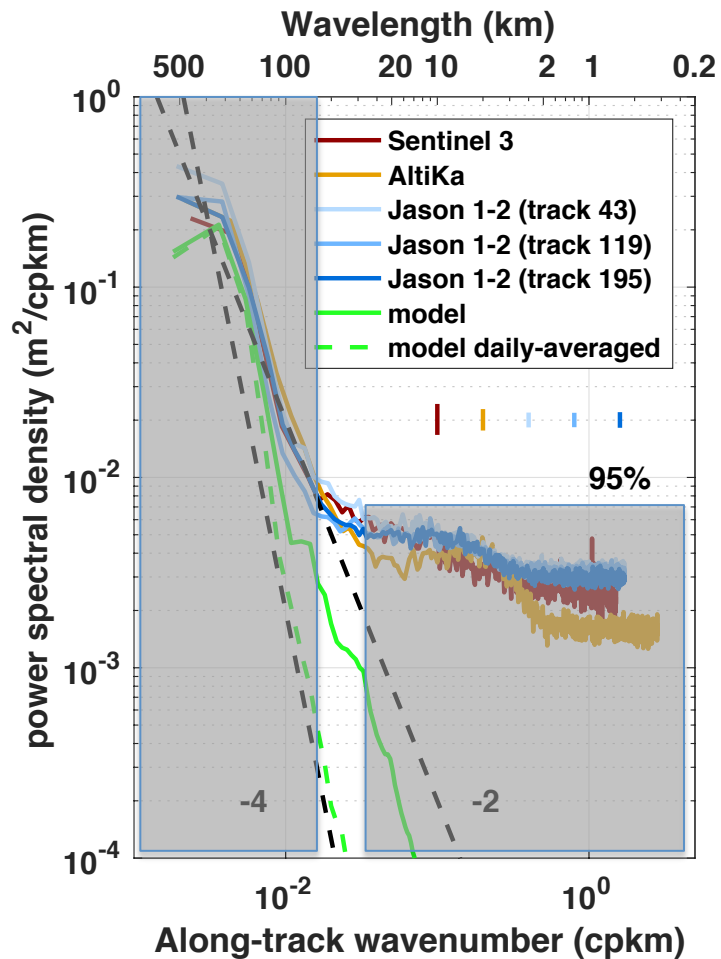
Low wavenumbers:  
Geostrophic flow  
implies  $k^{-4}$   
spectrum. Should  
be well resolved by  
most altimeters

Transition from  
geostrophic  
(balanced) to  
ageostrophic.  
Spectral slope  
prediction  
unclear



Spectral “bump”  
attributed to large  
satellite footprints

High wavenumbers:  
Noise floor  
determined by  
instrument



# Unbalanced motion: 70 to 30 km

Sea surface height spectra:  $k^{-2}$

Sentinel-3, Jason, and AltiKa agree within error bars

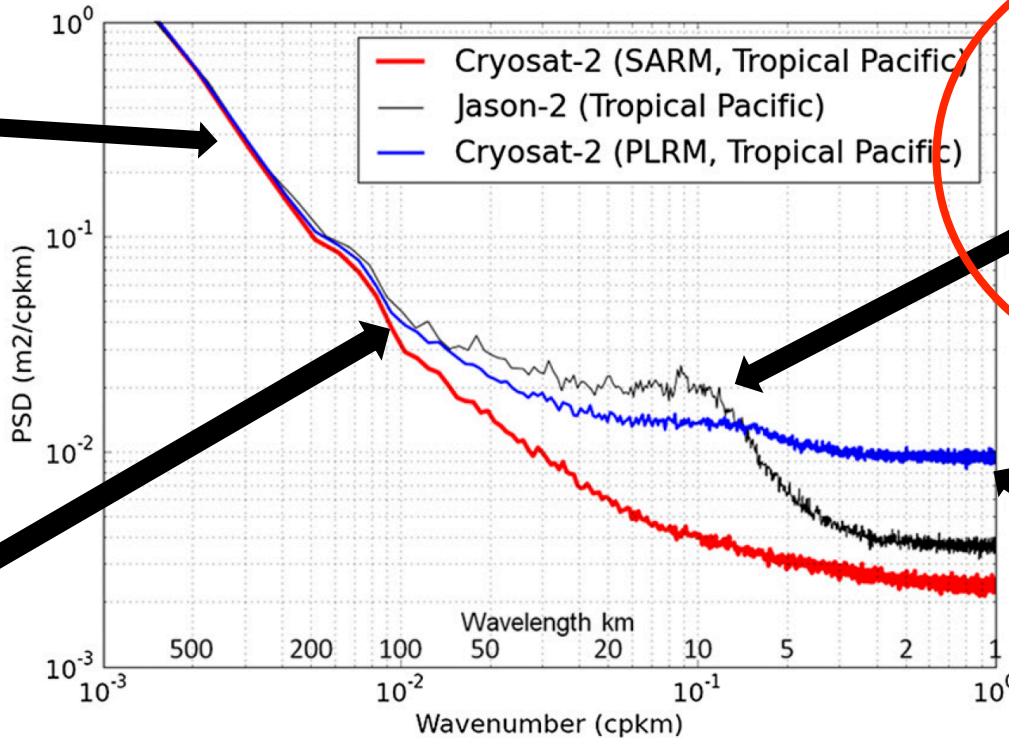
Does agreement tell us something about true sea surface height spectrum, or is it an artifact of noise floor?



