## Observation of $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$

P.-C. Lu, ${ }^{63}$ M.-Z. Wang, ${ }^{63}$ R. Chistov, ${ }^{45,55}$ P. Chang, ${ }^{63}$ I. Adachi, ${ }^{18,14}$ J. K. Ahn, ${ }^{41}$ H. Aihara, ${ }^{88}$ S. Al Said, ${ }^{81,39}$ D. M. Asner, ${ }^{3}$ H. Atmacan, ${ }^{77}$ V. Aulchenko, ${ }^{4,67}$ T. Aushev, ${ }^{56}$ R. Ayad, ${ }^{81}$ V. Babu, ${ }^{82}$ I. Badhrees, ${ }^{81,38}$ A. M. Bakich, ${ }^{80}$ V. Bansal,${ }^{69}$ P. Behera, ${ }^{26}$ C. Beleño, ${ }^{13}$ M. Berger, ${ }^{78}$ V. Bhardwaj, ${ }^{22}$ B. Bhuyan, ${ }^{24}$ T. Bilka, ${ }^{5}$ J. Biswal, ${ }^{34}$ G. Bonvicini, ${ }^{92}$ A. Bozek, ${ }^{64}$ M. Bračko, ${ }^{50,34}$ T. E. Browder, ${ }^{17}$ L. Cao, ${ }^{36}$ D. Červenkov, ${ }^{5}$ M.-C. Chang, ${ }^{95}$ V. Chekelian, ${ }^{51}$ A. Chen, ${ }^{61}$ B. G. Cheon, ${ }^{16}$ K. Chilikin, ${ }^{45}$ K. Cho, ${ }^{40}$ S.-K. Choi, ${ }^{15}$ Y. Choi, ${ }^{79}$ S. Choudhury, ${ }^{25}$ D. Cinabro, ${ }^{92}$ S. Cunliffe, ${ }^{8}$ N. Dash, ${ }^{23}$ S. Di Carlo, ${ }^{43}$ Z. Doležal, ${ }^{5}$ T. V. Dong, ${ }^{18,14}$ Z. Drásal, ${ }^{5}$ S. Eidelman, ${ }^{4,67,45}$ D. Epifanov, ${ }^{4,67}$ J. E. Fast, ${ }^{69}$ T. Ferber, ${ }^{8}$ B. G. Fulsom, ${ }^{69}$ R. Garg, ${ }^{70}$ V. Gaur, ${ }^{91}$ N. Gabyshev, ${ }^{4,67}$ A. Garmash,,${ }^{4,67}$ M. Gelb, ${ }^{36}$ A. Giri, ${ }^{25}$ P. Goldenzweig, ${ }^{36}$ E. Guido ${ }^{32}$ J. Haba,,${ }^{18,14}$ K. Hayasaka, ${ }^{66}$ H. Hayashii, ${ }^{60}$ S. Hirose ${ }^{57}$ W.-S. Hou, ${ }^{63}$ C.-L. Hsu, ${ }^{52}$ T. Iijima, ${ }^{58,57}$ K. Inami, ${ }^{57}$ G. Inguglia, ${ }^{8}$ A. Ishikawa, ${ }^{86}$ R. Itoh, ${ }^{18,14}$ M. Iwasaki, ${ }^{68}$ Y. Iwasaki, ${ }^{18}$ W. W. Jacobs, ${ }^{27}$ H. B. Jeon, ${ }^{42}$ S. Jia, ${ }^{2}$ Y. Jin, ${ }^{88}$ D. Joffe, ${ }^{37}$ K. K. Joo, ${ }^{6}$ T. Julius, ${ }^{52}$ A. B. Kaliyar, ${ }^{26}$ T. Kawasaki, ${ }^{66}$ H. Kichimi, ${ }^{18}$ C. Kiesling, ${ }^{51}$ D. Y. Kim, ${ }^{76}$ H. J. Kim, ${ }^{42}$ J. B. Kim, ${ }^{41}$ K. T. Kim ${ }^{41}$, S. H. Kim, ${ }^{16}$ K. Kinoshita, ${ }^{7}$ P. Kodyš, ${ }^{5}$ S. Korpar, ${ }^{50,34}$ D. Kotchetkov, ${ }^{17}$ P. Križan, ${ }^{46,34}$ R. Kroeger, ${ }^{53}$ P. Krokovny, ${ }^{4,67}{ }^{48}$ T. Kuhr, ${ }^{47}$ R. Kulasiri, ${ }^{37}$ A. Kuzmin ${ }^{4,67}$ Y.-J. Kwon, ${ }^{94}$ Y.-T. Lai, ${ }^{18}$ J. S. Lange, ${ }^{11}$ I. S. Lee, ${ }^{16}$ S. C. Lee, ${ }^{42}$ L. K. Li, ${ }^{28}$ Y. B. Li, ${ }^{71}$ L. Li Gioi, ${ }^{51}$ J. Libby, ${ }^{26}$ D. Liventsev, ${ }^{91,18}$ M. Lubej, ${ }^{34}$ T. Luo, ${ }^{10}$ M. Masuda, ${ }^{87}$ T. Matsuda, ${ }^{54}$ D. Matvienko, ${ }^{4,67,45}$ M. Merola, ${ }^{31,59}$ K. Miyabayashi, ${ }^{60}$ H. Miyata, ${ }^{66}$ R. Mizuk, ${ }^{45,55,56}$ G. B. Mohanty, ${ }^{82}$ H. K. Moon, ${ }^{41}$ T. Mori, ${ }^{57}$ R. Mussa, ${ }^{32}$ M. Nakao,,$_{5,14}^{18}$ T. Nanut, ${ }^{34}$ K. J. Nath,,${ }^{24}$ Z. Natkaniec,,${ }^{64}$ M. Nayak,,${ }^{92,18}$ N. K. Nisar, ${ }^{72}$ S. Nishida, ${ }^{18,14}$ S. Ogawa, ${ }^{85}$ S. Okuno, ${ }^{35}$ H. Ono, ${ }^{65,66}$ H. Ozaki, ${ }^{18,14}$ P. Pakhlov, ${ }^{45,55}$ G. Pakhlova, ${ }^{45,56}$ B. Pal, ${ }^{3}$ S. Pardi, ${ }^{31}$ H. Park, ${ }^{42}$ S. Paul, ${ }^{84}$ T. K. Pedlar, ${ }^{48}$ R. Pestotnik,,${ }^{34}$ L. E. Piilonen, ${ }^{91}$ V. Popov, ${ }^{45,56}$ E. Prencipe, ${ }^{20}$ A. Rabusov ${ }^{84}$ M. Ritter, ${ }^{47}$ A. Rostomyan, ${ }^{8}$ G. Russo, ${ }^{31}$ Y. Sakai,,${ }^{18,14}$ M. Salehi, ${ }^{49,47}$ S. Sandilya, ${ }^{7}$ L. Santelj, ${ }^{18}$ T. Sanuki, ${ }^{86}$ V. Savinov, ${ }^{72}$ O. Schneider, ${ }^{44}$ G. Schnell, ${ }^{1,21}$ C. Schwanda, ${ }^{29}$ Y. Seino ${ }^{66}$ K. Senyo, ${ }^{93}$ M. E. Sevior, ${ }^{52}$ V. Shebalin, ${ }^{4,67}$ C. P. Shen, ${ }^{2}$ T.-A. Shibata, ${ }^{89}$ J.-G. Shiu, ${ }^{63}$ B. Shwartz, ${ }^{4,67}$ F. Simon, ${ }^{51,83}$ J. B. Singh, ${ }^{70}$ A. Sokolov, ${ }^{30}$ E. Solovieva, ${ }^{45,56}$ M. Starič, ${ }^{34}$ J. F. Strube, ${ }^{69}$ M. Sumihama, ${ }^{12}$ T. Sumiyoshi, ${ }^{90}$ W. Sutcliffe, ${ }^{36}$ M. Takizawa, ${ }^{75,19,73}$ U. Tamponi, ${ }^{32}$ K. Tanida, ${ }^{33}$ F. Tenchini, ${ }^{52}$ M. Uchida, ${ }^{89}$ T. Uglov, ${ }^{45,56}$ Y. Unno, ${ }^{16}$ S. Uno ${ }^{18,14}$ P. Urquijo, ${ }^{52}$ Y. Usov, ${ }^{4,67}$ S. E. Vahsen, ${ }^{17}$ C. Van Hulse, ${ }^{1}$ R. Van Tonder, ${ }^{36}$ G. Varner ${ }^{17}{ }^{17}$ A. Vinokurova, ${ }^{4,67}$ V. Vorobyev, $, 4,67,45$ A. Vossen, ${ }^{9}$ B. Wang, ${ }^{7}$ C. H. Wang, ${ }^{62}$ X. L. Wang, ${ }^{10}$ M. Watanabe, ${ }^{66}$ S. Watanuki, ${ }^{86}$ E. Widmann, ${ }^{78}$ E. Won, ${ }^{41}$ H. Ye, ${ }^{8}$ J. H. Yin, ${ }^{28}$ C. Z. Yuan, ${ }^{28}$ Z. P. Zhang, ${ }^{74}$ V. Zhilich, ${ }^{4,67}$ V. Zhukova, ${ }^{45,55}$ V. Zhulanov, ${ }^{4,67}$ and A. Zupanc ${ }^{46,34}$

