

Valence effect on the thermopower of Eu systems

U. Stockert^{1,*}, S. Seiro^{1,2}, N. Caroca-Canales,¹ E. Hassinger^{1,3} and C. Geibel¹

¹Max Planck Institute for Chemical Physics of Solids, Nöthnitzer Straße 40, D-01187 Dresden, Germany

²Leibniz IFW Dresden, Helmholtzstr. 20, D-01069 Dresden, Germany

³Technical University Munich, Physics Department, James-Franck-Str. 1, 85748 Garching, Germany



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We investigated the thermoelectric transport properties of EuNi_2P_2 and EuIr_2Si_2 to evaluate the relevance of Kondo interaction and valence fluctuations in these materials. While the thermal conductivities behave conventionally, the thermopower curves exhibit large values with pronounced maxima as typically observed in Ce- and Yb-based heavy-fermion materials. However, neither the positions of these maxima nor the absolute thermopower values at low temperature are in line with the heavy-fermion scenario and the moderately enhanced effective charge carrier masses. Instead, we may relate the thermopower in our materials to the temperature-dependent Eu valence by taking into account changes in the chemical potential. Our analysis confirms that valence fluctuations play an important role in EuNi_2P_2 and EuIr_2Si_2 .

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I. INTRODUCTION

Intermetallic Eu compounds exhibit various exotic phenomena such as noninteger valence, valence transitions, and valence fluctuations. They are related to the existence of two Eu configurations with relatively small energetic distance: the nonmagnetic one of $\text{Eu}^{3+}(4f^6)$ and the magnetic one of $\text{Eu}^{2+}(4f^7)$ [1]. A noninteger average Eu valence may arise due to several physical reasons: (1) A trivial case is mixed-valent systems containing more than one crystallographic Eu site with different valences as, for example, Eu_3O_4 [2]. More interesting are materials with a single Eu site: (2) Valence-fluctuating (VF) systems such as $\text{Eu}_4\text{Pd}_{29+x}\text{B}_8$ [3] exhibit a noninteger valence due to thermal fluctuations between the two close-lying integer Eu configurations. The respective characteristic energy scale is given by the valence fluctuation temperature T_{VF} . (3) In intermediate valent (IV) systems, a noninteger Eu valence originates from hybridization between the Eu $4f$ and the conduction electron states due to Kondo interaction, for example in $\text{EuCu}_2(\text{Ge}_{1-x}\text{Si}_x)_2$ close to $x = 0.7$ [4,5]. In this case, the characteristic energy scale corresponds to the Kondo temperature T_{K} . Unfortunately, notations in literature are not consistent, and frequently the terms *valence fluctuating*, *intermediate valent*, and sometimes even *mixed valent* are used as synonyms. The situation is also complicated by the fact that more than one effect may be relevant in a material. For example, the two distinct Eu

configurations of a VF material usually also experience some energetic broadening due to interactions with the conduction electron states. Another possibility are mixed-valent systems with valence fluctuations, which may even be site dependent as discussed for $\text{Eu}_3\text{Pd}_{20}\text{Ge}_6$ [6].

EuNi_2P_2 and EuIr_2Si_2 have been classified as systems with VF or IV character. They exhibit a strongly temperature-dependent Eu valence ν that remains fractional down to lowest temperature T as revealed by Mössbauer spectroscopy [7,8]. Both materials have moderately enhanced effective charge carrier masses indicative of significant hybridization between Eu $4f$ and conduction electron states [9–12]. Recently, EuNi_2P_2 and EuIr_2Si_2 attracted considerable interest due to the question of how this hybridization, which is usually observed in Ce and Yb-based Kondo systems, is related to the fluctuating Eu valence [11,13–15].

In fact, some of the low-temperature properties of EuNi_2P_2 and EuIr_2Si_2 can be explained in the framework of a simple model for VF materials: the interconfiguration fluctuation model [16,17]. In its simplest form, it considers Eu^{2+} and Eu^{3+} states that are close in energy. A phenomenological spin-fluctuation energy is introduced to also account for interactions with conduction electron states. The model yields a temperature-dependent effective Eu valence via thermal excitations from the low-energy Eu^{3+} into the higher Eu^{2+} state. It has been applied to fit the magnetic susceptibility of EuNi_2P_2 [7]. Likewise, the T dependencies of the magnetic susceptibility and valence of EuIr_2Si_2 can be described within this model, although not with a single set of parameters [14].

Despite this success of the interconfiguration fluctuation model, there are several observations which require a more complex picture. Recent nuclear magnetic resonance (NMR) measurements on EuNi_2P_2 revealed a strong temperature dependence of the spin-lattice relaxation rate $1/T_1$ that cannot be explained assuming a simple combination of Eu^{2+} and Eu^{3+} states [13]. The enhanced effective charge carrier masses of

*ulrike.stockert@cpfs.mpg.de

EuNi₂P₂ and EuIr₂Si₂ mentioned above suggest a significant hybridization between 4*f* and conduction electron states at low *T* due to Kondo interaction corresponding to a considerable IV character. In fact, the formation of heavy bands resulting from a hybridization between Eu 4*f* and Ni 3*d* states has been directly observed in photoemission spectroscopy on EuNi₂P₂ [18]. Indication for a hybridization of 4*f* and conduction electron states has also been obtained from optical conductivity measurements on EuNi₂P₂ and EuIr₂Si₂ [19]. In addition, electrical resistivity and Hall effect measurements on EuNi₂P₂ have been interpreted with the formation of a heavy-fermion (HF) state as typically observed in Ce and Yb-based Kondo systems [11,15].