# Anatomy of a wavenumber spectra

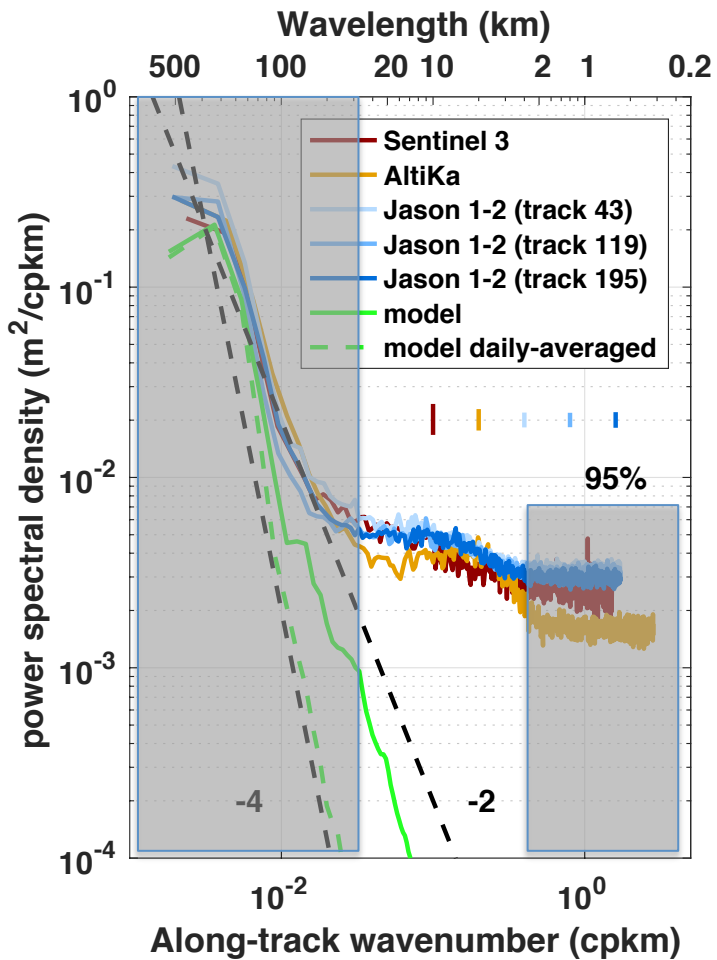
Low wavenumbers:  
Geostrophic flow  
implies  $k^{-4}$   
spectrum. Should  
be well resolved by  
most altimeters

Transition from  
geostrophic  
(balanced) to  
ageostrophic.  
Spectral slope  
prediction  
unclear