## (The Belle Collaboration)

${ }^{1}$ University of the Basque Country UPV/EHU, 48080 Bilbao<br>${ }^{2}$ Beihang University, Beijing 100191<br>${ }^{3}$ Brookhaven National Laboratory, Upton, New York 11973<br>${ }^{4}$ Budker Institute of Nuclear Physics SB RAS, Novosibirsk 630090<br>${ }^{5}$ Faculty of Mathematics and Physics, Charles University, 12116 Prague<br>${ }^{6}$ Chonnam National University, Kwangju 660-701<br>${ }^{7}$ University of Cincinnati, Cincinnati, Ohio 45221<br>${ }^{8}$ Deutsches Elektronen-Synchrotron, 22607 Hamburg<br>${ }^{9}$ Duke University, Durham, North Carolina 27708<br>${ }^{10}$ Key Laboratory of Nuclear Physics and Ion-beam Application (MOE) and Institute of Modern Physics,<br>Fudan University, Shanghai 200443<br>${ }^{11}$ Justus-Liebig-Universität Gießen, 35392 Gießen<br>${ }^{12}$ Gifu University, Gifu 501-1193<br>${ }^{13}$ II. Physikalisches Institut, Georg-August-Universität Göttingen, 37073 Göttingen<br>${ }^{14}$ SOKENDAI (The Graduate University for Advanced Studies), Hayama 240-0193<br>${ }^{15}$ Gyeongsang National University, Chinju 660-701<br>${ }^{16}$ Hanyang University, Seoul 133-791<br>${ }^{17}$ University of Hawaii, Honolulu, Hawaii 96822<br>${ }^{18}$ High Energy Accelerator Research Organization (KEK), Tsukuba 305-0801<br>${ }^{19}$ J-PARC Branch, KEK Theory Center, High Energy Accelerator Research Organization (KEK),<br>Tsukuba 305-0801<br>${ }^{20}$ Forschungszentrum Jülich, 52425 Jülich<br>${ }^{21}$ IKERBASQUE, Basque Foundation for Science, 48013 Bilbao<br>${ }^{22}$ Indian Institute of Science Education and Research Mohali, SAS Nagar, 140306<br>${ }^{23}$ Indian Institute of Technology Bhubaneswar, Satya Nagar 751007

[^0]${ }^{84}$ Department of Physics, Technische Universität München, 85748 Garching<br>${ }^{85}$ Toho University, Funabashi 274-8510<br>${ }^{86}$ Department of Physics, Tohoku University, Sendai 980-8578<br>${ }^{87}$ Earthquake Research Institute, University of Tokyo, Tokyo 113-0032<br>${ }^{88}$ Department of Physics, University of Tokyo, Tokyo 113-0033<br>${ }^{89}$ Tokyo Institute of Technology, Tokyo 152-8550<br>${ }^{90}$ Tokyo Metropolitan University, Tokyo 192-0397<br>${ }^{91}$ Virginia Polytechnic Institute and State University, Blacksburg, Virginia 24061<br>${ }^{92}$ Wayne State University, Detroit, Michigan 48202<br>${ }^{93}$ Yamagata University, Yamagata 990-8560<br>${ }^{94}$ Yonsei University, Seoul 120-749<br>${ }^{95}$ Department of Physics, Fu Jen Catholic University, Taipei 24205

(Received 27 July 2018; published 7 February 2019)


#### Abstract

We report the study of $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$decays using a $772 \times 10^{6} B \bar{B}$ pair data sample recorded on the $\Upsilon(4 S)$ resonance with the Belle detector at KEKB. The following branching fractions are measured: $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}\right)=\left(4.10_{-0.43}^{+0.45} \pm 0.50\right) \times 10^{-6}, \mathcal{B}\left(B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}\right)=$ $\left(3.70_{-0.37}^{+0.39} \pm 0.44\right) \times 10^{-6}, \mathcal{B}\left(\eta_{c} \rightarrow p \bar{\Lambda} K^{-}+\right.$c.c. $)=\left(2.83_{-0.34}^{+0.36} \pm 0.35\right) \times 10^{-3}$ and $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} \phi\right)=$ $(7.95 \pm 2.09 \pm 0.77) \times 10^{-7}$, where c.c. denotes the corresponding charge-conjugation process. The intermediate resonance decays are excluded in the four-body decay measurements. We also find evidence for $\mathcal{B}\left(\eta_{c} \rightarrow \Lambda(1520) \bar{\Lambda}+\right.$ c.c. $)=(3.48 \pm 1.48 \pm 0.46) \times 10^{-3}$ and $\mathcal{B}\left(B^{+} \rightarrow \Lambda(1520) \bar{\Lambda} K^{+}\right)=(2.23 \pm$ $0.63 \pm 0.25) \times 10^{-6}$. No significant signals are found for $J / \psi \rightarrow \Lambda(1520) \bar{\Lambda}+$ c.c. and $B^{+} \rightarrow$ $\bar{\Lambda}(1520) \Lambda K^{+}$; we set the $90 \%$ confidence level upper limits on their decay branching fractions as $<1.80 \times 10^{-3}$ and $<2.08 \times 10^{-6}$, respectively.