The thermopower is known as a sensitive probe for Kondo scattering in HF systems, where it reaches large absolute values around the characteristic Kondo temperature T_K and enhanced values of S/T in the zero-temperature limit. The absolute thermopower of Ce- and Yb-based IV systems typically reaches values of 50–100 $\mu\text{V}/\text{K}$. Here, we present thermal transport data on EuNi₂P₂ and EuIr₂Si₂ with a focus on the thermopower $S(T)$ to evaluate the relevance of the Kondo interaction and valence fluctuations in these materials. In both compounds, we indeed observe large thermopower values, larger than in other VF Eu compounds. However, the temperature dependencies $S(T)$ cannot be explained by simple models for HF systems with Kondo interaction. Instead, we may relate $S(T)$ directly to the temperature dependence of the Eu valence by considering changes in the chemical potential. These results suggest that EuNi₂P₂ and EuIr₂Si₂ cannot be understood within a pure Kondo scenario for HF compounds, but that thermal valence fluctuations between different Eu configurations have to be taken into account and are the main origin of the large thermopower in these materials.

II. EXPERIMENTAL DETAILS

We investigated single crystals of EuNi₂P₂ and EuIr₂Si₂ grown by a flux method as described in Refs. [9,18]. Thermal conductivity κ , thermopower S , and electrical resistivity ρ were measured simultaneously using the thermal transport option of a commercial physical property measurement system (PPMS) from Quantum Design. The electrical and heat currents were applied within the *ab* plane of our platelike single crystals. Measurements have been performed in the temperature range from 2 K to 300 K. With increasing temperature, the heat loss via radiation becomes large. This leads to a strong upturn of our thermal conductivity data above 200 K. Therefore, we do not show thermal conductivity data in this temperature range. The effect is not relevant for thermopower measurements, which allows us to discuss $S(T)$ up to 300 K.

The geometry factor of our samples has a large uncertainty due to the small crystal size of about $4 \times 1 \times 0.1 \text{ mm}^3$ and the relatively large contacts with a width of approximately 0.5 mm required for a good thermalization of the thermometers. Therefore, we scaled our electrical resistivity data to results from AC transport measurements on crystals from the same batches with an optimized geometry. We used the same scaling factor for our thermal conductivity data. The analysis of ρ and κ measured on the same contacts reduces

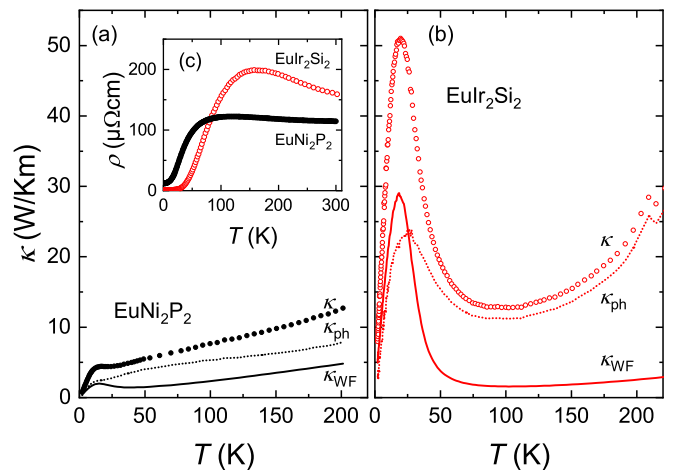


FIG. 1. Temperature dependencies of the total thermal conductivity κ and the estimated electron (κ_{WF}) and phonon contributions (κ_{ph}) for EuNi₂P₂ (a) and EuIr₂Si₂ (b). The inset (c) shows the corresponding electrical resistivities measured simultaneously on the same contacts.

uncertainties of the geometry factor in the estimation of the electronic thermal conductivity from the Wiedemann-Franz (WF) law. Thus, the uncertainty of the absolute values for κ could be reduced to about 10%. The thermopower is in principle independent of the geometry factor. However, the contact size in our measurement was not negligible compared to the sample dimensions. In a previous study on a 4*f* substitution series with the same crystal structure under similar conditions (platelike single crystals, similar contact geometry, using the same experimental setup), we could show that this uncertainty was also below 10% and does not affect the shape of $S(T)$ [20].

III. RESULTS

The electrical resistivities $\rho(T)$ of EuNi₂P₂ and EuIr₂Si₂ are plotted in Fig. 1(c). Our results are similar to data reported in literature [11,14]. Below room temperature, we observe a negative $\partial\rho/\partial T$ for both materials. Maxima are reached at about 120 K (EuNi₂P₂) and 160 K (EuIr₂Si₂). Toward lower *T*, the electrical resistivities strongly decrease. The residual resistivity ratio RRR determined as $\rho(300 \text{ K})/\rho(2 \text{ K})$ is significantly larger for the EuIr₂Si₂ sample (160) than for the EuNi₂P₂ sample (9.3).

The thermal conductivities $\kappa(T)$ of EuNi₂P₂ and EuIr₂Si₂ are plotted in Figs. 1(a) and 1(b), respectively. EuIr₂Si₂ has a significantly larger thermal conductivity than EuNi₂P₂. It exhibits a pronounced maximum around 20 K, while only a small hump is seen in this temperature region for EuNi₂P₂. To evaluate the origin of this difference, we estimated the thermal conductivity contributions from charge carriers (κ_{el}) and phonons (κ_{ph}) using the WF law. We assume that $\kappa_{\text{el}} = \kappa_{\text{WF}} = L_0 T / \rho$ with the Lorenz constant L_0 and determine κ_{ph} as $\kappa_{\text{ph}} = \kappa - \kappa_{\text{WF}}$. The results are also shown in Fig. 1. κ_{WF} is always lower than the total thermal conductivity as expected if the WF law is roughly valid due to a significant