Spectral “bump”  
attributed to large  
satellite footprints

High wavenumbers:  
Noise floor  
determined by  
instrument



# Spectral bump regime: 30 to 3 km

Altimeters diverge

**AltiKa:** Classic spectral bump, consistent with preferential response to bright spots on ocean surface.

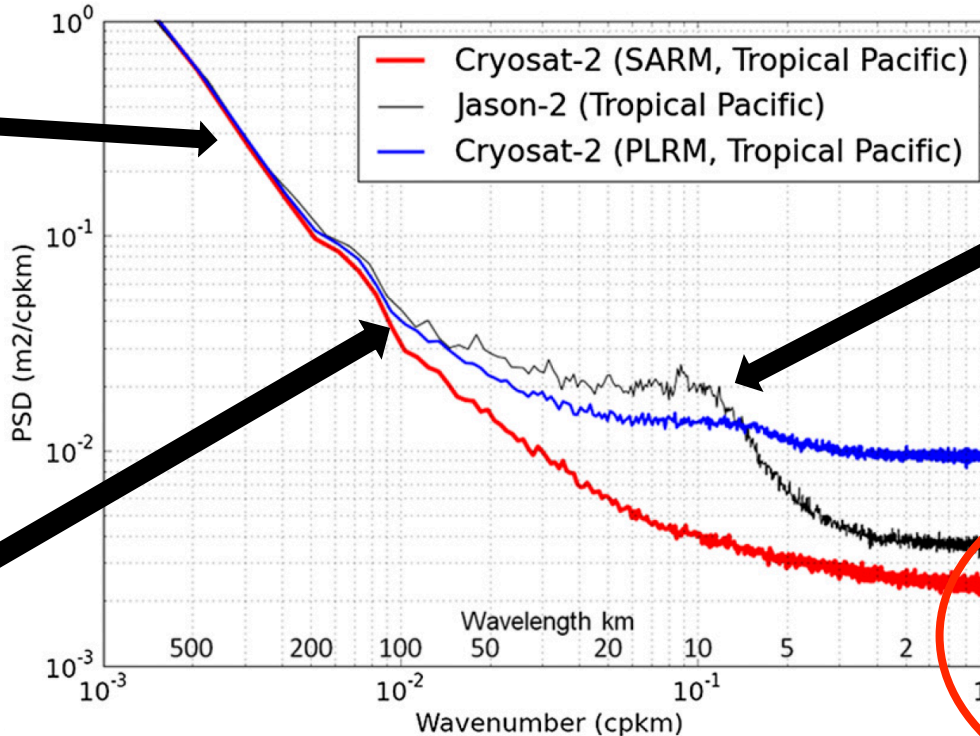
**Jason 1-2:** ALES processing reduces bump; step change in noise level.

**Sentinel-3:** SAR altimeter falls off gently. Short record implies noisy data that is not statistically different from Jason 1-2.

# Anatomy of a wavenumber spectra

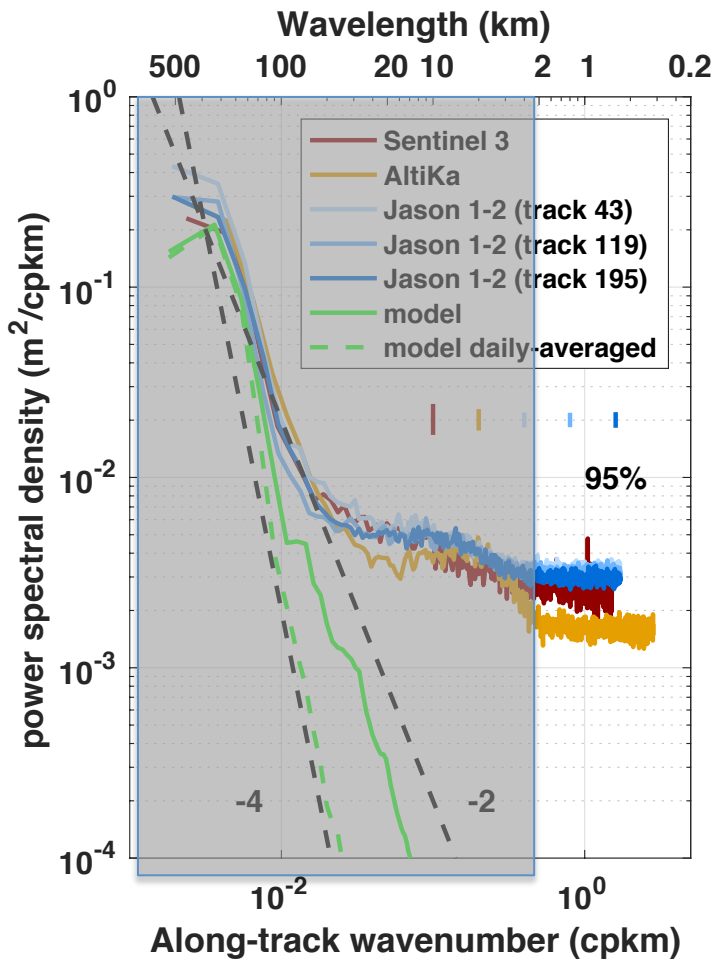
Low wavenumbers:  
Geostrophic flow  
implies  $k^{-4}$   
spectrum. Should  
be well resolved by  
most altimeters

Transition from  
geostrophic  
(balanced) to  
ageostrophic.  
Spectral slope  
prediction  
unclear



