

Fig. 2: Possible states of outstanding packets.

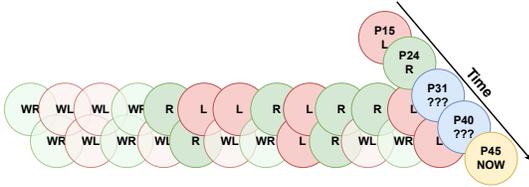


Fig. 3: Example nodes of the *belief network*.

can not be of state **WR(WL)**, when more fresh OPs are **R(L)**, as we do not allow out-of-order transmissions in the network. The probability of a node is the product of the probabilities of each OP being in the corresponding state. Fig. 3 gives an example of the BN construction. Here, the TL decides on the admission of the current packet at  $k = 45$ . ACK timeout has passed for the packet sent at  $k = 15$ , ACK has been received for the packet sent at  $k = 24$ . The BN nodes are built for two OPs, the exact state of which is not known.

After defining which information is presumably available at the controller for each BN node, the sensor augments the controller's state by repeating its estimation process. The difference between the current measurement value and the augmented controller estimation  $\tilde{x}_i^{node}$  represents the relevance of the current update for the control process. The expression for the benefit of transmitting the current update is:

$$B_i[k] = \sum_{\text{possible nodes}} p(\text{node}) |x_i[k] - \tilde{x}_i^{node}[k]|. \quad (3)$$

The computational complexity of (3) grows exponentially with OP count  $\Omega$ . In our experiments, we recorded that  $\Omega$  was less than 5, and the computation time was below the sampling period of 10ms. The complexity-accuracy trade-off is part of future work.

**Cost of Update.** The sensor approximates the expected packet delay depending on the time elapsed since the previous transmission. The delay scaled by maximum delay gives the cost of transmission  $C_i[k] \in [0, 1]$ . The admission decision is represented by  $\delta_i[k] = \mathbb{1}(B_i[k] \geq \lambda C_i[k])$ , where  $\lambda$  is a threshold. Note that the delay as a function of time passed since the previous transmission is typically a descending function. Indeed, if a new packet is sent right after another, there is a high probability that the second packet would wait in the MAC queue until the first packet is served. For control applications, it is desirable to eliminate unnecessary waiting times and deliver fresh updates. Our VoU policy prevents sending packets in bursts unless they are very significant.

#### IV. EXPERIMENTAL RESULTS

We conduct experiments with two control loops including Zolertia Re-Mote sensors following IEEE 802.15.4 standard [8]. There is a cross-traffic in the network independent of the actions of considered loops. We compare the LQG cost of the

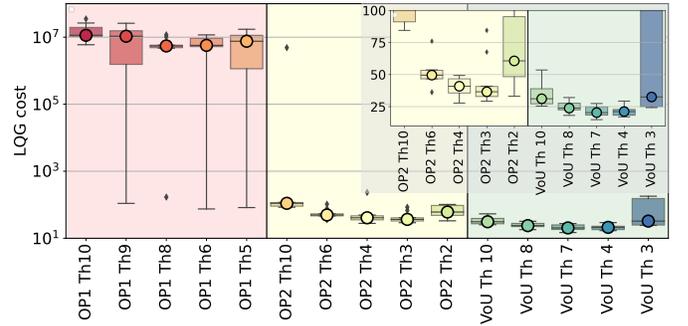


Fig. 4: Control performance of ET with the maximum OP count of 1, 2 and of proposed TL utilizing VoU.

VoU TL scheme with other two ET schemes. As in [4], both of them trigger sending updates based on the deviation of the current state from augmented controller estimation. The first scheme limits  $\Omega \leq 1$ , the second one allows  $\Omega \leq 2$ . Note that  $\Omega$  for VoU scheme is not limited.

LQG costs from (2) averaged over two loops and 10 simulation runs by 60 seconds are given in Fig. 4 for different  $\lambda$ . The performance of ET with maximum  $\Omega$  of one is unsatisfactory as when packets are lost because of cross-traffic, new updates are not admitted to the network until the ACK timeout expires, allowing for the state to grow. With maximum  $\Omega$  of two, LQG cost is lower, because losses can be secured by extra transmissions, but frequent sending of two consecutive packets results in higher waiting times, especially for the second admitted packet, deteriorating the control performance. The proposed VoU scheme achieves the 75% better performance as it admits new updates only when they carry relevant information provided that their expected delay is limited and the congestion level is controlled. Additional experiments show that perfect knowledge of the controller estimation by the sensor, i.e., perfect BN, would lead to a further performance increase of 15%, which is significantly smaller than 75% gain that can be achieved with the proposed BN construction method. That fact witnesses the accuracy of our method.

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