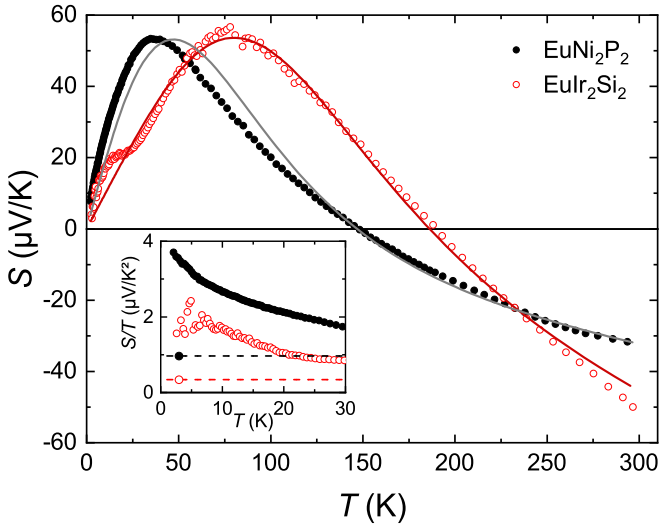


FIG. 2. Temperature dependence of the thermopower $S(T)$ for EuNi_2P_2 and EuIr_2Si_2 . The lines in the main plot are fits to the data, taking into account the temperature dependence of the valence as explained in the text. The hump at around 20 K for EuIr_2Si_2 , which is not reproduced by the fitted curve, is ascribed to phonon drag. The inset shows the low- T part as S/T (symbols) in comparison to the zero-temperature limit of S_d/T (lines) calculated from the effective charge-carrier masses as explained in the text.

phonon contribution in the investigated temperature range. We find that the small bump in the thermal conductivity of EuNi_2P_2 can be attributed almost completely to κ_{el} , while κ_{ph} exhibits only a weak temperature dependence. By contrast, the large maximum in the thermal conductivity of EuIr_2Si_2 is most probably due to maxima of both contributions, κ_{el} and κ_{ph} . Since the WF law is strictly valid only in the zero- T limit, we cannot exclude that κ_{el} of EuIr_2Si_2 is larger than our estimate. However, it seems unlikely that κ_{el} may account for the full thermal conductivity maximum. Most probably, the phonon thermal conductivity of EuIr_2Si_2 exhibits a maximum as expected for clean single crystals. The absence of such a maximum for EuNi_2P_2 is attributed to a lower sample quality, where scattering from defects leads to a suppression of κ_{ph} . This is also in line with the significantly smaller RRR for our EuNi_2P_2 sample compared to the EuIr_2Si_2 crystal.

The thermopower $S(T)$ of EuNi_2P_2 and EuIr_2Si_2 is plotted in Fig. 2 for the temperature range between 2 K and 300 K. Both compounds exhibit a similar qualitative temperature dependence of $S(T)$ with large, positive values at low T , and a change to negative values at higher T . Maxima are observed at $T_{\text{max}} = 37$ K and 81 K for EuNi_2P_2 and EuIr_2Si_2 , respectively. The thermopower of EuIr_2Si_2 exhibits an additional hump at about 20 K, i.e., close to the position of the maximum in our estimate of κ_{ph} . Therefore, we attribute this hump to a phonon-drag contribution. No such contribution is expected for EuNi_2P_2 due to the much lower phonon thermal conductivity in the respective T range.

An exact evaluation of the thermopower contribution due to phonon drag is difficult. It depends on the phonon spectrum and the electron-phonon scattering. Generally, the absolute phonon-drag thermopower increases initially with increasing

TABLE I. Summary of physical properties and fit results for EuNi_2P_2 and EuIr_2Si_2 . Literature data have been summarized from Refs. [7,8,12,14,42].

Compound	EuNi_2P_2	EuIr_2Si_2
Literature data		
T_{sf} (K)	53–80	84–101
$\frac{1}{k_B} E_{\text{exc}}$ (K)	160–192	269–390
Measurement results		
T_{max} (K)	37	81
Fit results		
$\frac{e}{k_B} A_1$ (K)	310	306
A_2 ($\mu\text{V}/\text{K}^2$)	−0.10	−0.19

temperature and phonon density. At higher T , as phonon-phonon interactions become more important, the phonon-drag thermopower decreases again. The maximum is observed typically at 0.1–0.3 of the Debye temperature Θ_D [21]. For EuIr_2Si_2 , a value of $\Theta_D = 270$ K has been estimated from specific-heat measurements [14]. Therefore, for a simple Debye approximation, we expect the phonon-drag contribution to be largest between 27 K and 80 K, which is in reasonable agreement with the observed hump in the thermopower.