DOI: 10.1103/PhysRevD. 99.032003

Baryonic $B$ decays have been studied at the B -factories [1], and many intriguing features have been found. Baryonantibaryon pairs are produced almost collinearly in most baryonic $B$ decays such that their masses peak near threshold. There seems to exist a hierarchical structure in the branching fractions of multibody decays, e.g., $\mathcal{B}\left(B^{0} \rightarrow p \bar{\Lambda}_{c}^{-} \pi^{+} \pi^{-}\right)>\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda}_{c}^{-} \pi^{+}\right)>\mathcal{B}\left(B^{0} \rightarrow p \bar{\Lambda}_{c}^{-}\right)$ [2,3]. The angular distribution of the proton against the energetic meson ( $K^{+}$or $\pi^{-}$for the following cases) in the dibaryon system of $B^{+} \rightarrow p \bar{p} K^{+}$and $B^{0} \rightarrow p \bar{\Lambda} \pi^{-}$show a trend opposite to those predicted by theory [1]. These two decays occur presumably via the $b \rightarrow s g$ penguin process, where $g$ denotes a hard gluon.

Lately, many more interesting phenomena in baryonic $B$ decays have been found by the LHCb experiment, e.g., very rare two-body decays like $B^{0} \rightarrow p \bar{p}$ [4], first evidence for $C P$ violation in baryonic $B$ decays [5], baryonic $B_{s}$ decay [6], baryonic $B_{c}$ decay [7], and many first observations of four-body $B^{0}$ and $B_{s}$ decays [8].

A generalized factorization picture [9] can qualitatively explain some of the experimental findings. However, the

[^1]predicted branching fractions may differ by a factor of ten from experimental measurements, e.g., $B^{0} \rightarrow p \bar{\Lambda} D^{*-}$ [10]. Later theoretical predictions [11] better compare with data after using improved baryonic form factors. It is clear that further studies of baryonic $B$ decays are needed in order to improve theoretical understanding. In this paper, we report measurements of $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$, for which theoretical predictions of $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}\right)$ [12] and $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} \phi\right)$ [13] are available.

The data sample used in this study corresponds to an integrated luminosity of $711 \mathrm{fb}^{-1}$, which contains $772 \times$ $10^{6} B \bar{B}$ pairs produced at the $\Upsilon(4 S)$ resonance. The Belle detector $[14,15]$ is located at the interaction point (IP) of the KEKB asymmetric-energy $e^{+}(3.5 \mathrm{GeV}) e^{-}(8 \mathrm{GeV})$ collider $[16,17]$. It is a large-solid-angle spectrometer comprising six specialized subdetectors: the Silicon Vertex Detector, the 50-layer Central Drift Chamber (CDC), the Aerogel Cherenkov Counter (ACC), the Time-Of-Flight scintillation counter (TOF), the electromagnetic calorimeter (ECL), and the $K_{L}^{0}$ and muon detector (KLM). A superconducting solenoid surrounding all but the KLM produces a 1.5 T magnetic field.

In this analysis, we combine $p \bar{\Lambda} K^{+} K^{-}\left(\bar{p} \Lambda K^{+} K^{+}\right)$to form $B^{+}$candidates. We require charged particles (tracks from $\Lambda$ are excluded) to originate near the IP, less than 1.0 cm away along the positron beam direction and less than 0.2 cm away in the transverse plane. To identify a kaon or a proton track, we use the likelihood information from
the charged-hadron identification system (CDC, ACC, TOF) [18] and apply the same selection criteria as in Ref. [19]. We use information from ECL and KLM to reject charged particles resembling electrons and muons. We require $\Lambda\left(p \pi^{-}\right)$candidates to have a displaced vertex that is consistent with a long-lived particle originating from the IP and a mass between 1.111 and $1.121 \mathrm{GeV} / c^{2}$.

We use the following two variables, $\Delta E \equiv E_{\text {recon }}-E_{\text {beam }}$ and $M_{\mathrm{bc}} \equiv \sqrt{\left(E_{\mathrm{beam}} / c^{2}\right)^{2}-\left(P_{\text {recon }} / c\right)^{2}}$, to identify signal, where $E_{\text {recon }} / P_{\text {recon }}$ and $E_{\text {beam }}$ are the reconstructed $B$ energy/momentum and beam energy measured in the $\Upsilon(4 S)$ rest frame, respectively. We define $5.24<M_{\mathrm{bc}}<$ $5.29 \mathrm{GeV} / c^{2}$ and $|\Delta E|<0.2 \mathrm{GeV}$ as the fit region; $5.27<$ $M_{\mathrm{bc}}<5.29 \mathrm{GeV} / c^{2}$ and $|\Delta E|<0.03 \mathrm{GeV}$ as the signal region.

The dominant background is from the continuum process ( $\left.e^{+} e^{-} \rightarrow q \bar{q}, q=u, d, s, c\right)$. We generate phase space $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$signal events and continuum background using EvtGen [20] and later process them with a GEANT3-based detector simulation program that provides the detector-level information [21]. These Monte Carlo (MC) samples are used to optimize the signal selection criteria. We use a neural network package, Neurobayes [22], for background suppression. There are 21 input variables for the training of Neurobayes: 17 modified Fox-Wolfram moments treating the information of particles involved in the signal $B$ candidate separately from those in the rest of the event $[23,24]$ to distinguish spherical $B \bar{B}$ events from the jetlike $q \bar{q}$ events, the missing mass of each event, the vertex difference between the $B^{+}$ candidate and the accompanying $B$, the angle between $B^{+}$ flight direction and the beam axis in the $\Upsilon(4 S)$ rest frame, and the tagging information for the accompanying $B$ [25]. The output value of Neurobayes is between +1 ( $B \bar{B}$-like) and -1 ( $q \bar{q}$-like). The optimized selection and its related systematic uncertainty is mode dependent.

We consider at most one $B^{+}$candidate in each event: if there are multiple candidates, we select the one with the smallest $\left(\chi_{B-v t x}^{2}+\chi_{\Lambda_{-v t x}}^{2}\right)$, where $\chi_{B(\Lambda) \text { _vtx }}^{2}$ represents the $\chi^{2}$ value of $B(\Lambda)$ vertex fit. The probability to have multiple $B$ candidates is less than $6 \%$ and the success rate of this selection is larger than $92 \%$ according to MC study.