Spectral “bump”  
attributed to large  
satellite footprints

High wavenumbers:  
Noise floor  
determined by  
instrument



# White noise floor: Scales smaller than 2-3 km

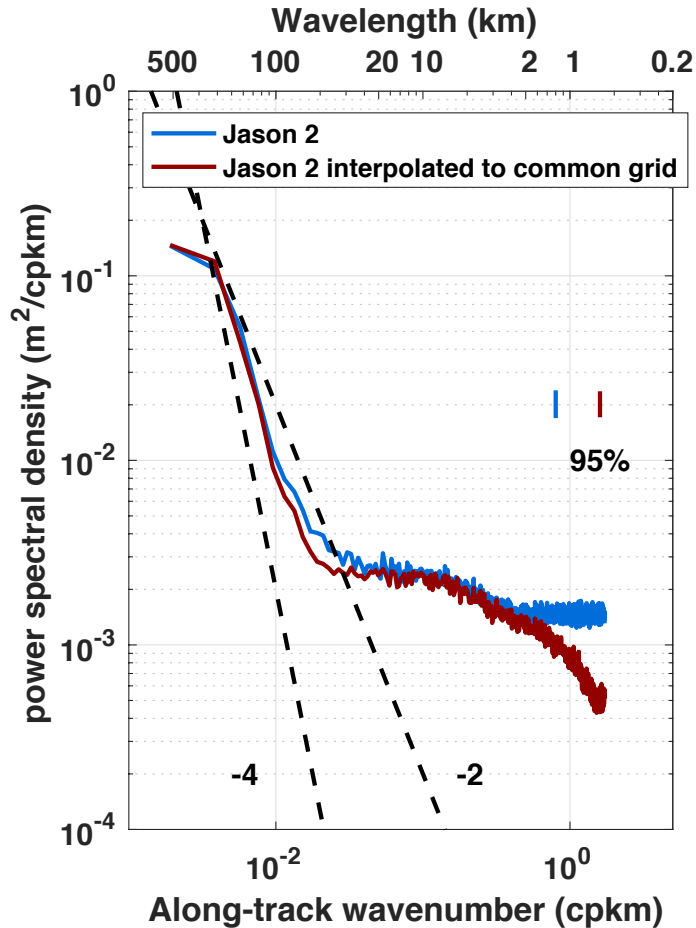
AltiKa: Lowest noise levels

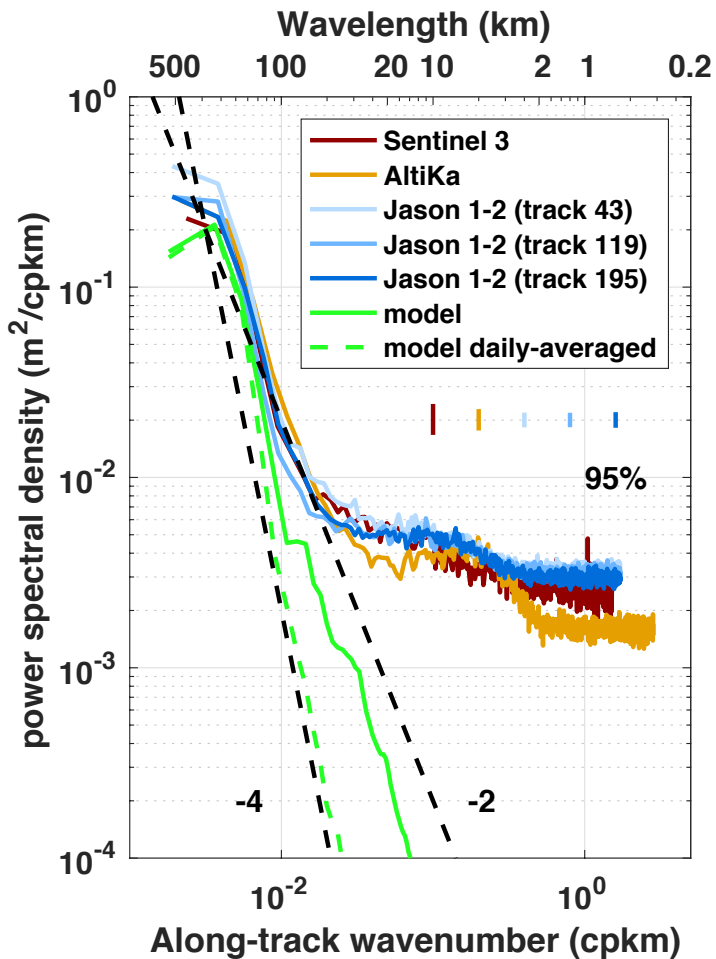
Jason 1-2: Highest noise

Sentinel-3: White noise, consistent with low significant wave height of region. Elsewhere Sentinel-3 has shown red spectra at high wavenumbers.

# White noise floor not a foregone conclusion

- Recall: Interpolation acts as a low-pass filter
- Computing spectra from interpolated data  $\eta'(x_m) - \langle \eta(x_m) \rangle$  leads to red spectrum at high wavenumbers





# Conclusions

- Sentinel 3, Jason-1/2 (ALES), AltiKa consistent for geostrophic regime and imbalanced (in 70-30 km)
- Sentinel 3 has no spectral bump but otherwise similar to Jason-1/2
- High-frequency noise floors: white in all cases for California Current.