At first glance, the thermopower of EuNi_2P_2 and EuIr_2Si_2 resembles those of other Eu systems discussed either as VF or IV materials (apart from the presumed phonon-drag contribution for EuIr_2Si_2). Eu-based VF systems usually have a positive thermopower with a single maximum close to the valence fluctuation temperature T_{VF} [22] as seen, for instance, in $\text{Eu}_3\text{Pd}_{20}\text{Ge}_6$ [23] and $\text{Eu}_4\text{Pd}_{29+x}\text{B}_8$ [3]. Our thermopower curves for EuNi_2P_2 and EuIr_2Si_2 exhibit a similar behavior, however, with some important differences: (1) Our absolute thermopower values are much larger, exceeding $50 \mu\text{V}/\text{K}$ at the maxima compared to about $10 \mu\text{V}/\text{K}$ in $\text{Eu}_3\text{Pd}_{20}\text{Ge}_6$ and $\text{Eu}_4\text{Pd}_{29+x}\text{B}_8$. In fact, the maxima of $S(T)$ of EuNi_2P_2 and EuIr_2Si_2 are comparable to those of Ce- and Yb-based IV systems or of Eu systems discussed as HF compounds with strong Kondo interaction such as EuCu_2Si_2 [4]. (2) Above 150 K, our thermopower curves change signs to negative values. (3) Moreover, the maxima in $S(T)$ are observed at rather low T compared to T_{VF} . An estimate for T_{VF} is given by the excitation energy E_{exc} between the two Eu configurations of the interconfiguration fluctuation model. Fits to Mössbauer spectroscopy and magnetic susceptibility data of EuNi_2P_2 [7,12] yielded values between 160 K and 190 K for E_{exc}/k_B compared to $T_{\text{max}} = 37$ K. Respective values for E_{exc}/k_B of EuIr_2Si_2 have been determined from susceptibility and x-ray absorption measurements on crystals grown under the same conditions as those used in our study. The results correspond to 269 K and 390 K, whereas $T_{\text{max}} = 81$ K [14]. These numbers, as well as other important parameters are summarized in Table I. It turns out that for both materials, the maximum in $S(T)$ is observed at significantly lower T than expected from E_{exc} . Actually, T_{max} is much closer to the spin-fluctuation temperature T_{sf} determined from the same fits to the interconfiguration-fluctuation model: T_{sf} of EuNi_2P_2 takes values from 53 K to 80 K, results for EuIr_2Si_2 range from 84 K to 101 K. Since the spin-fluctuation temperature of the

model accounts for interactions between the Eu states and the conduction electron states, this observation suggests that the Kondo interaction might be responsible for the T dependence of the thermopower of EuNi_2P_2 and EuIr_2Si_2 .

Therefore, and in view of the rather large thermopower values, we compare our $S(T)$ curves to those of IV systems. IV materials usually exhibit large absolute thermopower values of about 50–100 $\mu\text{V}/\text{K}$ with a maximum around the characteristic Kondo temperature T_K [24]. An estimate for the Kondo temperature of EuNi_2P_2 has been obtained from specific heat and thermal expansion data [11]. The value of $T_K \approx 80$ K is about a factor of 2 larger than T_{max} . No such evaluation has been performed for EuIr_2Si_2 . However, the Sommerfeld coefficient γ_0 of EuIr_2Si_2 is significantly smaller than that of EuNi_2P_2 (33 mJ/mole K vs 103 mJ/mole K [10,14]). Using $T_K \propto 1/\gamma_0$, we estimate a Kondo temperature of about 250 K for EuIr_2Si_2 compared to $T_{\text{max}} = 81$ K. It turns out that, for both materials, the maximum in $S(T)$ is observed at significantly lower T than expected from T_K .

Next, we consider the magnitude of our thermopower data. The diffusion thermopower S_d of a Fermi liquid S_d/T is expected to reach a constant value in the zero-temperature limit. Within a free electron model, S_d/T is related directly to the Sommerfeld coefficient γ_0 via a dimensionless constant q as $S_d/T = q(N_A e)^{-1}\gamma_0$ with $N_A e$ being Faraday's number [25]. For a wide range of compounds, including a number of HF materials, q has been demonstrated to be close to ± 1 , whereas the sign of q depends on the type of charge carriers. This observation has also been substantiated theoretically for HF materials [26]. In the inset of Fig. 2, we show the low-temperature part of our thermopower curves as S/T vs T . The values expected from the Sommerfeld coefficients are indicated by lines. It turns out that over a considerable temperature range, the thermopower of our materials is much larger than the one expected from this simple estimation. In the case of EuIr_2Si_2 , this may be attributed to at least to some extent to the phonon-drag contribution. However, the large thermopower values of EuNi_2P_2 cannot be explained solely by the hybridization effects responsible for the moderately enhanced Sommerfeld coefficients. In fact, S/T of EuNi_2P_2 is increasing down to 2 K, without indication for a saturation. This is not surprising since the valence of the system remains temperature dependent down to low T . The situation is less clear for EuIr_2Si_2 due to the relatively large scattering of the thermopower data. However, the phonon-drag contribution for this sample is expected to mask any linear behavior of the diffusion thermopower in this T range. Altogether, neither the shape nor the absolute thermopower values of EuNi_2P_2 and EuIr_2Si_2 can be understood in terms of pure Kondo interaction and an IV scenario.

IV. DISCUSSION

So far, we have discussed the thermopower curves of EuNi_2P_2 and EuIr_2Si_2 rather qualitatively. In the following, we compare our thermopower data to several models considering valence fluctuations and Kondo interaction. Thereafter, we propose a very simple, phenomenological description of our thermopower curves taking into account only the temperature dependence of the valence. Examples of calculated ther-