In the investigation of possible intermediate states in $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$, we check the mass spectra from combinations of various final-state particles in and near the signal region. We find many intermediate resonances: $\eta_{c}, J / \psi$ and $\chi_{c 1}$ in $M\left(p \bar{\Lambda} K^{-}\right) ; \phi$ in $M\left(K^{+} K^{-}\right)$; $\Lambda(1520)$ in $M\left(p K^{-}\right)$. As an example, Fig. 1 shows the $p K^{-}$ mass distribution for $p \bar{\Lambda} K^{+} K^{-}$events in and near signal region with all selection cuts applied (including the charmonia veto and $\phi$ veto mentioned below). A clear $\Lambda(1520)$ peak is observed. After removing events in the mass windows of resonances: $2.92<M\left(p \bar{\Lambda} K^{-}\right)<$ $3.11 \mathrm{GeV} / c^{2}$ for $\eta_{c}$ and $J / \psi, 3.49<M\left(p \bar{\Lambda} K^{-}\right)<$ $3.53 \mathrm{GeV} / c^{2}$ for $\chi_{c 1}, 1.01<M\left(K^{+} K^{-}\right)<1.03 \mathrm{GeV} / c^{2}$


FIG. 1. Invariant mass distribution of $p K^{-}$for $p \bar{\Lambda} K^{+} K^{-}$ candidate events.
for $\phi$, and $1.46<M\left(p K^{-}\right)<1.58 \mathrm{GeV} / c^{2}$ for $\Lambda(1520)$, we still observe a large number of signal events. Ignoring other possible but unseen intermediate resonances, we attribute them to signal events of $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$four-body decays. Note that there is no significant $D^{0}$ peak found. We also find a threshold peak mixed with the phase space distribution in the $p \bar{\Lambda}$ mass spectrum. Therefore, we generate signal MC samples with this feature to mimic data. This mixing ratio is mode dependent in order to match with data.

We use an extended unbinned maximum likelihood fit to extract signal yields of $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow$ $\bar{p} \Lambda K^{+} K^{+}$four-body decays. The likelihood function is defined as

$$
\mathcal{L}=\frac{e^{-\left(N_{s}+N_{b}\right)}}{N!} \prod_{i=1}^{N}\left(N_{s} P_{s}\left(\Delta E^{i}, M_{\mathrm{bc}}^{i}\right)+N_{b} P_{b}\left(\Delta E^{i}, M_{\mathrm{bc}}^{i}\right)\right)
$$

where $N$ is the number of total events, $i$ denotes the event index, $N_{s}$ and $N_{b}$ are fit parameters representing the numbers of signal events and background events, respectively; $P_{s}$ and $P_{b}$ are the probability density functions of signal and background, respectively.

Backgrounds like generic $(b \rightarrow c) B$ decays and other rare $(b \rightarrow u, d, s) B$ decays, after investigation of MC simulation, show no peak in the fit region. We combine them with continuum background as the general background to fit with. We use Gaussian functions to model the signal shapes in both $\Delta E$ and $M_{\mathrm{bc}}$, a second-order polynomial function for the background $\Delta E$ distribution and an ARGUS function [26] for the background $M_{\mathrm{bc}}$ distribution. The fit results are displayed in Fig. 2. Note that the possible


FIG. 2. Fit results of four-body decays in projection plots of $\quad \Delta E \quad\left(5.27<M_{b c}<5.29 \mathrm{GeV} / c^{2}\right) \quad$ and $M_{b c} \quad(|\Delta E|<$ 0.03 GeV ). (a), (c) are for the final state $p \bar{\Lambda} K^{+} K^{-}$; (b), (d) are for the final state $\bar{p} \Lambda K^{+} K^{+}$.
feed-down events from $B^{+} \rightarrow p \overline{\Sigma^{0}} K^{+} K^{-}$and $B^{+} \rightarrow$ $\bar{p} \Sigma^{0} K^{+} K^{+}$will form a peak around -0.1 GeV in the $\Delta E$ spectra. The fit bias due to this excess around -0.1 GeV is negligible $(<0.4 \%)$. We apply the same fitting procedure in bins of $M_{p \bar{\Lambda} / \bar{p} \Lambda}$ to determine the signal yields. The corresponding normalized and efficiency-corrected signal yield distributions are shown in Fig. 3.


FIG. 3. Normalized and efficiency-corrected signal yield distributions of $\mathrm{M}(p \bar{\Lambda})$ and $\mathrm{M}(\bar{p} \Lambda)$ for four-body decays. Clear threshold peaks are observed.

Since the signal yield is significant enough, we fix the signal shapes in a similar likelihood fit to extract the signal yields with intermediate resonances $\eta_{c}, J / \psi, \chi_{c 1}, \Lambda(1520)$ and $\phi$. In addition to $\Delta E$ and $M_{\mathrm{bc}}$, we include the invariant mass of an intermediate resonance as a third variable in our fit assuming that the probability density function, $P\left(M_{\text {res }}\right)$, is independent of $P\left(\Delta E, M_{\mathrm{bc}}\right)$. We use the world average mass and width values of these resonances to generate MC samples [2]. For $\eta_{c}$ and $\phi$, we use a Breit-Wigner function convolved with a Gaussian function; for $J / \psi$ and $\chi_{c 1}$, we use the sum of two Gaussian functions in order to fit the corresponding MC mass distributions; for $\Lambda(1520)$, we use one Breit-Wigner function. The obtained signal shapes are fixed in the later data fit. We use a 2 nd-order polynomial function to model the background shape in the resonance mass spectrum. The different components of the fit function are the resonance signal (peaking in all spectra),


FIG. 4. Fit results of $B^{+} \rightarrow \eta_{c} K^{+}\left(\eta_{c} \rightarrow p \bar{\Lambda} K^{-}\right)$and $B^{+} \rightarrow$ $J / \psi K^{+}\left(J / \psi \rightarrow p \bar{\Lambda} K^{-}\right)$with $2.75<M_{p \bar{\Lambda} K^{-}} / M_{\bar{p} \Lambda K^{+}}<3.2 \mathrm{GeV} / c^{2}$ in projection plots of $\Delta E\left(5.27<M_{b c}<5.29 \mathrm{GeV} / c^{2}\right), M_{b c}$ ( $|\Delta E|<0.03 \mathrm{GeV}$ ) and $M_{p \bar{\Lambda} K_{-}^{-}} / M_{\bar{p} \Lambda K^{+}}$(in signal box). (a), (c), (e) are for the final state $p \bar{\Lambda} K^{+} K^{-}$; (b), (d), (f) are for the final state $\bar{p} \Lambda K^{+} K^{+}$. For illustration purpose, we only show signal curve peaking in all spectra and four-body decay as horizontal-line region, and merge all backgrounds as crosshatched region.
four-body decay signal (only peaking in $\Delta E$ and $M_{\mathrm{bc}}$ ), background with resonances produced by other processes (only peaking in $M_{\text {res }}$ ) and nonpeaking background. In contrast to fixed peaking shapes, all non-peaking shapes are floated and determined from the fit. Figure 4 shows the fit results for $B^{+} \rightarrow \eta_{c} K^{+}\left(\eta_{c} \rightarrow p \bar{\Lambda} K^{-}\right)$and $B^{+} \rightarrow$ $J / \psi K^{+}\left(J / \psi \rightarrow p \bar{\Lambda} K^{-}\right)$. Figure 5 shows the fit result of $B^{+} \rightarrow \chi_{c 1} K^{+}$. Figure 6 shows the fit result of $B^{+} \rightarrow p \bar{\Lambda} \phi$. After applying charmonia veto and $\phi$ veto, the fit results of $B^{+} \rightarrow \Lambda(1520) \bar{\Lambda} K^{+}$and $B^{+} \rightarrow \bar{\Lambda}(1520) \Lambda K^{+}$are shown in Fig. 7.

