Multi-scale model of the ionosphere from the combination of modern space-geodetic satellite techniques

Urs Hugentobler¹, Michael Schmidt², Norbert Jakowski³, Denise Dettmering³, M. Mainul Hoque⁴, Marco Limberger⁵, Wenjing Liang⁵, Volker Wilken³

¹ Technische Universität München (TUM), Institut für Astronomische und Physikalische Geodäsie (IAPG), Munich, Germany, urs.hugentobler@pv.tu-muenchen.de
² Deutsches Geodätisches Forschungs Institut (DGF), Munich, Germany, schmidt@dgi.badw.de
³ Deutsches Zentrum für Luft- und Raumfahrt (DLR), Institut für Kommunikation und Navigation, Neustrelitz, Germany, Norbert.Jakowski@dlr.de

Project overview
Near real-time high resolution and high precision ionosphere models are used for a large number of applications e.g. in navigation, positioning, telecommunications or astronautics. Today, these ionosphere models are mostly empirical, relying on extensive pure mathematical approaches. However, the complex phenomena within the ionosphere can only be understood and modeled when taking into account the physics governing the phenomena.
Here we present the basic structure of a model for the electron density of the ionosphere, which is developed by a cooperation of the German Geodetic Research Institute (DGFI), the Institute of Astronomical and Physical Geodesy (IAPG) of the Technical University Munich (TUM) and the German Aerospace Center (DLR), Neustrelitz.

The main features of the project are:
1. the consideration of physics-motivated modeling approaches, which are introduced in the multi-dimensional ionosphere model by means of appropriate mathematical base functions,
2. the estimation of the model parameters from the combination of various space-geodetic techniques, such as terrestrial and space-based GPS observations, altimetry and/or VLIB as well as
3. the transformation of the results into a multi-scale representation, which allows both an effective data compression necessary for handling the huge ionosphere data sets and near real-time applications as well as the identification of physical phenomena at different spatial and temporal scales.

For testing the procedure, the model will be applied to an appropriate region in South America, which covers relevant ionospheric processes and phenomena such as the Equatorial Anomaly.

The project structure is given by the following flowchart where the boxes symbolize the workpackages (WP). More information on the selected WP is given on the right.

Data (WP 10)
For this project, a database consisting of observations from various techniques will be established. Beside GNSS data of the IGS and SIRGAS network stations, dual-frequency altimetry observations, e.g., derived from Jason-1 and Jason-2, are included to close measurement gaps over the oceans. To overcome the insensitivity of ground-based GNSS to the radial geometry, radio occultation measurements to Low-Earth-Orbiting (LEO) satellites like CHAMP, GRACE and COSMIC are considered. The suitability of further techniques such as VLBI, DORIS or the usage of ionosonde data is to be analyzed.

Physical model part (WP 30)
The Chapman layer function is very efficient for describing the vertical structure of the electron density. It is a physics-motivated function depending on height which means that its parameters have a physical meaning. In this project, the height dependency of the electron density will be modeled by combining a F2-Chapman layer and a plasmashere profile, i.e.

\[ N_e(h) = N_e^\infty + N_e^H \]  

where the Chapman layer for the F2 layer reads

\[ N_e^\infty(h) = N_e \exp \left[ 0.50(1 - z - \exp(-z)) \right] \]

\[ \text{with } z = k h \exp(-k h) \]

The plasmashere profile is given by

\[ N_e^H(h) = N_e K \exp \left[ - \frac{h^2}{H_e^2} \right] \]

\[ \text{for } \frac{h}{H_e^2} < 1 \]

where \( N_e^H \) and \( K \) are the F2-peak electron density and peak height, \( H_e^2 \) is the F2-scale height, \( N_e^\infty \) and \( H_e^\infty \) are the plasmashere basis density and scale height.

Each of the five unknown target parameters

\[ N_e^\infty, \frac{N_e}{H_e^2}, \frac{K}{N_e} \]

can be modeled in three-dimensional (3-D) series expansions depending on the spatial position and time (see WP 40).

Physical-mathematical modeling (WP 20, WP 40)
The space-geodetic techniques (WP 10) provide information on ionospheric parameters, e.g. a geometry-free GNSS observation yields the slant Total Electron Content (TSEC).
The TSEC is defined as the integral of the space- and time-dependent 4-D electron density \( N_e(h, \phi, \varphi, t) \) along the ray path between the satellite \( s \) and the receiver \( r \), i.e.

\[ \text{TSEC} \equiv \int N_e(h, \phi, \varphi, t) ds \]

where \( \phi, \varphi \) and \( t \) denote latitude, longitude and time.

Inserting Eq. (2) into Eq. (1) yields

\[ N_e(h) = N_e \exp \left[ 0.50(1 - z - \exp(-z)) \right] + N_e^\infty \]

The representation of the unknown Chapman parameter \( N_e^\infty \) reads

\[ N_e^\infty = N_e^\infty + \Delta N_e^\infty \]

As background model \( N_e^\infty \) we can choose e.g. IRI-2007. The correction part \( \Delta N_e \) is modeled by a series expansion

\[ \Delta N_e(\phi, \varphi, t) = \sum_{l=1}^{\infty} \sum_{m=-l}^{l} a_{l,m}^\infty (\phi^l \varphi^m) \]

in tensor products of three 1-D scaling functions \( q_l^m(\cdot) \) with initial unknown scaling coefficients \( a_{l,m}^\infty \).

For each sensitivity technique (GNSS, altimetry, radio occultation, etc.) or mission (JASON-1/2, Envisat, etc.), resp., denoted as group \( i \), we derive an observation equation for estimating the coefficients \( a_{l,m}^\infty \) of the B-spline model within an adjustment process (Gauss-Markov Model), i.e.

\[ y_{i,n} + \epsilon_{i,n} = D_{i,n} \theta_{i,n} + \nu_{i,n} \]

where \( y_{i,n} \) and \( \theta_{i,n} \) are the observation and the unknown scaling coefficients, \( \epsilon_{i,n} \) is the observation error, \( \nu_{i,n} \) and \( P_i \) are the unknown variance factor and the given positive definite weight matrix. The vector \( \theta_i \) consists of the unknown coefficients \( a_{l,m}^\infty \) and other auxiliary variables (DCBs, bias, etc.).

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