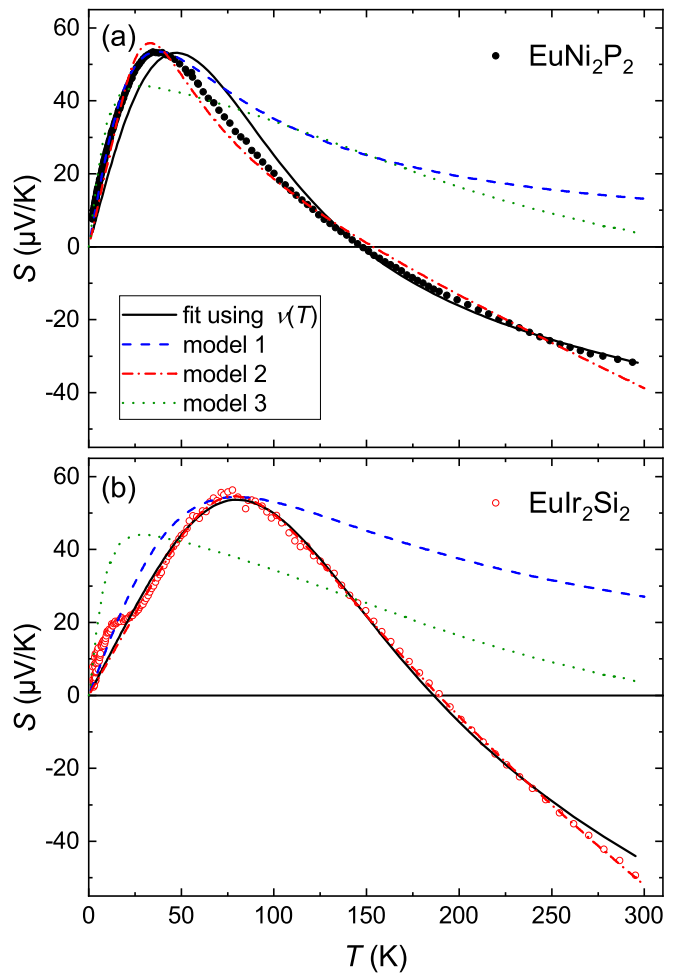


FIG. 3. Thermopower of EuNi_2P_2 (a) and EuIr_2Si_2 (b) in comparison to different calculated or fitted curves. The solid lines correspond to our fits using the temperature dependence of the valence, which is also shown in Fig. 2. The other curves are calculated for different models as explained in the text.

mopower curves for EuNi_2P_2 and EuIr_2Si_2 are summarized in Fig. 3.

The thermopower of $4f$ systems is frequently discussed in relation to the density of states (DOS). This approach is based on a simplified Mott expression derived from the Boltzmann equation using various approximations, amongst others the Sommerfeld approximation, a spherical Fermi surface, and an isotropic relaxation time [27,28]. It relates the diffusion thermopower to the energy derivative of the logarithmic DOS $N(E)$: $S/T \propto \partial \ln N / \partial E|_{E_F}$. The large thermopower values in Kondo systems can then be qualitatively explained by the strong peak in the DOS appearing at low temperature. However, a calculation of the thermopower based on this equation requires exact knowledge of the DOS close to the Fermi level. Alternatively, one may start with a model DOS to calculate the thermopower of $4f$ systems.

This procedure is used in a phenomenological model introduced by Hirst [29], which yields a very simple expression for the thermopower of $4f$ systems. It starts with two competing configurations and a finite mixing interaction. The $4f$ DOS is approximated by a Lorentzian form with half

width Γ and the maximum at an energy $\epsilon_0 - \epsilon_F$ with respect to the Fermi level. Within Boltzmann theory and using the relaxation time approximation, the thermopower then takes the form $S = AT/(B^2 + T^2)$ [30]. The parameters A and B are related to Γ and $\epsilon_0 - \epsilon_F$. Fitting thermopower data of Ce- and Yb-based IV materials to this simple relation often yields reasonable agreement with measured curves, especially at intermediate T around the maximum [31,32]. However, the model does not describe our thermopower data for EuNi_2P_2 and EuIr_2Si_2 in a wide temperature range. In Fig. 3, we show calculated curves (model 1) for EuNi_2P_2 and EuIr_2Si_2 . A and B have been adjusted to fit the data around the maxima. Although the maxima of $S(T)$ are reproduced quite well, there are significant deviations, especially at higher T . In particular, the model cannot account for the sign changes.

Subsequently, the model was extended by including a temperature dependence of the $4f$ line width $W = 2\Gamma$ of the form $W = T_{\text{sf}} \exp(-T_{\text{sf}}/T)$ [33]. The thermopower is then given by $S = c_1 T T_0 / (T_0^2 + W^2)$ with $k_B T_0 = \epsilon_0 - \epsilon_F$. A second term $c_2 T$ is frequently added to account for a band of light charge carriers (d or s type) [33,34]. However, this approach is problematic since thermopower contributions from different scattering channels do not add directly, but are weighted by the electrical resistivities according to the Nordheim-Gorter relation. Moreover, the temperature-dependent $4f$ line width of the model goes to zero in the zero-temperature limit, a situation that is not consistent with the noninteger valence of EuNi_2P_2 and EuIr_2Si_2 . Actually, we can describe our thermopower data by this model, however, only when the linear term is large — much larger than expected for light charge carriers and those typically observed in Ce-based IV systems [33,34]. We show the respective curves for EuNi_2P_2 and EuIr_2Si_2 in Fig. 3 (model 2). For EuIr_2Si_2 , the agreement between fit and data is almost perfect. In the case of EuNi_2P_2 , the deviations are somewhat larger and the shape of $S(T)$ is not well reproduced. Since the assumptions of the model are not applicable for our materials, it seems that the good quality of the fit is accidental and probably also facilitated by the relatively large number of — in total four — free parameters. Other attempts to extend the model, for instance, by also introducing a temperature dependence of T_0 [35], even further increase the number of fit parameters.

A different starting point to understand the thermopower of IV systems is the Anderson impurity model, which considers the Kondo interaction between conduction and Eu $4f$ electrons. It is frequently used to discuss the thermopower of HF compounds with Ce and Yb [24] but has been applied also successfully to Eu-based IV materials [36]. The main parameters of this model are the position of the (undisturbed) $4f$ level and the hybridization strength. Thermopower curves were calculated using the noncrossing approximation for different sets of parameters. $S(T)$ exhibits a maximum at low temperatures and a sign change at higher T as observed in our measurements. However, these curves are highly asymmetric close to the maxima, which is not in agreement with our experiments. To illustrate this, we show one curve from Ref. [36] in Fig. 3 (model 3). The sign change of this curve is expected above 300 K.