In the mass window of $\eta_{c}$, we observe a clear resonance in $M\left(p K^{-}\right)$, at the nominal mass of $\Lambda(1520)$. So there is a non-negligible fraction of $\eta_{c} \rightarrow p \bar{\Lambda} K^{-}$from $\eta_{c} \rightarrow$ $\Lambda(1520) \bar{\Lambda}$. In the same manner, we fit the $\Delta E, M_{b c}$, $M\left(p \bar{\Lambda} K^{-}\right)$and $M\left(p K^{-}\right)$spectra simultaneously in order to determine the yields of $\eta_{c} \rightarrow \Lambda(1520) \bar{\Lambda}$ and $J / \psi \rightarrow$ $\Lambda(1520) \bar{\Lambda}$. The fit results are shown in Fig. 8.


FIG. 5. Fit results of $B^{+} \rightarrow \chi_{c 1} K^{+}$with $3.42<M_{p \bar{\Lambda} K^{-}} /$ $M_{\bar{p} \Lambda K^{+}}<3.6 \mathrm{GeV} / c^{2}$ in projection plots of $\Delta E\left(5.27<M_{b c}<\right.$ $\left.5.29 \mathrm{GeV} / c^{2}\right), M_{b c}(|\Delta E|<0.03 \mathrm{GeV})$ and $M_{p \bar{\Lambda} K^{-}} / M_{\bar{p} \Lambda K^{+}}$ (in signal box). (a), (c), (e) are for the final state $p \bar{\Lambda} K^{+} K^{-}$; (b), (d), (f) are for the final state $\bar{p} \Lambda K^{+} K^{+}$. For illustration purpose, we only show signal curve peaking in all spectra and four-body decay as horizontal-line region, and merge all backgrounds as cross-hatched region.

The value of the fit significance is defined by $\sqrt{-2 \times \ln \left(\mathcal{L}_{0} / \mathcal{L}_{s}\right)}(\sigma)$, where $\mathcal{L}_{0}$ is the likelihood with null signal yield and $\mathcal{L}_{s}$ is the likelihood with measured yield. In the above calculation, we have used the likelihood function which is smeared by considering the additive systematic uncertainties that would affect the fitted yield. For those modes with fit significance less than $3 \sigma$, we integrate the smeared likelihood function in order to find out the upper limit yield at the $90 \%$ confidence level. That is, to calculate N that satisfies

$$
\int_{0}^{N} \mathcal{L}(n) d n=0.9 \int_{0}^{\infty} \mathcal{L}(n) d n
$$

where $\mathcal{L}(n)$ denotes the likelihood function with the condition that the number of signal events is fixed to the value $n$.

For systematic uncertainty, we consider tracking uncertainty per track for charged particles $(0.35 \%$ for each charged particle and $0.70 \%$ for $\Lambda$ ). The uncertainty of the estimated number of $B \bar{B}$ pairs is $1.4 \%$. The $\Lambda$ selection uncertainty is determined by the difference of the flightdistance distribution between data and MC (3.0\%). Some of systematic uncertainties are mode-dependent. The uncertainty in proton/antiproton identification is determined by using the study of $\Lambda / \bar{\Lambda}(0.38 \%$ to $0.53 \%)$ in data, while the uncertainty in kaon identification is determined from the study of $D^{*+} \rightarrow D^{0} \pi^{+}, D^{0} \rightarrow K^{-} \pi^{+}$in data $(2.0 \%$ to $3.7 \%)$. We generate two kinds of signal MC: one considering a threshold enhancement in the dibaryonic


FIG. 6. Fit result of $B^{+} \rightarrow p \bar{\Lambda} \phi$ with $1.00<M_{\mathrm{K}^{+} \mathrm{K}^{-}}<$ $1.08 \mathrm{GeV} / c^{2}$ in projection plots of $\Delta E\left(5.27<M_{b c}<\right.$ $\left.5.29 \mathrm{GeV} / c^{2}\right), M_{b c}(|\Delta E|<0.03 \mathrm{GeV})$ and $M_{K^{+} K^{-}}$(in signal box). For illustration purpose, we only show signal curve peaking in all spectra and four-body decay as horizontal-line region, and merge all backgrounds as cross-hatched region.


FIG. 7. Fit results of $B^{+} \rightarrow \Lambda(1520) \bar{\Lambda} K^{+}$and $B^{+} \rightarrow$ $\bar{\Lambda}(1520) \Lambda K^{+}$with $1.44<M_{p K^{-}} / M_{\bar{p} K^{+}}<1.8 \mathrm{GeV} / c^{2}$ in projection plots of $\Delta E \quad\left(5.27<M_{b c}<5.29 \mathrm{GeV} / c^{2}\right), \quad M_{b c}$ ( $|\Delta E|<0.03 \mathrm{GeV}$ ) and $M_{p K_{-}^{-}} / M_{\bar{p} K^{+}}$(in signal box). (a), (c), (e) are for the final state $p \bar{\Lambda} K^{+} K^{-}$; (b), (d), (f) are for the final state $\bar{p} \Lambda K^{+} K^{+}$. For illustration purpose, we only show signal curve peaking in all spectra and four-body decay as horizontal-line region, and merge all backgrounds as crosshatched region.
system, the other with only phase space decays, and we mix the two samples to mimic the real data. The MC modeling uncertainty is set to be the larger difference in reconstruction efficiency between the threshold enhancement MC and phase space $\mathrm{MC}(0.52 \%$ to $9.3 \%)$. The smallest value, $0.52 \%$, is for $B^{+} \rightarrow \eta_{c} K^{+}$due to limited phase space. The uncertainty from the fixed signal probability density function is obtained by varying all of the shape variables by one sigma and refitting ( $2.7 \%$ to $3.3 \%$ ). The statistical uncertainty of the MC reconstruction efficiency is $0.31 \%$ to $0.47 \%$. The uncertainty of $q \bar{q}$ suppression is obtained from the reconstruction efficiency difference with and without the cut ( $0.50 \%$ to $5.0 \%$ ). We apply the $D^{0}$ veto to redo the analysis and attribute the possible veto uncertainty $2.2 \%$ to $7.4 \%$, where the statistical uncertainty from data is included. All the above uncertainties are combined in quadrature to obtain the total systematic uncertainties ( $5.9 \%$ to $12 \%$ ).