Another approach to discuss the thermopower of IV Eu systems is based on the Falicov-Kimball model [37], which consists of a combination of localized and itinerant states with varying occupation due to thermal fluctuations [38,39]. However, in the zero-temperature limit, this model predicts an integer valence, which is not valid for our materials. In fact, as pointed out in Ref. [38], a complete theoretical description of $4f$ fluctuating states requires a combination of the periodic Anderson model with the Falicov-Kimball model. This appears to be rather challenging and has not been accomplished till now.

All models discussed so far are microscopic ones in the sense that they assume either a certain shape of the DOS or a specific type of interaction and then calculate the thermopower. In what follows, we use a different approach, namely, we evaluate directly the effect of the valence change with temperature on the thermopower without considering the reason for the valence change. In fact, any temperature gradient in our materials is accompanied by a valence gradient because of the strong T dependence of ν . This gives rise to a thermopower contribution S_{VF} due to the variation of the number of available charge carriers or, more precisely, the change of the chemical potential μ along the samples. It has been shown [40,41], that this anomalous contribution is approximately proportional to the valence change with temperature $d\nu/dT$. In brief, this relation is obtained from the generalized transport equations by using the electrochemical potential $\mu + e\Phi$ instead of the electrical potential $e\Phi$, e being the electron charge. For simplicity, we only consider the isotropic situation, where the transport coefficients are scalar. The thermopower then contains two contributions:

$$S = L_{12}/L_{11} - \frac{1}{e} \frac{d\mu}{dT} = S_{\text{ref}} + S_{\text{VF}}. \quad (1)$$

L_{11} and L_{12} are the transport coefficients. If $d\mu/dT$ can be ignored, then $S = S_{\text{ref}} = L_{12}/L_{11}$, which is the well-known relation for S of (physically) homogeneous materials without a temperature-dependent valence, i.e., S_{ref} corresponds to the thermopower of a suitable reference material. We approximate this contribution by a linear thermopower $S_{\text{ref}} \propto T$, as expected for a simple metal. The second term of Eq. (1) arises due to the temperature dependence of the chemical potential. Assuming that this is dominated by the valence effect, we may replace the temperature derivative of the chemical potential by the one of the valence. In this case, the anomalous thermopower contribution has the form

$$S_{\text{VF}} = -\frac{1}{e} \frac{\partial \mu}{\partial \nu} \frac{d\nu}{dT} = -A_1 \frac{d\nu}{dT}. \quad (2)$$

In Refs. [40,41], it was suggested that $\partial \mu / \partial \nu$ should be of the order of the Fermi energy E_F which was then related to the DOS D as $E_F \propto 1/D$. However, since in our case the valence change arises due to excitations from the $J = 0$ state of Eu^{3+} to the $J = 7/2$ state of Eu^{2+} , the relevant energy scale is rather the excitation energy E_{exc} , so eA_1 should be of similar magnitude as E_{exc} . Above, we have already used this energy as an estimate for the valence fluctuation temperature T_{VF} . The respective values determined from fits to the interconfiguration fluctuation model are given in Table I.

In conclusion, we get a very simple relation for the thermopower of materials with a strongly temperature-dependent valence:

$$S = A_2 T - A_1 \frac{d\nu}{dT}. \quad (3)$$

At this point, we would like to mention that there is an important difference between our linear-in- T term to the thermopower and the linear thermopower contribution often added in literature to account for light charge carriers — a procedure that may be questioned as discussed above. In our case, the simple sum for the two thermopower contributions stems from using the electrochemical potential, which consists of two components, the electrical and the chemical one, i.e., the sum describes the thermopower of a single channel but with a temperature-dependent number of carriers.

We fitted our thermopower curves for EuNi_2P_2 and EuIr_2Si_2 to Eq. (3) omitting the data below 30 K in case of EuIr_2Si_2 . To reduce the scattering, we used modeled curves for $\nu(T)$ from Ref. [7] (EuNi_2P_2) and Ref. [14] (EuIr_2Si_2) instead of measured valence data to calculate the derivatives $d\nu/dT$. The results of this procedure are shown in Fig. 2 in comparison to the data. The curves are also plotted in Fig. 3 [fit using $\nu(T)$] to allow for a direct comparison to the other calculated curves. The fit parameters $(e/k_B)A_1$ and A_2 are given in Table I.

It turns out that the simple relation Eq. (3) describes the measured thermopower curves fairly well. The fit parameters A_1 and A_2 are mainly determined by the height of the maximum in $S(T)$ and the thermopower value at room temperature. By contrast, the position of the maximum T_{max} depends only weakly on the fit parameters and mostly on the derivative $d\nu/dT$. T_{max} is very well reproduced by the fit, especially for EuIr_2Si_2 . This provides strong evidence that the maximum in $S(T)$ is indeed caused by the temperature-dependent Eu valence and not by Kondo interaction. Further confirmation for this picture is given by the values for the fit parameter A_1 . For EuIr_2Si_2 , $(e/k_B)A_1$ actually lies within the range expected from E_{exc}/k_B . The agreement for EuNi_2P_2 is less perfect, which is discussed below.

The quality of the fits is also illustrated by Fig. 3, which compares the different calculated thermopower curves and fits to the measured data of EuNi_2P_2 and EuIr_2Si_2 . Only model 2 provides a similar good description of the data as Eq. (3), however, by using four instead of two free parameters. For EuIr_2Si_2 , the differences between these two curves and the data are small. In the case of EuNi_2P_2 , the actual maximum in $S(T)$ is at slightly lower T than predicted by our fit to Eq. (3). However, the overall shape of $S(T)$ is well reproduced by this relation, while model 2 oscillates around the data.

Altogether, the agreement between fit and data is better for EuIr_2Si_2 than for EuNi_2P_2 . The same holds for the fit parameter $(e/k_B)A_1$ if compared to E_{exc}/k_B . These deviations may be partially due to the use of fitted data for $\nu(T)$. Any deviation between these curves and the real valence will also lead to systematic errors in the derivatives $d\nu/dT$ used in our fitting of $S(T)$. The valence fit for EuIr_2Si_2 has been obtained from valence data measured on samples grown under the same conditions as those investigated here. By contrast, the valence curve for EuNi_2P_2 stems from a fit to susceptibility data,

which is only an indirect measure for $\nu(T)$. The respective fit parameters reproduced the Mössbauer isomer shift with limited accuracy, in particular below 40 K, i.e., in the region of our maximum in $S(T)$. Therefore, we may not exclude that the deviations between the peak positions of data and fit for EuNi_2P_2 are caused by uncertainties in $\nu(T)$ or due to sample dependencies.

Actually, the quality of our fits to $S(T)$ is rather surprising taking into account the approximations used in the derivation of Eq. (3). Our assumption of a linear reference thermopower is a very simple one. Although $S_d \propto T$ in the free-electron approximation at very low and at high temperatures, these two regimes have different slopes and are connected by a crossover region with deviating behavior [21]. Moreover, reference materials for EuNi_2P_2 and EuIr_2Si_2 in the sense of Eq. (1) may still exhibit a hybridization between $4f$ and conduction electrons. This may be the reason for the large values for A_2 obtained from our fits. They are significantly larger than those observed in simple metals, which typically reach thermopower values of 2 to $10 \mu\text{V}/\text{K}$ at 300 K [21]. It may also give rise to a nonlinear behavior of $S_{\text{ref}}(T)$. Thus, it appears that deviations from $S_{\text{ref}} \propto T$ are rather to be expected than unusual. Another assumption, which may be questioned, is the temperature-independent relation between μ and ν . It allowed us to use a constant parameter $A \propto E_{\text{exc}}$ in Eq. (2). However, early Mössbauer spectroscopy experiments on EuIr_2Si_2 suggested a temperature-dependent excitation energy E_{exc} [8,42]. It is, therefore, not trivial that we may fit our data using a constant value for A_1 . Despite these approximations, Eq. (3) provides a very good and simple description of the thermopower of EuNi_2P_2 and EuIr_2Si_2 with only two fit parameters. Since relation Eq. (3) uses directly the temperature dependence of the valence and does not assume a specific functional form of $S(T)$, it might be applicable more generally. Systematic investigations on a larger number of materials with a strong temperature dependence of the valence are necessary to confirm this possibility. The VF materials $\text{Eu}_3\text{Pd}_{20}\text{Ge}_6$ and $\text{Eu}_4\text{Pd}_{29+3}\text{B}_8$ mentioned above have rather weak temperature dependencies of their valence [3,6]. Therefore, S_{VF} is expected to be small, which is in line with the relatively small thermopowers observed in these materials.

Our analysis of the thermopower of EuNi_2P_2 and EuIr_2Si_2 revealed that the large values and the characteristic temperature dependencies are not caused predominantly by Kondo interaction between Eu and conduction electron states, but arise mainly from the strong temperature dependence of the Eu valence. Both the position and the height of the maxima in $S(T)$ are in line with this scenario. This demonstrates that thermal valence fluctuations between distinct Eu states play an important role in these materials at least above 10 K.

V. SUMMARY

We studied the thermoelectric transport properties of the VF compounds EuNi_2P_2 and EuIr_2Si_2 . The thermal conductivity of these materials shows no unusual behavior. By contrast, the thermopower of EuNi_2P_2 and EuIr_2Si_2 exhibits large values and a characteristic temperature dependence. We were able to explain this behavior taking into account the

temperature dependence of the Eu valence, which leads to an additional thermopower contribution due to variations in the chemical potential. Further experimental and theoretical investigations on the thermopower of materials with a strongly

temperature-dependent valence are necessary to evaluate the relevance of this effect in general. Our results confirm that valence fluctuations have to be taken into consideration for an understanding of EuNi_2P_2 and EuIr_2Si_2 .