FIG. 8. Fit results of $B^{+} \rightarrow \eta_{c} K^{+}\left(\eta_{c} \rightarrow \Lambda(1520) \bar{\Lambda}\right)$ and $B^{+} \rightarrow$ $J / \psi K^{+} \quad(J / \psi \rightarrow \Lambda(1520) \bar{\Lambda})$ in projection plots of $\Delta E$ (5.27< $M_{b c}<5.29, \quad 2.9<M_{p \bar{\Lambda} K_{2}^{-}} / M_{\bar{p} \Lambda K^{+}}<3.12 \mathrm{GeV} / c^{2}$ and $\left.1.45<M_{p K^{-}} / M_{\bar{p} K^{+}}<1.58 \mathrm{GeV} / c^{2}\right), \quad M_{b c} \quad(|\Delta E|<0.03 \mathrm{GeV}$, $2.9<M_{p \bar{\Lambda} K^{-}} / M_{\bar{p} \Lambda K^{+}}<3.12 \mathrm{GeV} / c^{2}$ and $1.45<M_{p K^{-}} / M_{\bar{p} K^{+}}<$ $\left.1.58 \mathrm{GeV} / c^{2}\right), \quad M_{p \bar{\Lambda} K^{-}} / M_{\bar{p} \Lambda K^{+}}$(in signal box and $1.45<$ $M_{p K^{-}} / M_{\bar{p} K^{+}}<1.58 \mathrm{GeV} / c^{2}$ ) and $M_{p K^{-}} / M_{\bar{p} K^{+}}$(in signal box and $2.9<M_{p \bar{\Lambda} K^{-}} / M_{\bar{p} \Lambda K^{+}}<3.12 \mathrm{GeV} / c^{2}$ ). (a), (c), (e), (g) are for the final state $p \bar{\Lambda} K^{+} K^{-}$; (b), (d), (f), (h) are for the final state $\bar{p} \Lambda K^{+} K^{+}$. For illustration purpose, we only show signal curve peaking in all spectra, and merge other $B$ decay signals as horizontal-line region and all backgrounds as cross-hatched region.

Table I summarizes the fit yields, reconstruction efficiencies and corresponding systematic uncertainties of significant and evident modes; Table II summarizes the upper limit yields and reconstruction efficiencies for modes with fit significance less than $3 \sigma$. Note that the

TABLE I. Signal yields $\left(N_{s}\right)$, reconstruction efficiencies ( $\varepsilon_{\text {eff }}$ ), systematic uncertainties (sys) and significances ( $\sigma$ ) from extended unbinned maximum likelihood fits for modes with fit significance greater than $3 \sigma$.

| Mode | $N_{s}$ | $\varepsilon_{\text {eff }}(\%)$ | sys $(\%)$ | $\sigma$ |
| :--- | :---: | ---: | :---: | :---: |
| $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$ | $190.1_{-19.6}^{+20.3}$ | 5.84 | 12.2 | 11.7 |
| $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$ | $188.0_{-18.4}^{+19.2}$ | 6.40 | 11.8 | 12.7 |
| $\left(B^{+} \rightarrow \eta_{c} K^{+}\right) \times\left(\eta_{c} \rightarrow p \bar{\Lambda} K^{-}\right)$ | $89.7_{-13.1}^{+13.3}$ | 7.19 | 5.91 | 8.46 |
| $\left(B^{+} \rightarrow \eta_{c} K^{+}\right) \times\left(\eta_{c} \rightarrow \bar{p} \Lambda K^{+}\right)$ | $67.0_{-13.3}^{+14.1}$ | 7.36 | 7.55 | 5.63 |
| Total significance of the $\eta_{c}$ mode |  |  |  |  |
| $\left(B^{+} \rightarrow J / \psi K^{+}\right) \times\left(J / \psi \rightarrow p \bar{\Lambda} K^{-}\right)$ | $19.0_{-5.0}^{+5.7}$ | 6.57 | 7.83 | 4.92 |
| $\left(B^{+} \rightarrow J / \psi K^{+}\right) \times\left(J / \psi \rightarrow \bar{p} \Lambda K^{+}\right)$ | $25.5_{-5.9}^{+6.6}$ | 6.56 | 5.90 | 5.50 |
| Total significance of the $J / \psi$ mode |  |  |  | 7.38 |
| $\left(B^{+} \rightarrow \chi_{c 1} K^{+}\right) \times\left(\chi_{c 1} \rightarrow p \bar{\Lambda} K^{-}\right)$ | $10.2_{-3.9}^{+4.6}$ | 7.39 | 11.9 | 3.18 |
| $\left(B^{+} \rightarrow \chi_{c 1} K^{+}\right) \times\left(\chi_{c 1} \rightarrow \bar{p} \Lambda K^{+}\right)$ | $13.4_{-4.3}^{+5.0}$ | 6.38 | 10.5 | 3.79 |
| Total significance of the $\chi_{c 1}$ mode |  |  |  | 4.95 |
| $\left(B^{+} \rightarrow p \bar{\Lambda} \phi\right) \times\left(\phi \rightarrow K^{+} K^{-}\right)$ | $23.2 \pm 6.1$ | 7.52 | 5.15 |  |
| $\left(B^{+} \rightarrow \Lambda(1520) \bar{\Lambda} K^{+}\right) \times\left(\Lambda(1520) \rightarrow p K^{-}\right)$ | $30.3 \pm 8.6$ | 7.60 | 10.5 | 4.08 |
| $\left(B^{+} \rightarrow \eta_{c} K^{+}\right) \times\left(\eta_{c} \rightarrow \Lambda(1520) \bar{\Lambda}\right) \times\left(\Lambda(1520) \rightarrow p K^{-}\right)$ | $19.2 \pm 12.5$ | 7.58 | 9.68 | 1.97 |
| $\left(B^{+} \rightarrow \eta_{c} K^{+}\right) \times\left(\eta_{c} \rightarrow \bar{\Lambda}(1520) \Lambda\right) \times\left(\bar{\Lambda}(1520) \rightarrow \bar{p} K^{+}\right)$ | $23.9 \pm 13.4$ | 6.95 | 6.40 | 2.50 |
| Total significance of the $\eta_{c}$ submode |  |  | 3.18 |  |

TABLE II. Upper limits of yields ( $N_{\text {upper }}$ ) and reconstruction efficiencies ( $\varepsilon_{\text {eff }}$ ) from extended unbinned maximum likelihood fits for modes with fit significance less than $3 \sigma$. For the $J / \psi$ decay, we determine its upper limit of branching fraction with the combined $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$data samples.

| Mode | $N_{\text {upper }}$ | $\varepsilon_{\text {eff }}(\%)$ | comment |
| :--- | :---: | :---: | :---: |
| $\left(B^{+} \rightarrow J / \psi K^{+}\right) \times(J / \psi \rightarrow \Lambda(1520) \bar{\Lambda}) \times\left(\Lambda(1520) \rightarrow p K^{-}\right)$ | 17.2 | 5.88 | $90 \%$ C.L. |
| $\left(B^{+} \rightarrow \bar{\Lambda}(1520) \Lambda K^{+}\right) \times\left(\bar{\Lambda}(1520) \rightarrow \bar{p} K^{+}\right)$ | 19.8 | 5.70 | $90 \%$ C.L. |

reconstruction efficiencies in Table I and Table II include the decay branching fraction $63.9 \%$ for the long-lived $\Lambda \rightarrow p \pi^{-}$in the MC simulation and efficiencies have been corrected for the MC-data difference of the proton/kaon identification.

TABLE III. Summary of measured branching fractions. Here c.c. stands for the corresponding charge-conjugation process. The listed four-body modes exclude the mentioned intermediate resonances.

| Mode | Branching fraction |
| :--- | :---: |
| $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$ | $\left(4.10_{-0.43}^{+0.45} \pm 0.50\right) \times 10^{-6}$ |
| $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$ | $\left(3.70_{-0.37}^{+0.39} \pm 0.44\right) \times 10^{-6}$ |
| $B^{+} \rightarrow p \bar{\Lambda} \phi$ | $(7.95 \pm 2.09 \pm 0.77) \times 10^{-7}$ |
| $\eta_{c} \rightarrow p \bar{\Lambda} K^{-}+$c.c. | $\left(2.83_{-0.34}^{+0.36} \pm 0.35\right) \times 10^{-3}$ |
| $J / \psi \rightarrow p \bar{\Lambda} K^{-}+$c.c. | $\left(8.32_{-1.45}^{+1.63} \pm 0.49\right) \times 10^{-4}$ |
| $\chi_{c 1} \rightarrow p \bar{\Lambda} K^{-}+$c.c. | $\left(9.15_{-2.25}^{+2.63} \pm 0.86\right) \times 10^{-4}$ |
| $B^{+} \rightarrow \Lambda(1520) \bar{\Lambda} K^{+}$ | $(2.23 \pm 0.63 \pm 0.25) \times 10^{-6}$ |
| $\eta_{c} \rightarrow \Lambda(1520) \bar{\Lambda}+$ c.c. | $(3.48 \pm 1.48 \pm 0.46) \times 10^{-3}$ |
| $J / \psi \rightarrow \Lambda(1520) \bar{\Lambda}+$ c.c. | $<1.80 \times 10^{-3}$ |
| $B^{+} \rightarrow \bar{\Lambda}(1520) \Lambda K^{+}$ | $<2.08 \times 10^{-6}$ |

We use the world average values [2] of $\mathcal{B}\left(\Upsilon(4 S) \rightarrow B^{+} B^{-}\right), \mathcal{B}\left(\phi \rightarrow K^{+} K^{-}\right), \mathcal{B}\left(\Lambda(1520) \rightarrow p K^{-}\right)$, $\mathcal{B}\left(B^{+} \rightarrow \eta_{c} K^{+}\right), \mathcal{B}\left(B^{+} \rightarrow J / \psi K^{+}\right)$and $\mathcal{B}\left(B^{+} \rightarrow \chi_{c 1} K^{+}\right)$, to obtain the results listed in Table III. The measured branching fractions of four-body decay of $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$ and $B^{+} \rightarrow p \bar{\Lambda} \phi$ are consistent with theoretical predictions [12,13]. Note that $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}\right)$is compatible with $\mathcal{B}\left(B^{+} \rightarrow p \bar{\Lambda} \pi^{+} \pi^{-}\right)$[27].

In summary, using a sample of $772 \times 10^{6} B \bar{B}$ pair events, we measure the branching fractions of the fourbody decays $B^{+} \rightarrow p \bar{\Lambda} K^{+} K^{-}$and $B^{+} \rightarrow \bar{p} \Lambda K^{+} K^{+}$with intermediate resonance modes being excluded. The feature of a threshold enhancement of the dibaryon system persists, but with a non-negligible phase space contribution. We also observe the three-body decay of $\eta_{c} \rightarrow p \bar{\Lambda} K^{-}+$c.c. The measured $\mathcal{B}\left(J / \psi \rightarrow p \bar{\Lambda} K^{-}+\right.$c.c. $)$is in good agreement with the world average [2]. We also confirm the observation of $\chi_{c 1} \rightarrow p \bar{\Lambda} K^{-}+$c.c. These decay amplitudes can be useful for a better understanding of the charmonium system. We observe the charmless decay $B^{+} \rightarrow p \bar{\Lambda} \phi$ with a smaller branching fraction than that of the four-body decay. Its signal yield is not significant enough to perform an angular analysis.

## ACKNOWLEDGMENTS

We thank the KEKB group for excellent operation of the accelerator; the KEK cryogenics group for efficient solenoid operations; and the KEK computer group, the NII, and PNNL/EMSL for valuable computing and SINET5 network support. We acknowledge support from MEXT, JSPS and Nagoya's TLPRC (Japan); ARC (Australia); FWF (Austria); NSFC and CCEPP (China);