- [1] Y. Ōnuki, A. Nakamura, F. Honda, D. Aoki, T. Takeuchi, M. Nakashima, Y. Amako, H. Harima, K. Matsubayashi, Y. Uwatoko, S. Kayama, T. Kagayama, K. Shimizu, S. E. Muthu, D. Braithwaite, B. Salce, H. Shiba, T. Yara, Y. Ashitomi, H. Akamine, K. Tomori, M. Hedo, and T. Nakama, *Philos. Mag.* **97**, 3399 (2017).
- [2] R. C. Rau, *Acta Cryst.* **20**, 716 (1966).
- [3] R. Gumeniuk, W. Schnelle, M. A. Ahmida, M. M. Abd-Elmeguid, K. O. Kvashnina, A. A. Tsirlin, A. Leithe-Jasper, and C. Geibel, *J. Phys.: Condens. Matter* **28**, 115601 (2016).
- [4] Z. Hossain, C. Geibel, N. Senthilkumaran, M. Deppe, M. Baenitz, F. Schiller, and S. L. Molodtsov, *Phys. Rev. B* **69**, 014422 (2004).
- [5] W. Iha, T. Yara, Y. Ashitomi, M. Kakihana, T. Takeuchi, F. Honda, A. Nakamura, D. Aoki, J. Gouchi, Y. Uwatoko, T. Kida, T. Tahara, M. Hagiwara, Y. Haga, M. Hedo, T. Nakama, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **87**, 064706 (2018).
- [6] S. Tsutsui, M. Mizumaki, Y. Kobayashi, J. Kitagawa, and T. Takabatake, *Phys. Rev. B* **80**, 235115 (2009).
- [7] R. Nagarajan, G. K. Shenoy, L. C. Gupta, and E. V. Sampathkumaran, *Phys. Rev. B* **32**, 2846 (1985).
- [8] B. Chevalier, J. M. D. Coey, B. Lloret, and J. Etourneau, *J. Phys. C: Solid State Phys.* **19**, 4521 (1986).
- [9] S. Seiro and C. Geibel, *J. Phys.: Condens. Matter* **23**, 375601 (2011).
- [10] R. A. Fisher, P. Radhakrishna, N. E. Phillips, J. V. Badding, and A. M. Stacy, *Phys. Rev. B* **52**, 13519 (1995).
- [11] Y. Hiranaka, A. Nakamura, M. Hedo, T. Takeuchi, A. Mori, Y. Hirose, K. Mitamura, K. Sugiyama, M. Hagiwara, T. Nakama, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **82**, 083708 (2013).
- [12] U. B. Paramanik, A. Bar, D. Das, N. Caroca-Canales, R. Prasad, C. Geibel, and Z. Hossain, *J. Phys.: Condens. Matter* **28**, 166001 (2016).
- [13] N. Higa, M. Yogi, H. Kuroshima, T. Toji, H. Niki, Y. Hiranaka, A. Nakamura, T. Nakama, M. Hedo, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **87**, 094708 (2018).
- [14] S. Seiro, Y. Prots, K. Kummer, H. Rosner, R. C. Gil, and C. Geibel, *J. Phys.: Condens. Matter* **31**, 305602 (2019).
- [15] H. Wada, K. Tanabe, I. Yamamoto, and A. Mitsuda, *Solid State Commun.* **300**, 113665 (2019).
- [16] B. C. Sales and D. K. Wohlleben, *Phys. Rev. Lett.* **35**, 1240 (1975).
- [17] W. Franz, F. Steglich, W. Zell, D. Wohlleben, and F. Pobell, *Phys. Rev. Lett.* **45**, 64 (1980).
- [18] S. Danzenbächer, D. V. Vyalikh, Y. Kucherenko, A. Kade, C. Laubschat, N. Caroca-Canales, C. Krellner, C. Geibel, A. V. Fedorov, D. S. Dessau, R. Follath, W. Eberhardt, and S. L. Molodtsov, *Phys. Rev. Lett.* **102**, 026403 (2009).
- [19] V. Guritanu, S. Seiro, J. Sichelschmidt, N. Caroca-Canales, T. Izuka, S. Kimura, C. Geibel, and F. Steglich, *Phys. Rev. Lett.* **109**, 247207 (2012).
- [20] U. Köhler, N. Oeschler, F. Steglich, S. Maquilon, and Z. Fisk, *Phys. Rev. B* **77**, 104412 (2008).
- [21] F. J. Blatt, P. A. Schroeder, C. L. Foiles, and D. Greig, *Thermoelectric Power of Metals* (Plenum Press, New York, 1976).
- [22] D. Jaccard and J. Sierro, *Valence Instabilities* (North-Holland, Amsterdam, 1982), p. 469.
- [23] J. Kitagawa, T. Sasakawa, T. Suemitsu, T. Takabatake, and M. Ishikawa, *J. Phys. Soc. Jpn.* **71**, 1222 (2002).
- [24] V. Zlatić and R. Monnier, *Phys. Rev. B* **71**, 165109 (2005).
- [25] K. Behnia, D. Jaccard, and J. Flouquet, *J. Phys.: Condens. Matter* **16**, 5187 (2004).
- [26] K. Miyake and H. Kohno, *J. Phys. Soc. Jpn.* **74**, 254 (2005).
- [27] N. F. Ziman, *Electrons and Phonons* (Clarendon Press, Oxford, 1960).
- [28] N. F. Mott and E. A. Davis, *Electronic Processes in Noncrystalline Materials* (Oxford University, Oxford, 1971).
- [29] L. L. Hirst, *Phys. Rev. B* **15**, 1 (1977).
- [30] U. Gottwick, K. Gloos, S. Horn, F. Steglich, and N. Grewe, *J. Magn. Magn. Mater.* **47-48**, 536 (1985).
- [31] R. Gumeniuk, R. Sarkar, C. Geibel, W. Schnelle, C. Paulmann, M. Baenitz, A. A. Tsirlin, V. Guritanu, J. Sichelschmidt, Y. Grin, and A. Leithe-Jasper, *Phys. Rev. B* **86**, 235138 (2012).
- [32] U. Stockert, S. Hartmann, M. Deppe, N. Caroca-Canales, J. G. Sereni, C. Geibel, and F. Steglich, *Phys. Rev. B* **92**, 054415 (2015).
- [33] A. Freimuth, *J. Magn. Magn. Mater.* **68**, 28 (1987).
- [34] D. Kaczorowski and K. Gofryk, *Solid State Commun.* **138**, 337 (2006).
- [35] C. S. Garde and J. Ray, *Phys. Rev. B* **51**, 2960 (1995).
- [36] V. Zlatić, R. Monnier, and J. Freericks, *Physica B* **378-380**, 661 (2006).
- [37] L. M. Falicov and J. C. Kimball, *Phys. Rev. Lett.* **22**, 997 (1969).
- [38] V. Zlatić and J. K. Freericks, *Acta Phys. Pol. B* **32**, 3253 (2001).
- [39] V. Zlatić, R. Monnier, J. Freericks, and K. W. Becker, *Phys. Rev. B* **76**, 085122 (2007).
- [40] B. Wittershagen and D. Wohlleben, *J. Magn. Magn. Mater.* **47-48**, 497 (1985).
- [41] H. Schneider, Ph.D. thesis, University of Cologne, 1984.
- [42] S. Patil, R. Nagarajan, L. C. Gupta, R. Vijayaraghavan, and B. D. Padalia, *Solid State Commun.* **63**, 955 (1987).