MSMT (Czechia); CZF, DFG, EXC153, and VS (Germany); DST (India); INFN (Italy); MOE, MSIP, NRF, RSRI, FLRFAS project and GSDC of KISTI (Korea); MNiSW and NCN (Poland); MES under Contract No. 14.W03.31.0026 (Russia); ARRS (Slovenia); IKERBASQUE and MINECO (Spain); SNSF (Switzerland); MOE and MOST (Taiwan); and DOE and NSF (USA).
[1] A. J. Bevan et al., Eur. Phys. J. C 74, 3026 (2014).
[2] C. Patrignani et al. (Particle Data Group), Chin. Phys. C 40, 100001 (2016).
[3] Through out this paper, inclusion of charge-conjugate mode is always implied if the charge-conjugate final states are not specifically mentioned together.
[4] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 119, 232001 (2017).
[5] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 113, 141801 (2014).
[6] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 119, 041802 (2017).
[7] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 113, 152003 (2014).
[8] R. Aaij et al. (LHCb Collaboration), Phys. Rev. D 96, 051103 (2017).
[9] C.-H. Chen, H.-Y. Cheng, C. Q. Geng, and Y. K. Hsiao, Phys. Rev. D 78, 054016 (2008).
[10] Y.-Y.Chang et al. (Belle Collaboration), Phys. Rev. Lett. 115, 221803 (2015).
[11] Y. K. Hsiao and C. Q. Geng, Phys. Rev. D 93, 034036 (2016).
[12] Y. Hsiao and C. Geng, Phys. Lett. B 770, 348 (2017).
[13] C. Q. Geng and Y. K. Hsiao, Phys. Rev. D 85, 017501 (2012).
[14] A. Abashian et al. (Belle Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 479, 117 (2002).
[15] J. Brodzicka et al., Prog. Theor. Exp. Phys. 04D001 (2012).
[16] S. Kurokawa and E. Kikutani, Nucl. Instrum. Methods Phys. Res., Sect. A 499, 1 (2003).
[17] T. Abe et al., Prog. Theor. Exp. Phys. 03A001 (2013).
[18] E. Nakano et al. (Belle Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 494, 402 (2002).
[19] J.-T. Wei et al. (Belle Collaboration), Phys. Lett. B 659, 80 (2008).
[20] D. J. Lange, Nucl. Instrum. Methods Phys. Res., Sect. A 462, 152 (2001).
[21] R. Brun et al., CERN Report No. DD/EE/84-1, 1984.
[22] M. Feindt and U. Kerzel, Nucl. Instrum. Methods Phys. Res., Sect. A 559, 190 (2006).
[23] G. Fox and S. Wolfram, Phys. Rev. Lett. 41, 1581 (1978).
[24] S. H. Lee et al. (Belle Collaboration), Phys. Rev. Lett. 91, 261801 (2003).
[25] H. Kakuno et al., Nucl. Instrum. Methods Phys. Res., Sect. A 533, 516 (2004).
[26] H. Albrecht et al. (ARGUS Collaboration), Phys. Lett. B 210, 263 (1988).
[27] P. Chen et al. (Belle Collaboration), Phys. Rev. D 80, 111103 (2009).


[^0]:    ${ }^{24}$ Indian Institute of Technology Guwahati, Assam 781039
    ${ }^{25}$ Indian Institute of Technology Hyderabad, Telangana 502285
    ${ }^{26}$ Indian Institute of Technology Madras, Chennai 600036
    ${ }^{27}$ Indiana University, Bloomington, Indiana 47408
    ${ }^{28}$ Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049
    ${ }^{29}$ Institute of High Energy Physics, Vienna 1050
    ${ }^{30}$ Institute for High Energy Physics, Protvino 142281
    ${ }^{31}$ INFN-Sezione di Napoli, 80126 Napoli
    ${ }^{32}$ INFN-Sezione di Torino, 10125 Torino
    ${ }^{33}$ Advanced Science Research Center, Japan Atomic Energy Agency, Naka 319-1195
    ${ }^{34}$ J. Stefan Institute, 1000 Ljubljana
    ${ }^{35}$ Kanagawa University, Yokohama 221-8686
    ${ }^{36}$ Institut für Experimentelle Teilchenphysik, Karlsruher Institut für Technologie, 76131 Karlsruhe
    ${ }^{37}$ Kennesaw State University, Kennesaw, Georgia 30144
    ${ }^{38}$ King Abdulaziz City for Science and Technology, Riyadh 11442
    ${ }^{39}$ Department of Physics, Faculty of Science, King Abdulaziz University, Jeddah 21589
    ${ }^{40}$ Korea Institute of Science and Technology Information, Daejeon 305-806
    ${ }^{41}$ Korea University, Seoul 136-713
    ${ }^{42}$ Kyungpook National University, Daegu 702-701
    ${ }^{43}$ LAL, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, Orsay
    ${ }^{44}$ École Polytechnique Fédérale de Lausanne (EPFL), Lausanne 1015
    ${ }^{45}$ P.N. Lebedev Physical Institute of the Russian Academy of Sciences, Moscow 119991
    ${ }^{46}$ Faculty of Mathematics and Physics, University of Ljubljana, 1000 Ljubljana
    ${ }^{47}$ Ludwig Maximilians University, 80539 Munich
    ${ }^{48}$ Luther College, Decorah, Iowa 52101
    ${ }^{49}$ University of Malaya, 50603 Kuala Lumpur
    ${ }^{50}$ University of Maribor, 2000 Maribor
    ${ }^{51}$ Max-Planck-Institut für Physik, 80805 München
    ${ }^{52}$ School of Physics, University of Melbourne, Victoria 3010
    ${ }^{53}$ University of Mississippi, University, Mississippi 38677
    ${ }^{54}$ University of Miyazaki, Miyazaki 889-2192
    ${ }^{55}$ Moscow Physical Engineering Institute, Moscow 115409
    ${ }^{56}$ Moscow Institute of Physics and Technology, Moscow Region 141700
    ${ }^{57}$ Graduate School of Science, Nagoya University, Nagoya 464-8602
    ${ }^{58}$ Kobayashi-Maskawa Institute, Nagoya University, Nagoya 464-8602
    ${ }^{59}$ Università di Napoli Federico II, 80055 Napoli
    ${ }^{60}$ Nara Women's University, Nara 630-8506
    ${ }^{61}$ National Central University, Chung-li 32054
    ${ }^{62}$ National United University, Miao Li 36003
    ${ }^{63}$ Department of Physics, National Taiwan University, Taipei 10617
    ${ }^{64}$ H. Niewodniczanski Institute of Nuclear Physics, Krakow 31-342
    ${ }^{65}$ Nippon Dental University, Niigata 951-8580
    ${ }^{66}$ Niigata University, Niigata 950-2181
    ${ }^{67}$ Novosibirsk State University, Novosibirsk 630090
    ${ }^{68}$ Osaka City University, Osaka 558-8585
    ${ }^{69}$ Pacific Northwest National Laboratory, Richland, Washington 99352
    ${ }^{70}$ Panjab University, Chandigarh 160014
    ${ }^{71}$ Peking University, Beijing 100871
    ${ }^{72}$ University of Pittsburgh, Pittsburgh, Pennsylvania 15260
    ${ }^{73}$ Theoretical Research Division, Nishina Center, RIKEN, Saitama 351-0198
    ${ }^{74}$ University of Science and Technology of China, Hefei 230026
    ${ }^{75}$ Showa Pharmaceutical University, Tokyo 194-8543
    ${ }^{76}$ Soongsil University, Seoul 156-743
    ${ }^{77}$ University of South Carolina, Columbia, South Carolina 29208
    ${ }^{78}$ Stefan Meyer Institute for Subatomic Physics, Vienna 1090
    ${ }^{79}$ Sungkyunkwan University, Suwon 440-746
    ${ }^{80}$ School of Physics, University of Sydney, New South Wales 2006
    ${ }^{81}$ Department of Physics, Faculty of Science, University of Tabuk, Tabuk 71451
    ${ }^{82}$ Tata Institute of Fundamental Research, Mumbai 400005
    ${ }^{83}$ Excellence Cluster Universe, Technische Universität München, 85748 Garching

[^1]:    Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP ${ }^{3}$.

